

Nuclear Weak Processes of Astrophysical Interest

Toshio Suzuki
Nihon University



Primosten June. 10, 2011

○ **ν -nucleus reactions**

- **ν - ^{12}C reactions and synthesis of light elements by supernova ν**

- **ν - ^{13}C reactions; effects of contamination of ^{13}C (1.1%) on ν - ^{12}C reactions**

- **ν -induced reactions on ^{16}O**

- **$^{40}\text{Ar} (\nu, e^-) ^{40}\text{K}$ solar ν -reactions**

- **ν - ^{56}Fe ν - ^{56}Ni and synthesis of Mn**

○ **e-capture on Ni isotopes in stellar environments**

- **New shell model Hamiltonians with proper tensor components, which give successful description of spin responses in nuclei**

New shell model Hamiltonians

→ success in better description of spin modes in nuclei

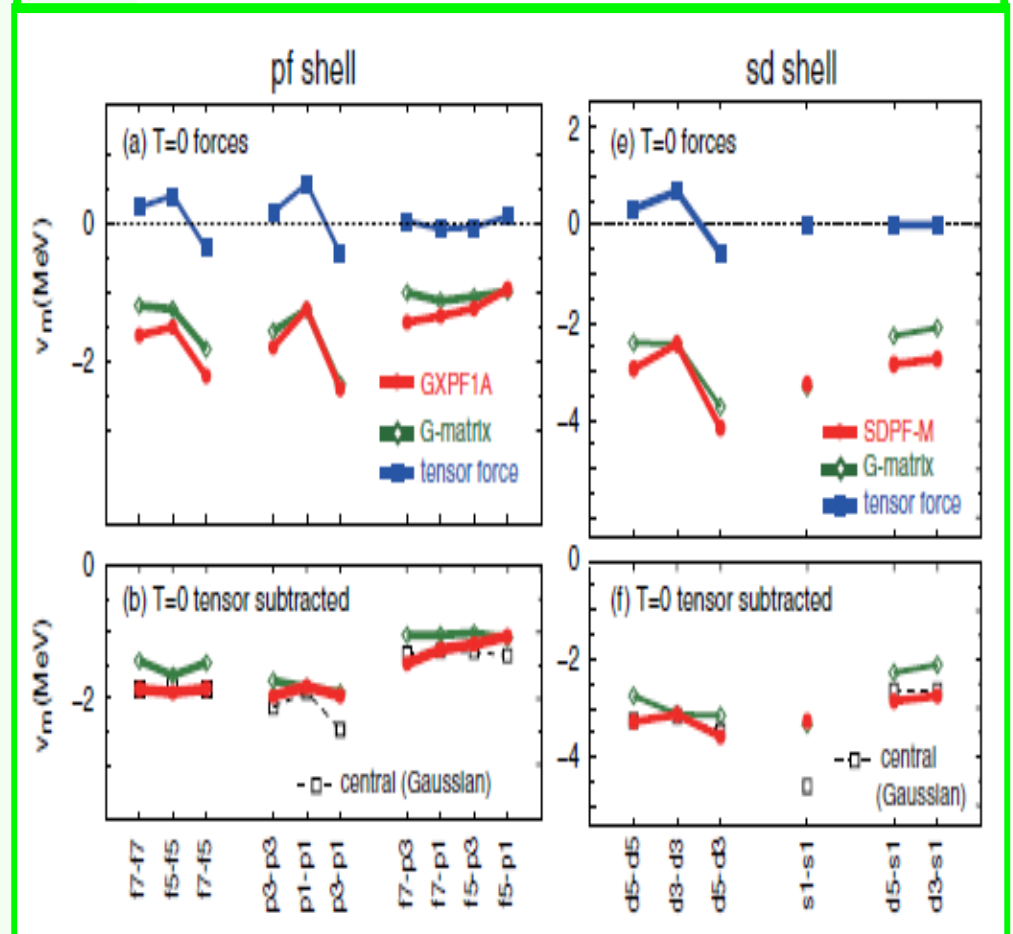
- Important roles of tensor force
→ SFO (p, p-sd)
(Suzuki-Fujimoto-Otsuka)

- Shell evolutions
- GT transitions and magnetic moments

- Monopole-based universal interaction (VMU)

Monopole terms of V_{NN}

$$V_M^T(j_1 j_2) = \frac{\sum_J (2J + 1) \langle j_1 j_2; JT | V | j_1 j_2; JT \rangle}{\sum_J (2J + 1)}$$



tensor force

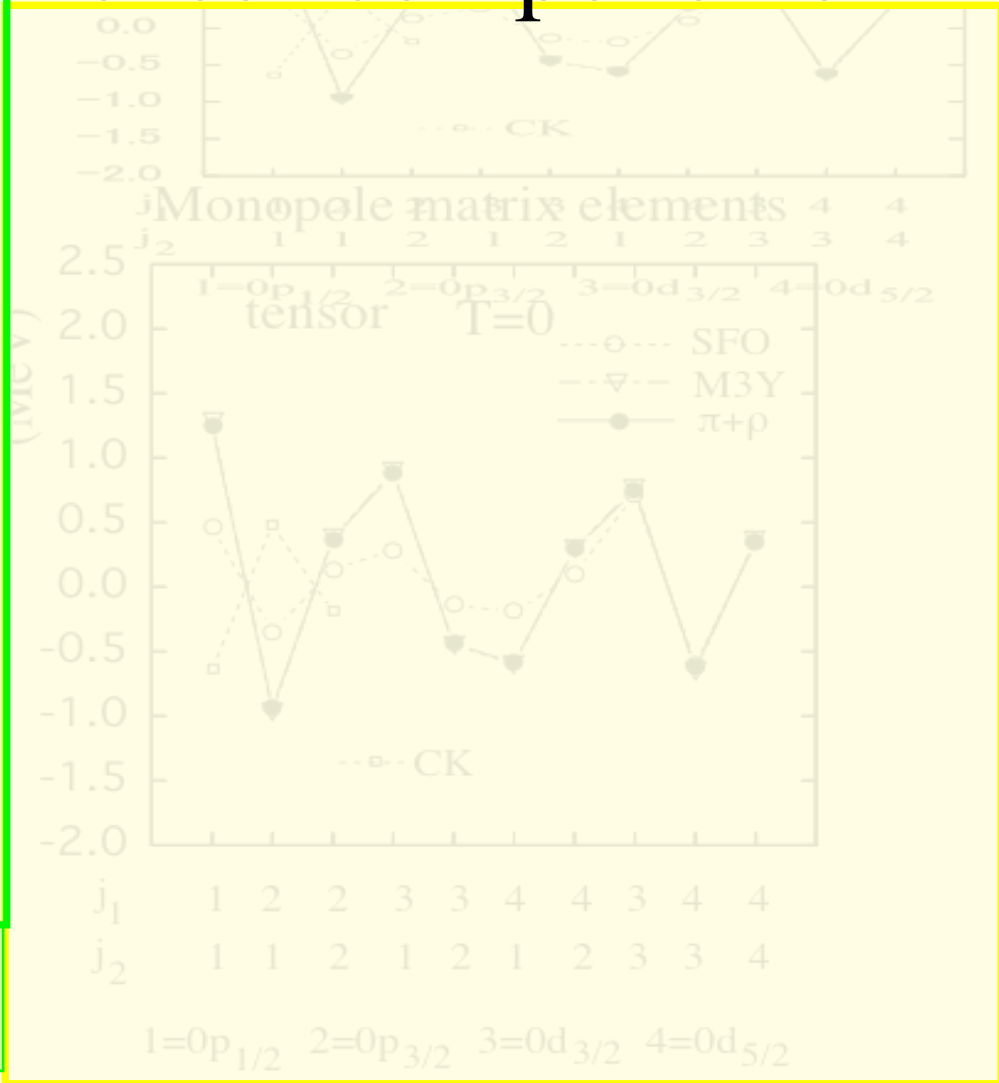
SFO

Suzuki, Fujimoto, Otsuka, PR C67 (2003)

p-sd shell

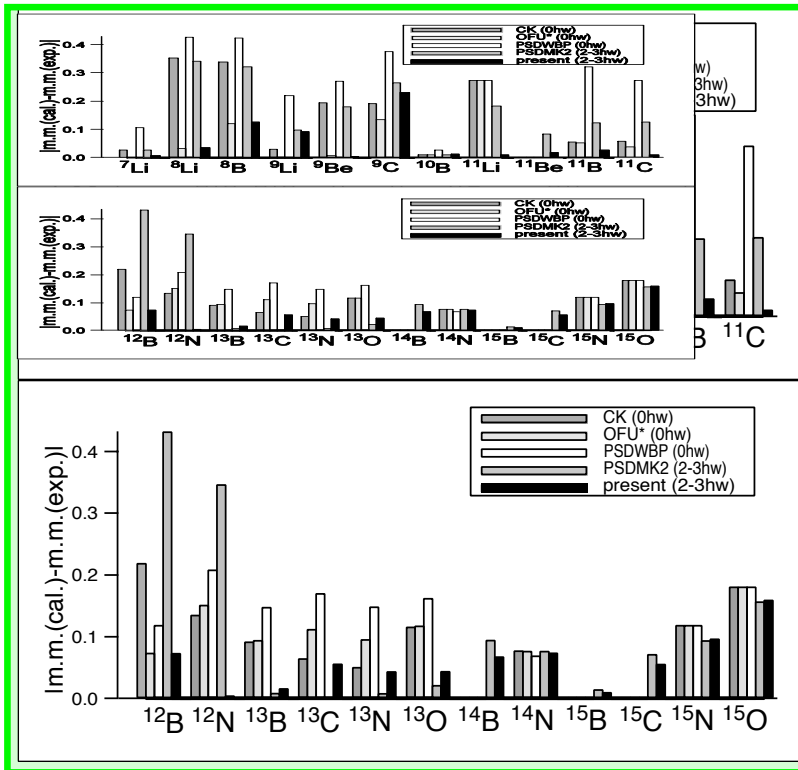
$$V = V_C (\text{central}) + V_T (\text{tensor}) + V_{LS} (\text{LS})$$

Tensor components



monopole T=0
 CK → SFO p_{3/2}-p_{1/2} -1.9 MeV

Magnetic moments of p-shell nuclei

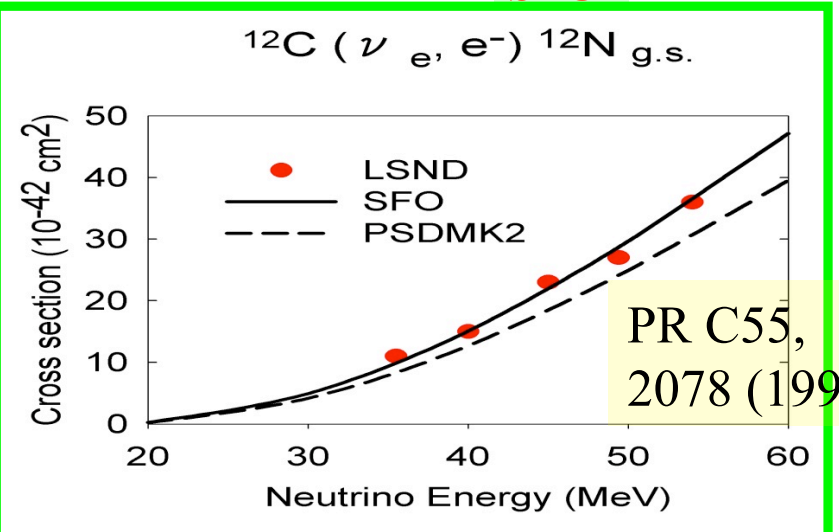
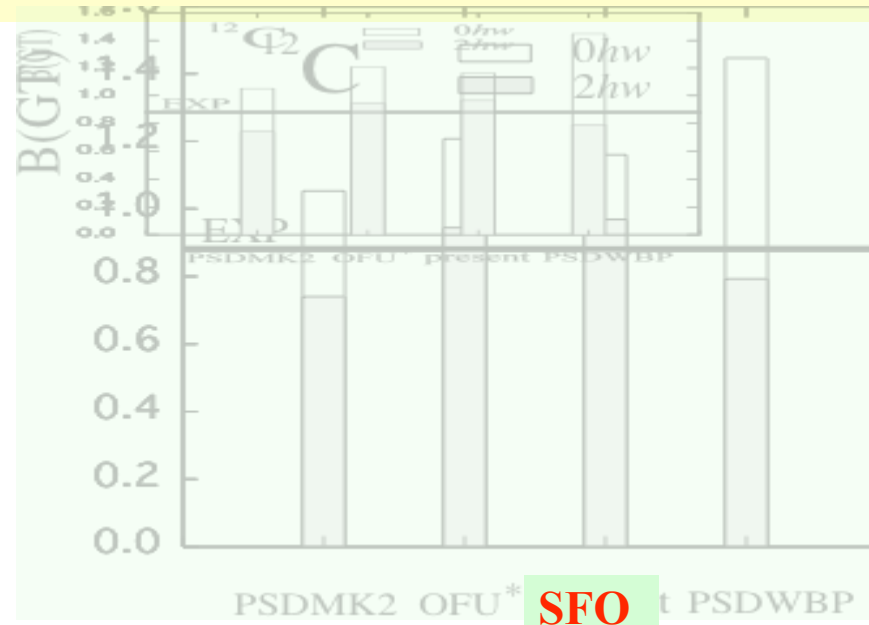


present = **SFO** Suzuki, Fujimoto, Otsuka, PR C67 (2003)

Space: up to 2-3 hw

SFO*: $g_A^{\text{eff}}/g_A = 0.95$
 B(GT: ${}^{12}\text{C}$)_{cal} = experiment

B(GT) for ${}^{12}\text{C} \rightarrow {}^{12}\text{N}$

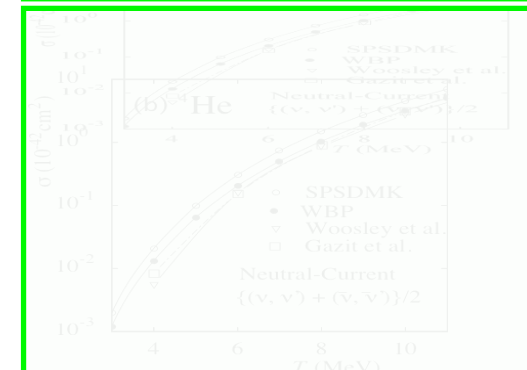
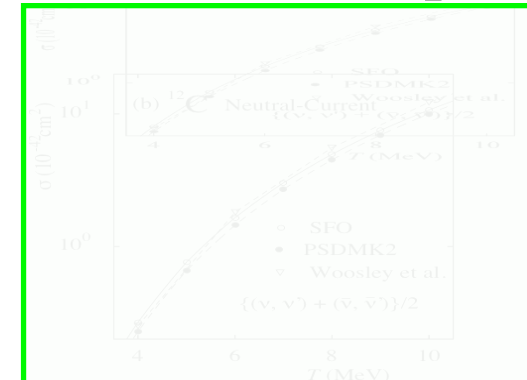
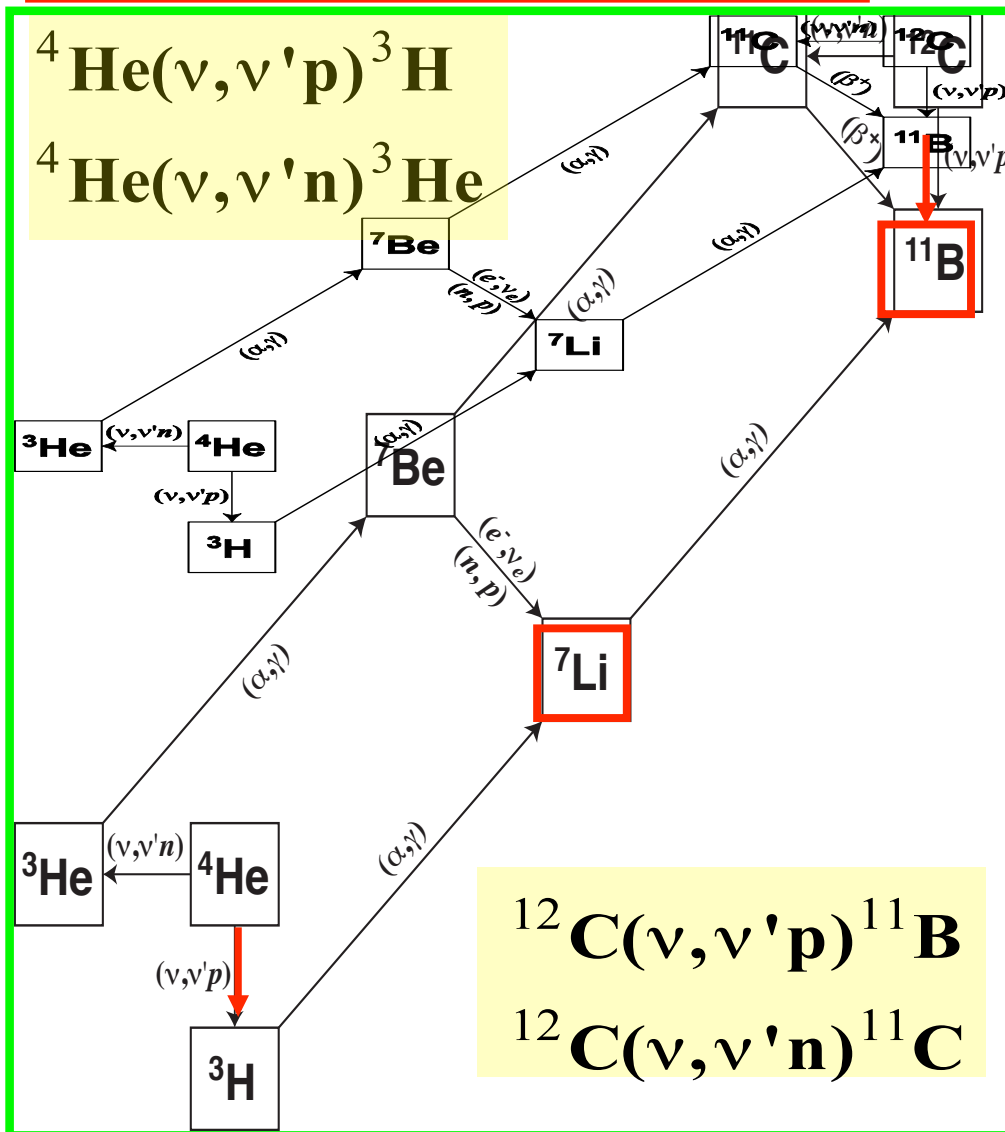


Suzuki, Chiba, Yoshida, Kajino, Otsuka, PR C74, 034307, (2006).

Nucleosynthesis processes of light elements

Enhancement of ^{11}B and ^7Li in supernova explosions

Cross sections for Supernova Neutrinos with temperature T



Effects of contamination of ^{13}C on inclusive ν - ^{12}C reaction cross sections

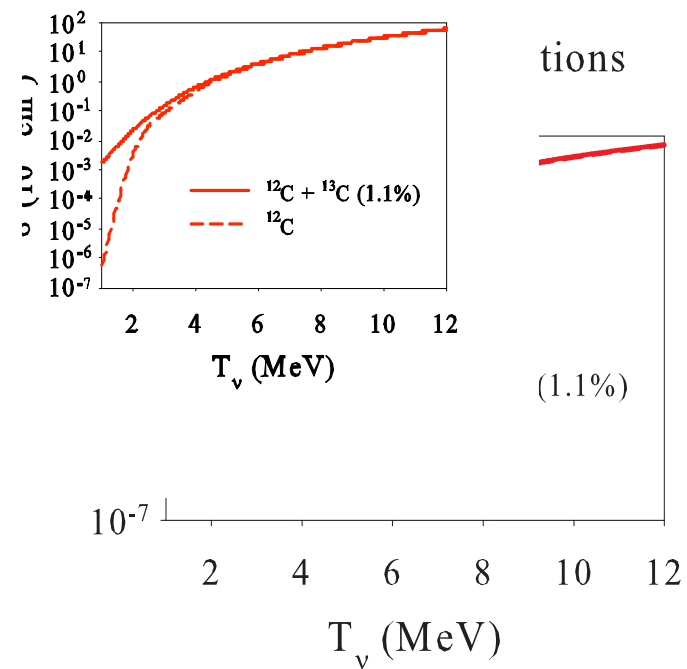
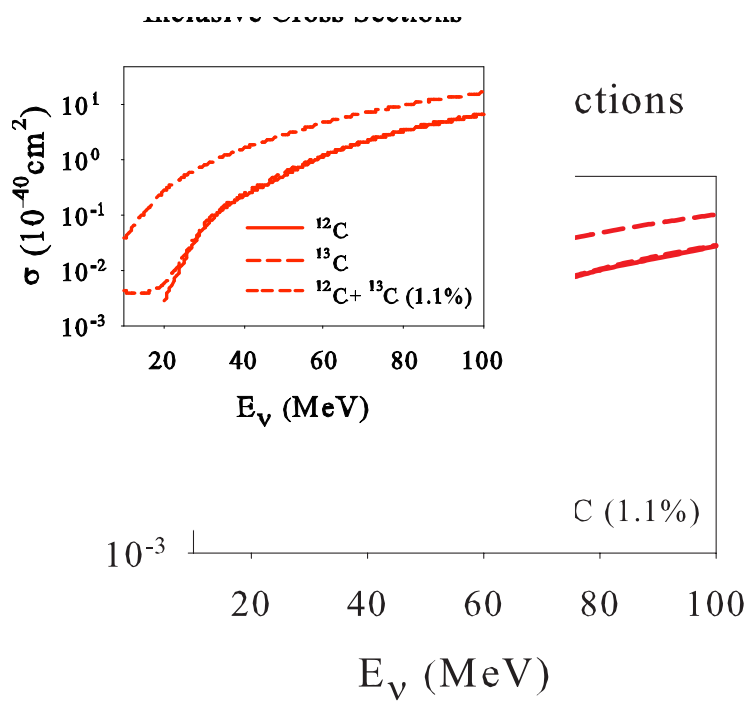
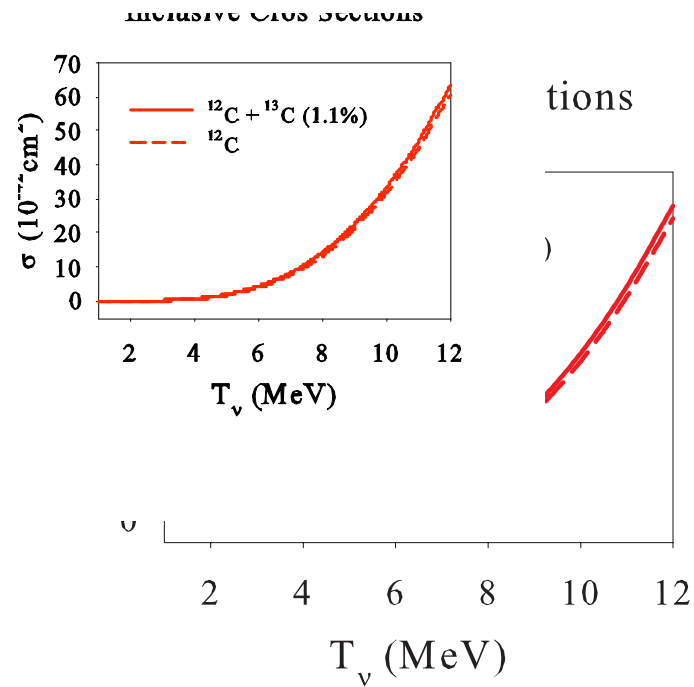
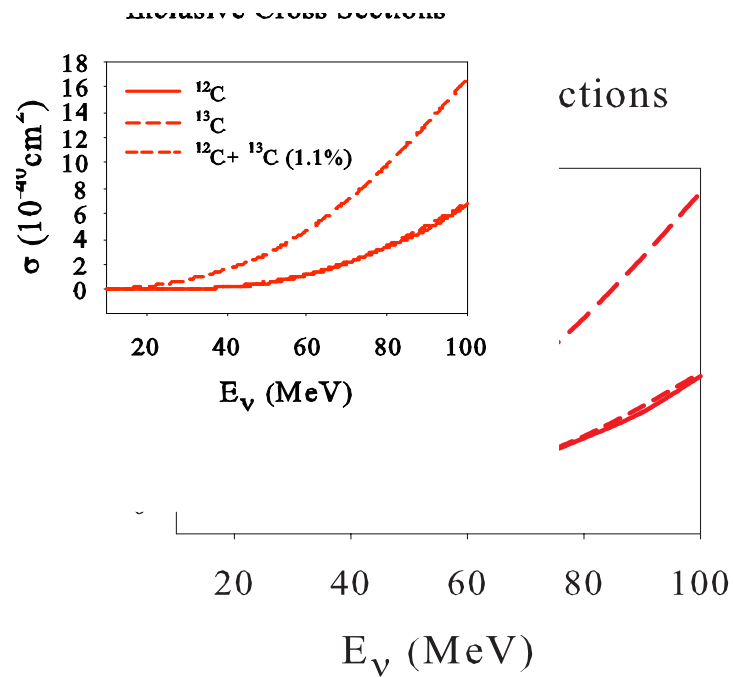
^{12}C 98.9%

^{13}C 1.1%

$^{12}\text{C} (\nu, e^-) ^{12}\text{N g.s.} \quad \Delta M = 16.83 \text{ MeV}$

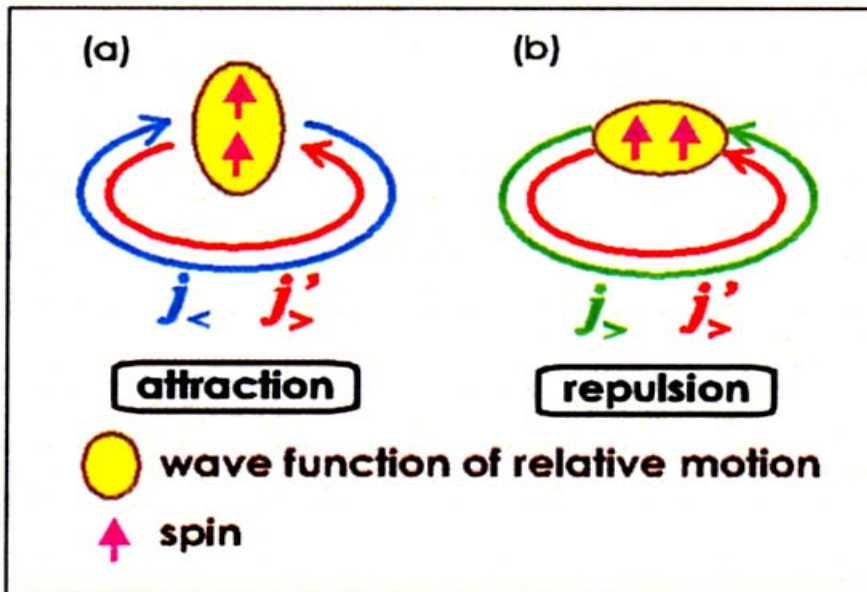
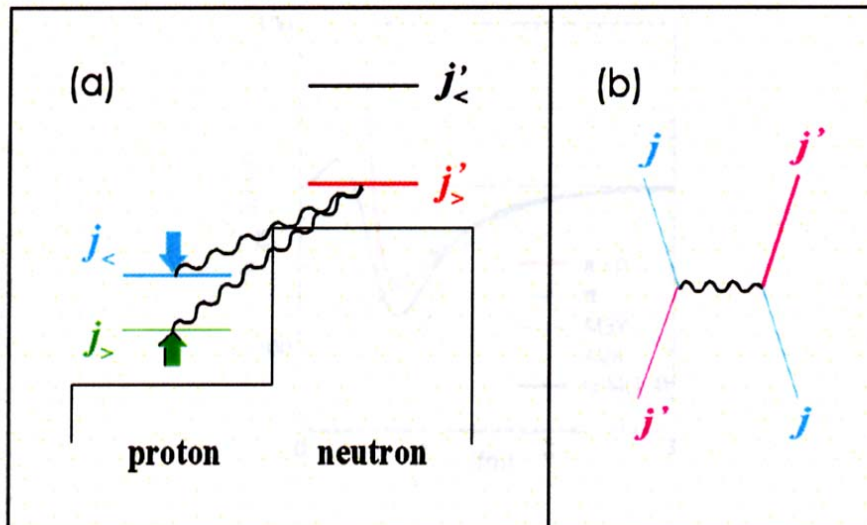
$^{12}\text{C} (\nu, e^-) ^{13}\text{N g.s.} \quad \Delta M = 1.71 \text{ MeV}$

$\sigma(^{13}\text{C}) > \sigma(^{12}\text{C})$

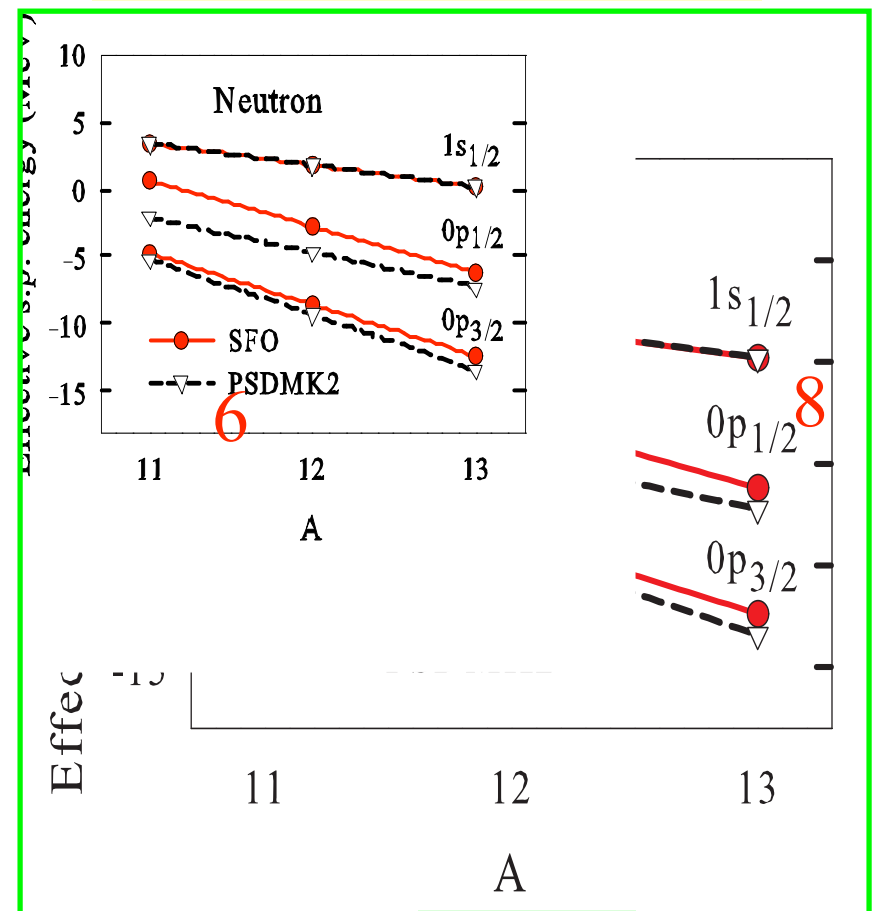


Tensor Force and Shell Evolution

Otsuka, Suzuki, Fujimoto, Grawe, Akaishi, PRL 69 (2005)



Shell evolution in N=8 isotone



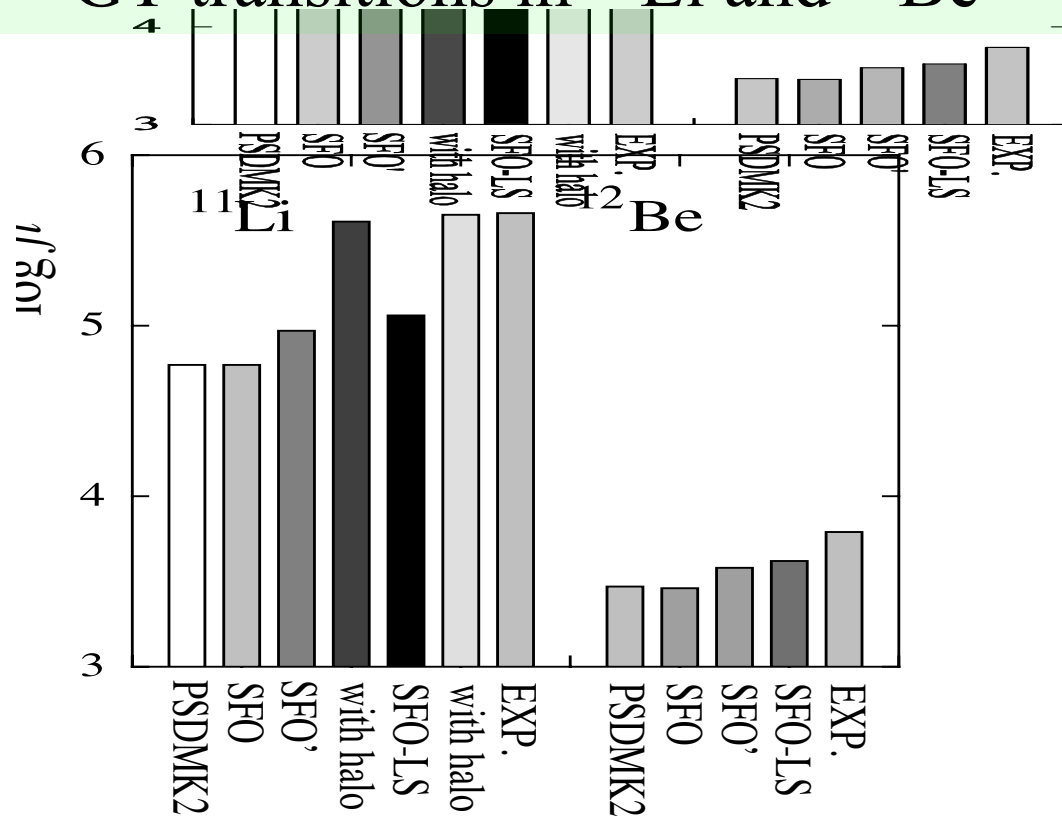
$\pi p_{3/2}$

Large p-sd shell mixing

^{11}Li	PSDMK2	SFO	SFO'	(SFO-tls)
$P(p^7)$	88%	60%	39%	(28%)
^{12}Be				
$P(p^8)$	85%	59%	44%	(39%)

SFO' : $\Delta s_{1/2} = -0.5$ MeV

GT transitions in ^{11}Li and ^{12}Be



^{11}Li :

Importance of halo
& sd-shell mixing

^{12}Be :

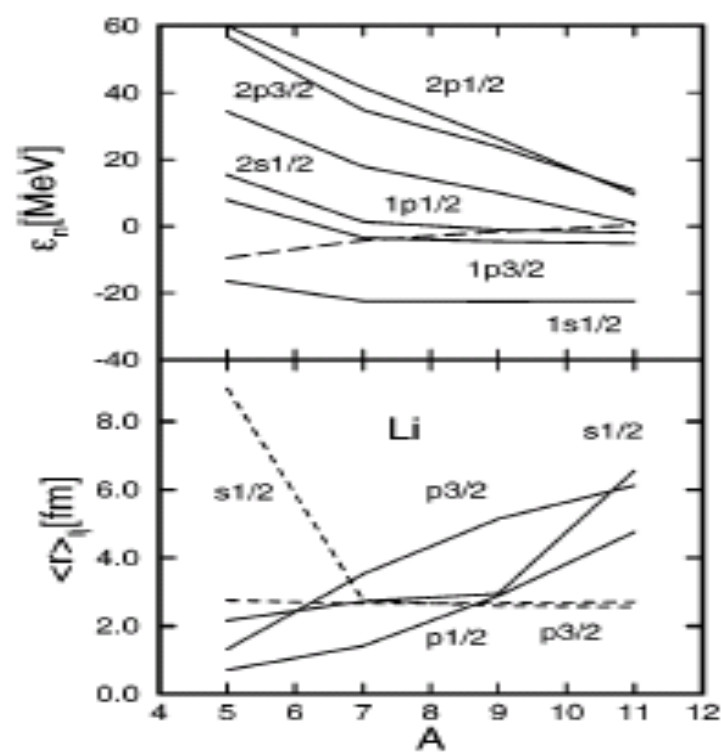
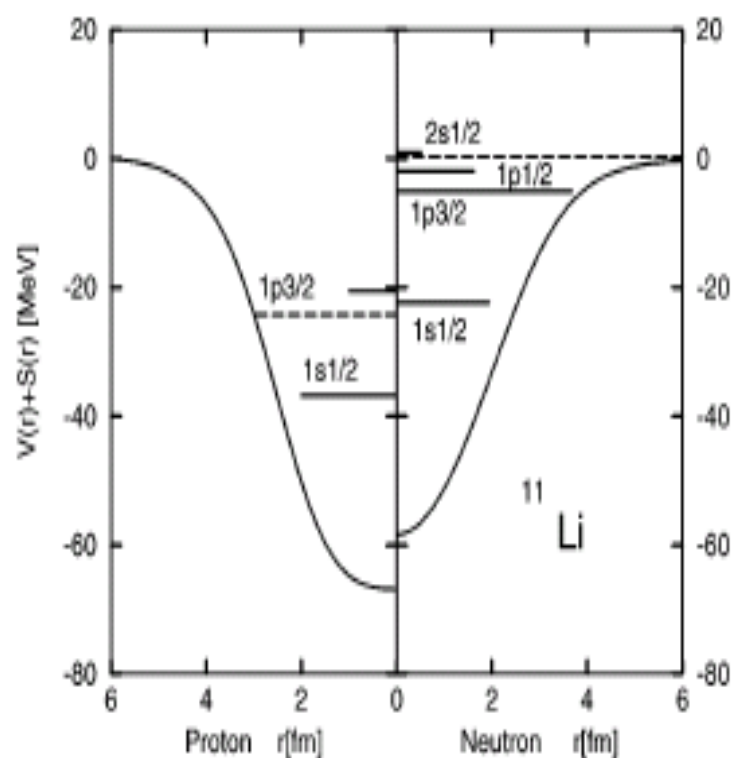
Importance of
sd-shell mixing

Relativistic Hartree-Bogoliubov Description of the Neutron Halo in ^{11}Li

J. Meng and P. Ring

Physik-Department der Technischen Universität München, D-85748 Garching, Germany

(Received 4 June 1996)



• ν -induced reactions on ^{16}O

• Modification of SFO

Full inclusion of tensor force

• p-sd: tensor $\rightarrow \pi + \rho$

LS $\rightarrow \sigma + \rho + \omega$

$$V = V_C + V_T + V_{LS}$$

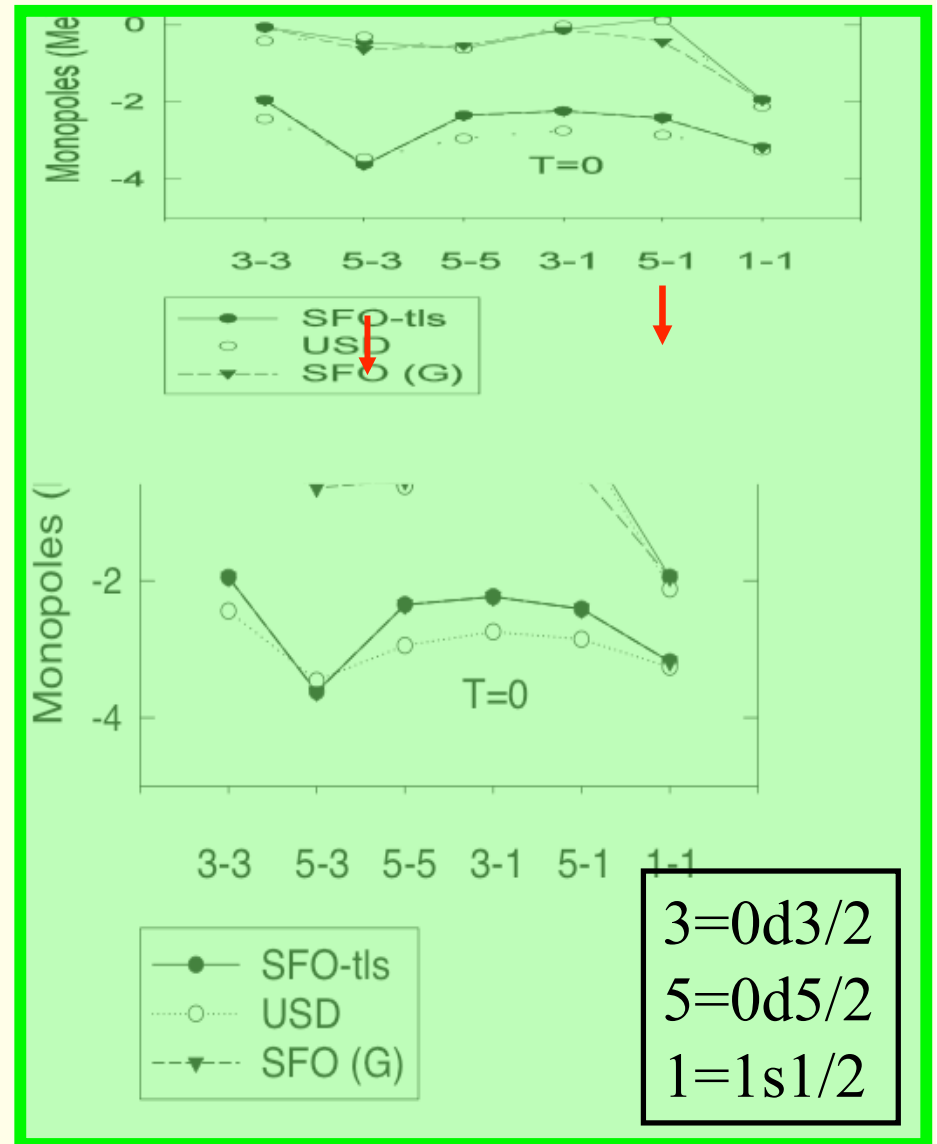
$$V_T = V_\pi + V_\rho$$

$$V_{LS} = V_{\sigma + \omega + \rho}$$

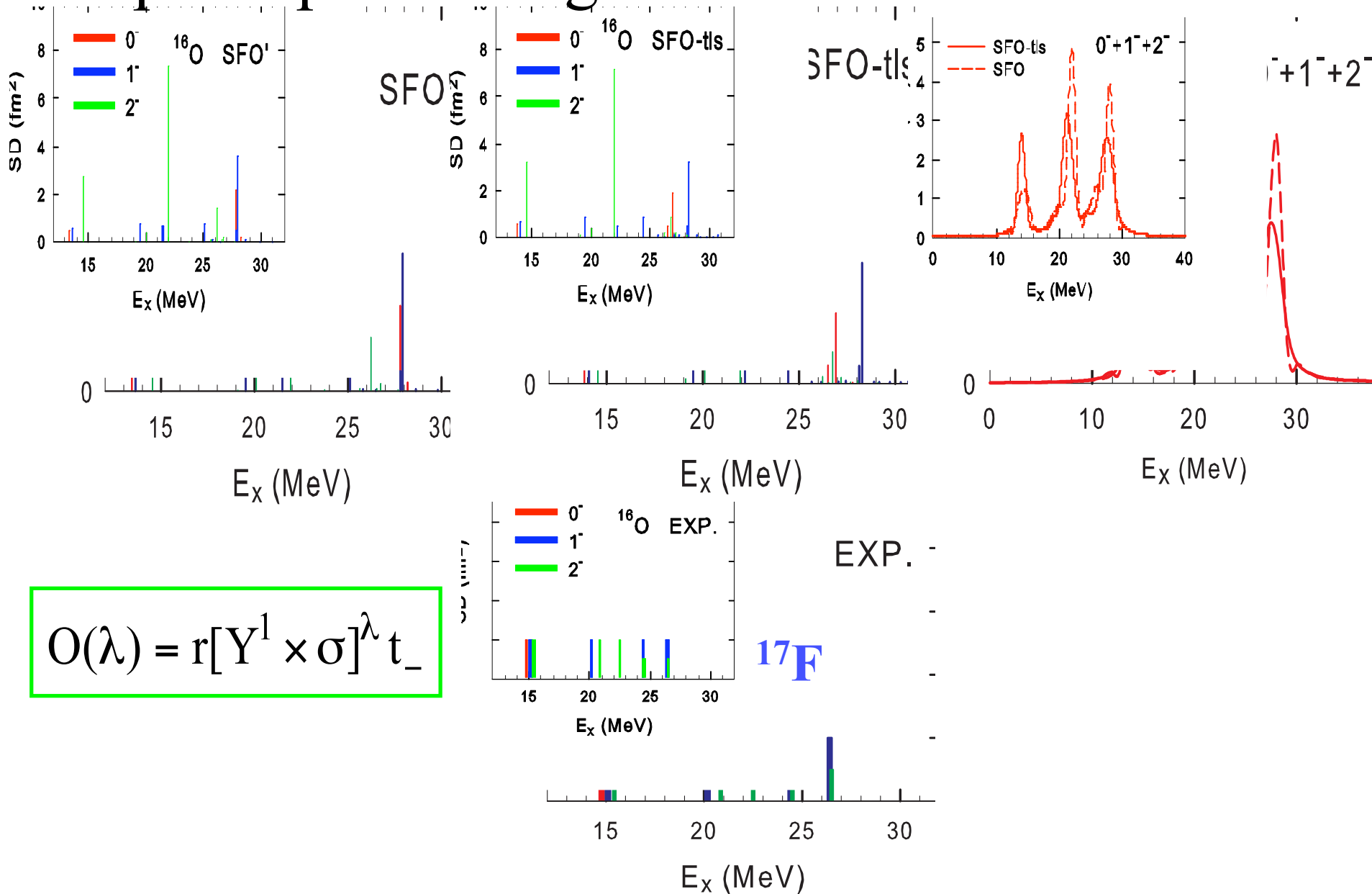
• sd: Kuo G-matrix

T=1 monopole terms
more repulsive

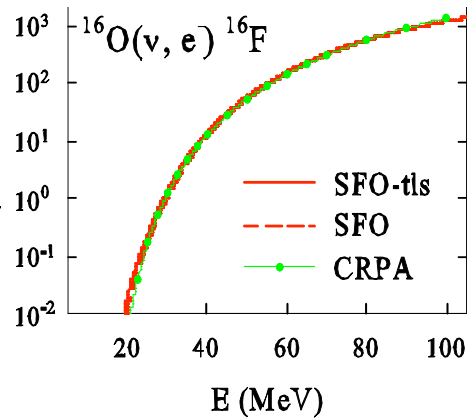
\rightarrow SFO-tls



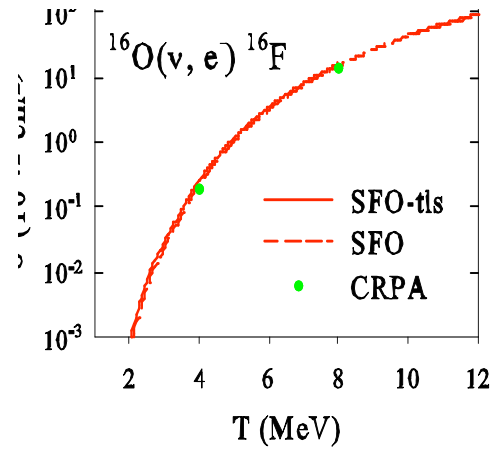
Spin-dipole strengths in ^{16}O



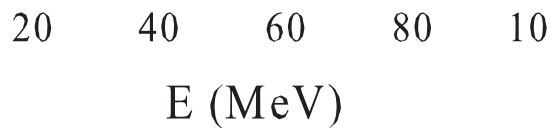
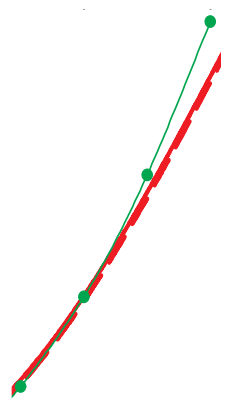
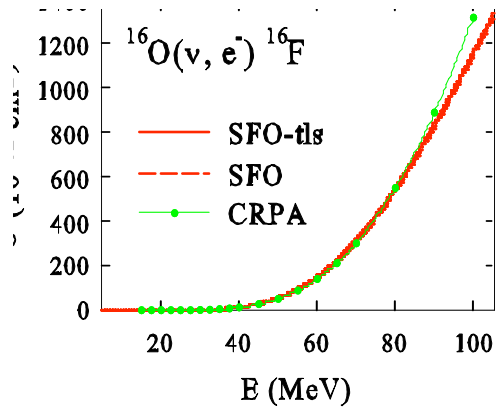
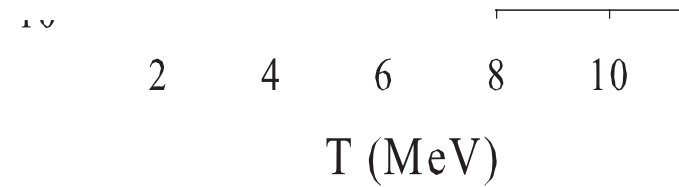
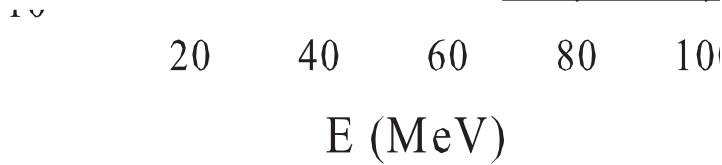
$$O(\lambda) = r[Y^1 \times \sigma]^\lambda t_-$$



SFO-tls
SFO
CRPA



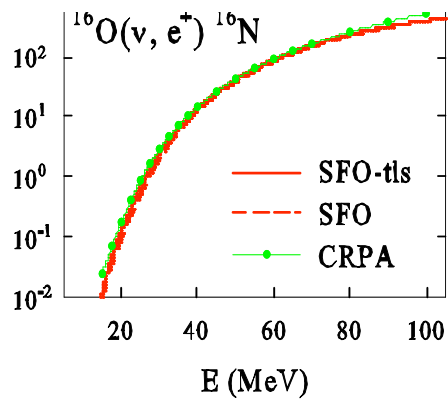
SFO-tls
SFO
CRPA



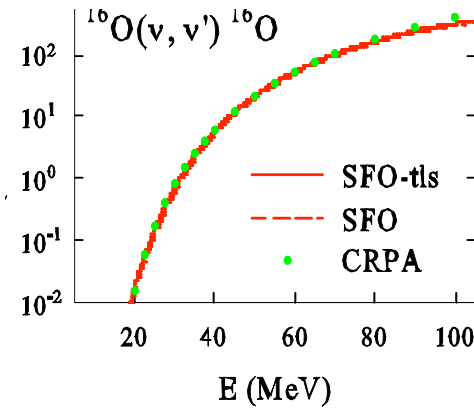
T= temperature of supernova ν

$$g_A^{\text{eff}}/g_A = 0.95$$

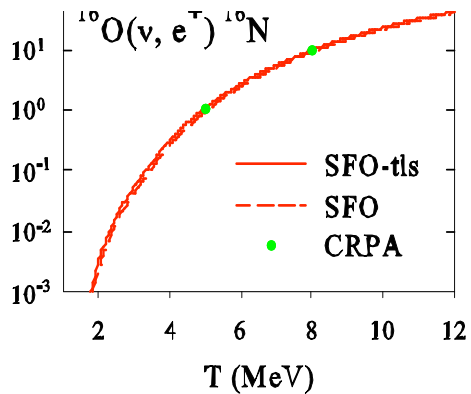
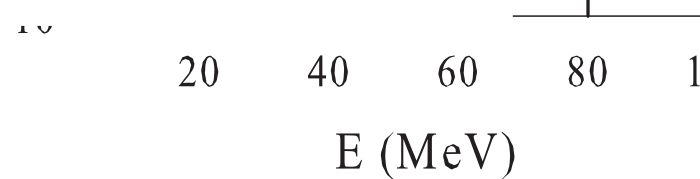
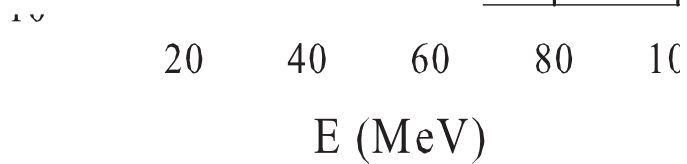
CRPA: Kolbe, Langanke & Vogel,
PR D66 (2002)



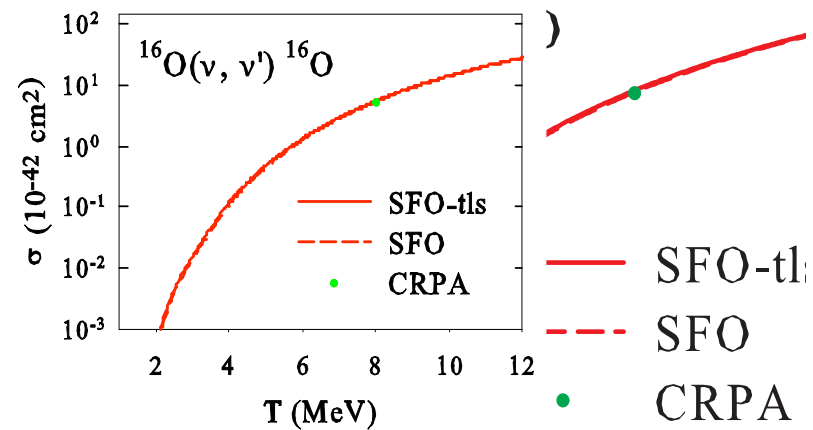
SFO-tls
SFO
CRPA



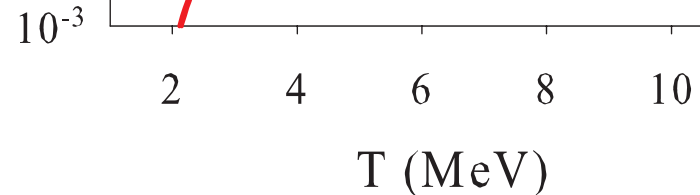
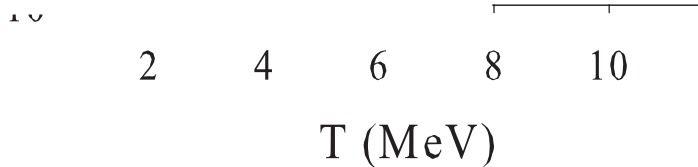
SFO-tls
SFO
CRPA



SFO-tls
SFO
CRPA



SFO-tls
SFO
CRPA



T= temperature of supernova v

CRPA: Kolbe, Langanke & Vogel, PR D66 (2002)

VMU= Monopole based Universal Interaction

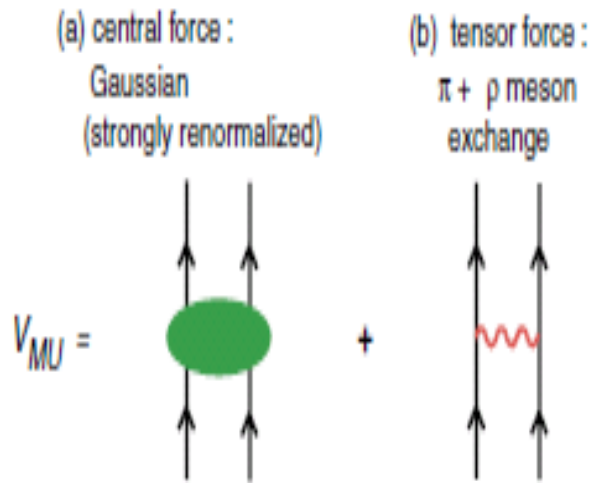
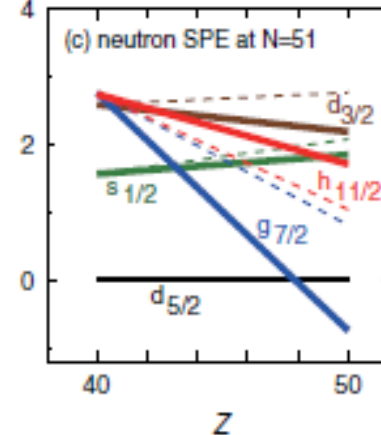
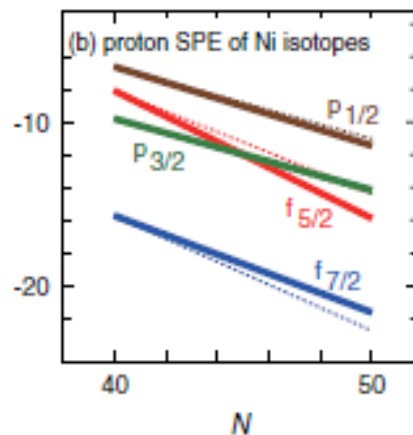
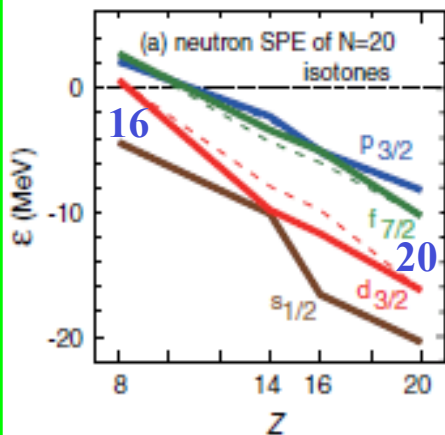
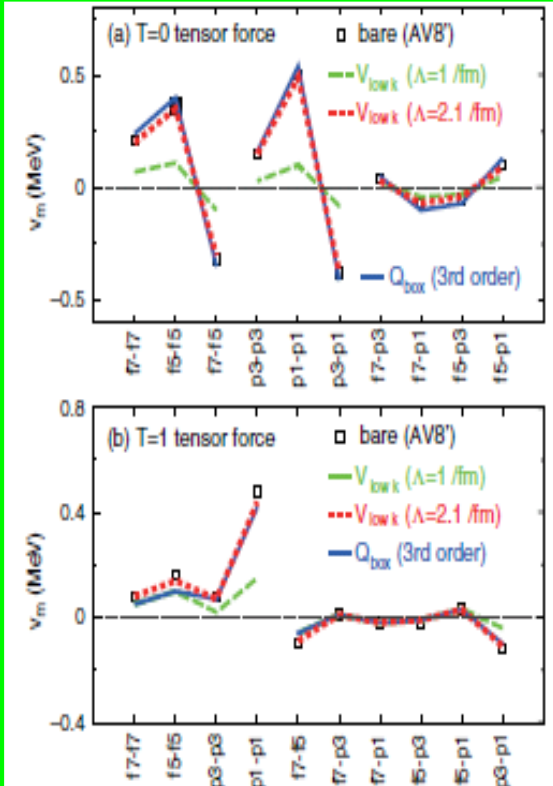
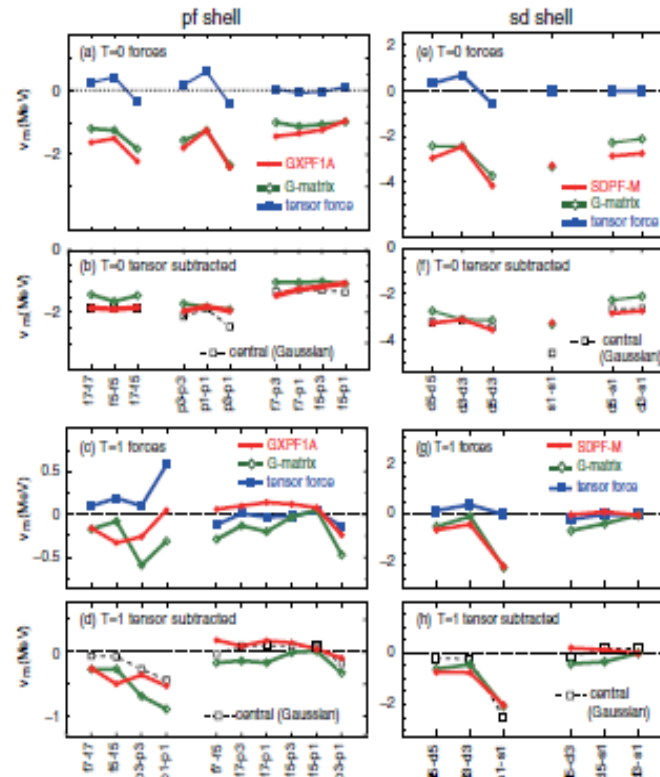


FIG. 2 (color online). Diagrams for the V_{MU} interaction.



Tensor:
bare \approx renormalized

Otsuka, Suzuki, Honma,
Utsuno, Tsunoda,
Tsukiyama, Hjorth-Jensen
PRL 104 (2010) 012501

$^{40}\text{Ar} (\nu, e^-) ^{40}\text{K}$

SDPF-VMU

sd: SDPF-M (Utsuno et al.)

fp: GXPF1 (Honma et al.)

sd-pf: VMU

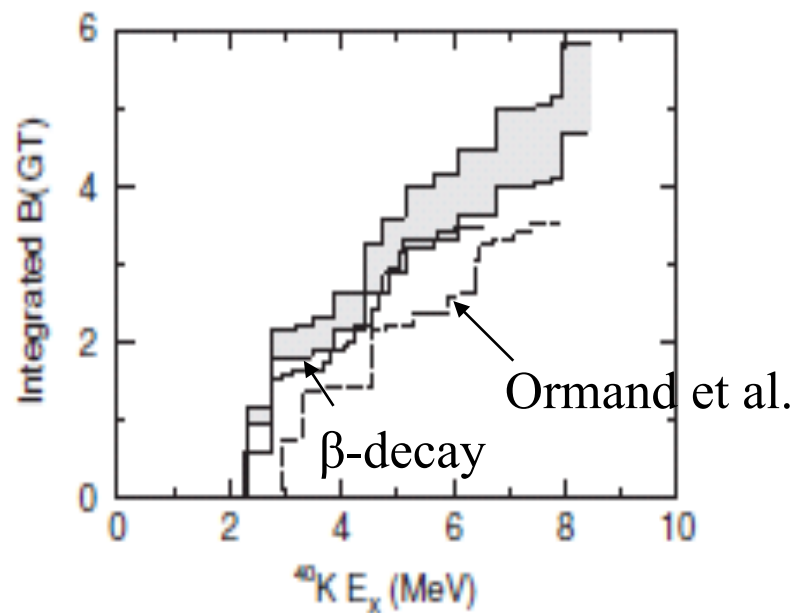
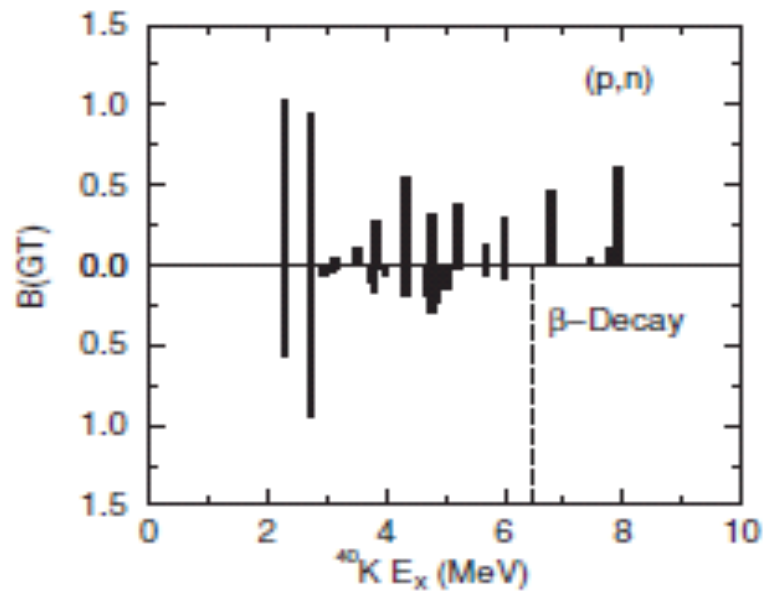
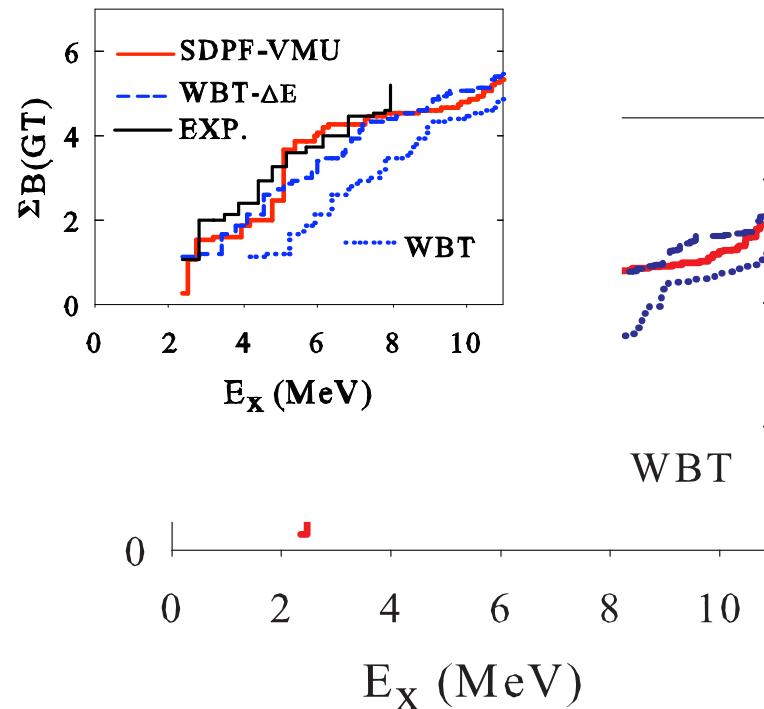
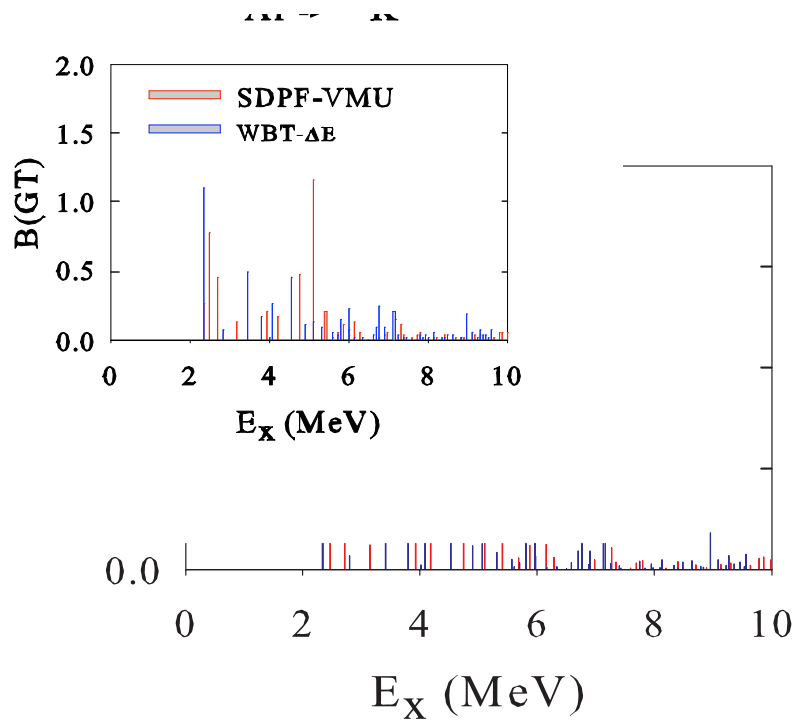
$(\text{sd})^{-2} (\text{fp})^2 : 2\text{hw}$

B(GT)

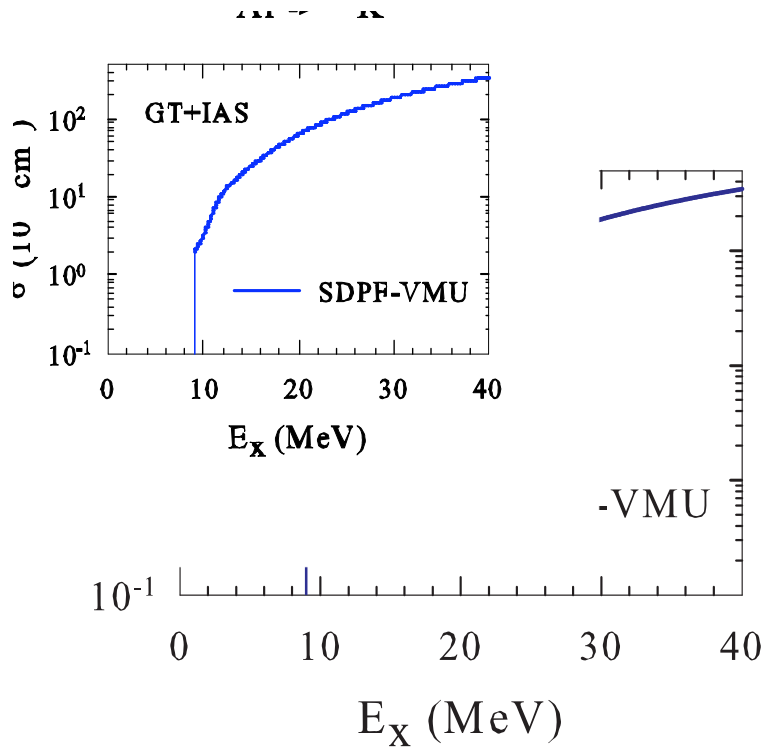
ν - ^{40}Ar cross sections

Solar ν cross sections folded over ^8B ν spectrum

$B(\text{GT}) = \sum |\langle f || f_q \sigma t_- || i \rangle|^2 \quad f_q = 0.775$ (Ormand et al.)



(p,n) Bhattacharya et al., PR C80 (2009)



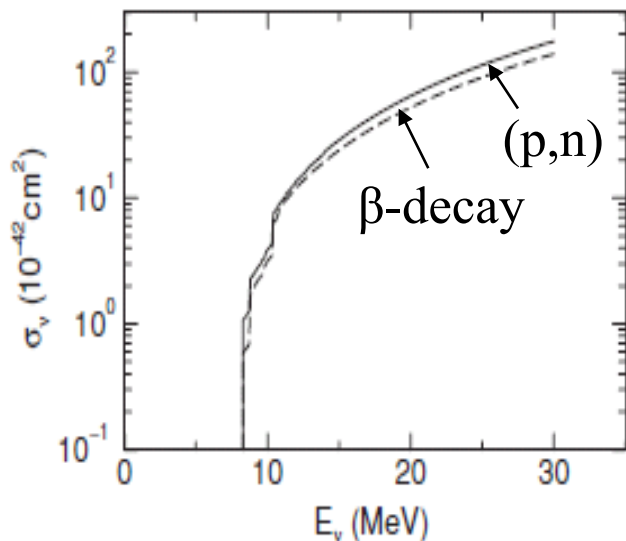
GT+IAS

$E_e > 5$ MeV : ICARUS

Solar ν cross sections
folded over ^8B ν spectrum

	GT	IAS	GT+IAS
SDPF-VMU:	10.36	$1.94 * 12.3 \times 10^{-43} \text{cm}^2$	
WBT- ΔE :	10.18	1.94	12.1
(WBT:	2.65	1.94	4.6)

Ormand et al,: 7.7^{++} 3.8^+ 11.5
(PL B345, 343 (1995))



IAS: * $C_0 + L_0 \approx [(q^2 - \omega^2)/q^2]^2 \times C_0$
+ C_0 only

GT: $E_1^5 + M1 + C_1^5 + L_1^5$
 $^{++} E_1^5$ only

(p,n) Bhattacharya et al., PR C80, 055501 (2009)

- **New shell-model Hamiltonians in fp-shell:**

- GXPF1:** Honma et al., PR C65 (2002); C69 (2004)

- KB3:** Caurier et al., Rev. Mod. Phys. 77, 427 (2005)

- KB3G $A = 47-52$ KB + monopole corrections

- GXPF1 $A = 47-66$

- Systematic reproduction of $E(2^+)$ and $B(E2)$ in fp-shell nuclei

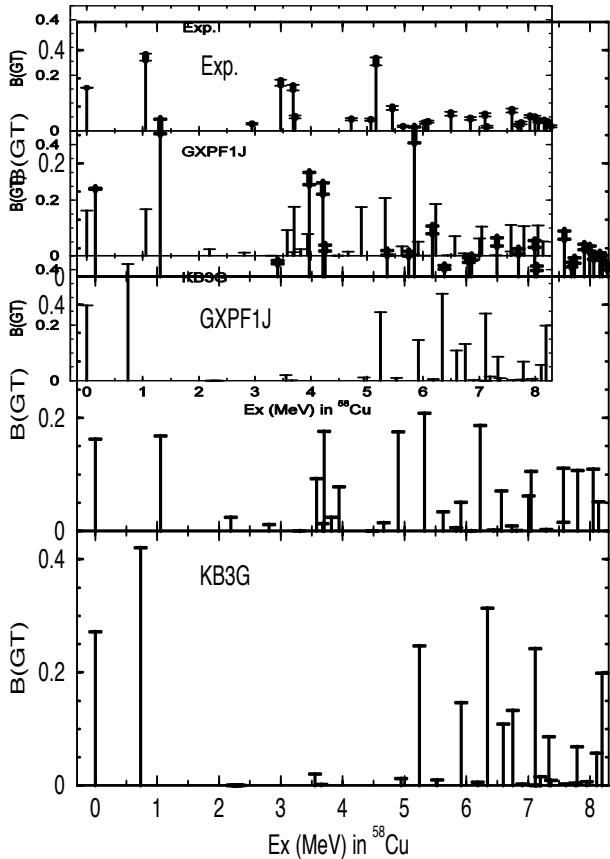
- **Spin properties of fp-shell nuclei are well described**

- **GT Strengths in Ni and Fe Isotopes and M1 strengths in fp-shell nuclei**

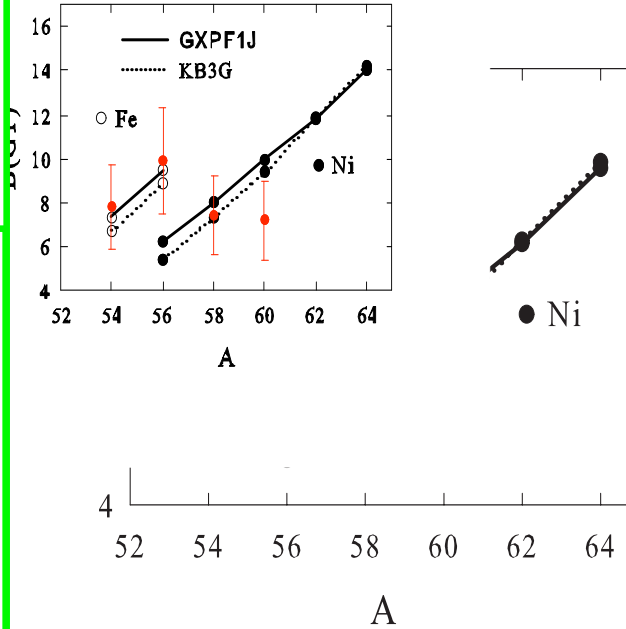
fp-shell

B(GT₋) for ⁵⁸Ni

Exp: Fujita et al.



$$g_A^{\text{eff}}/g_A^{\text{free}}=0.74$$



B(GT₊)

	GXPf1J	EXP.
⁵⁴ Fe	4.0	3.3±0.5
⁵⁶ Fe	2.9	2.8±0.3
⁵⁸ Ni	4.7	3.8±0.4
⁶⁰ Ni	3.4	3.1±0.1

EXP: GT₋; Rapaport et al., NP A410, 371 (1983)

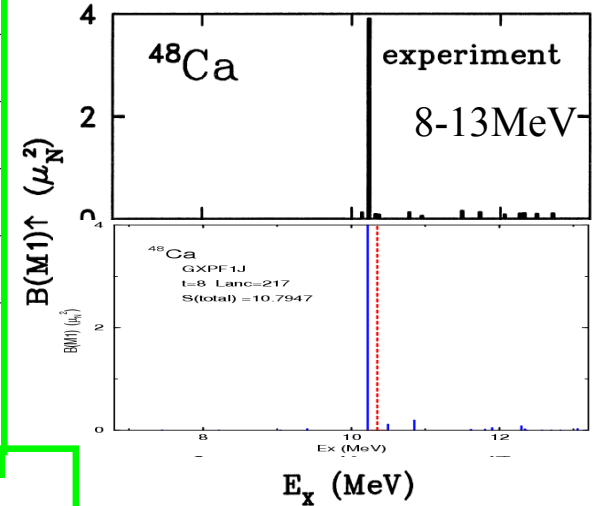
0 < E_x < 13-15 MeV

GT₊; Caurier et al., NP A653, 439 (1999)

0 < E_x < 8 MeV

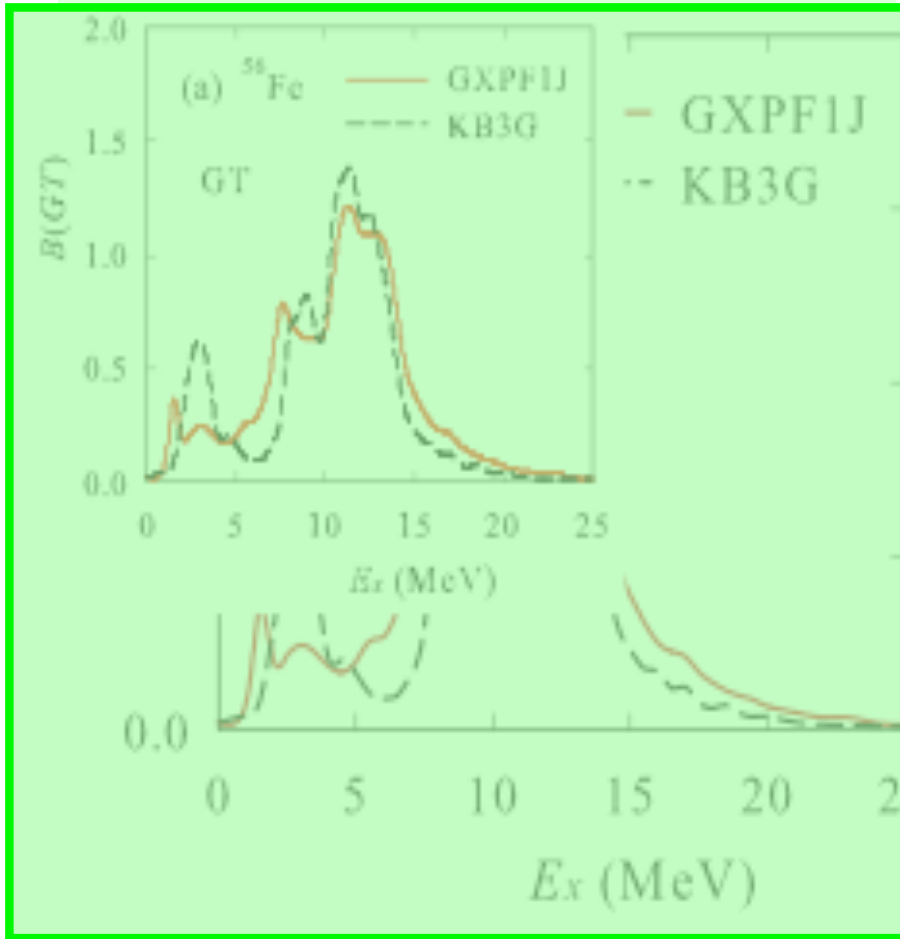
M1 strength (GXPf1J)

$$g_S^{\text{eff}}/g_S=0.75\pm0.2$$



Honma

$^{56}\text{Fe}(\nu_e, e^-)^{56}\text{Co}$

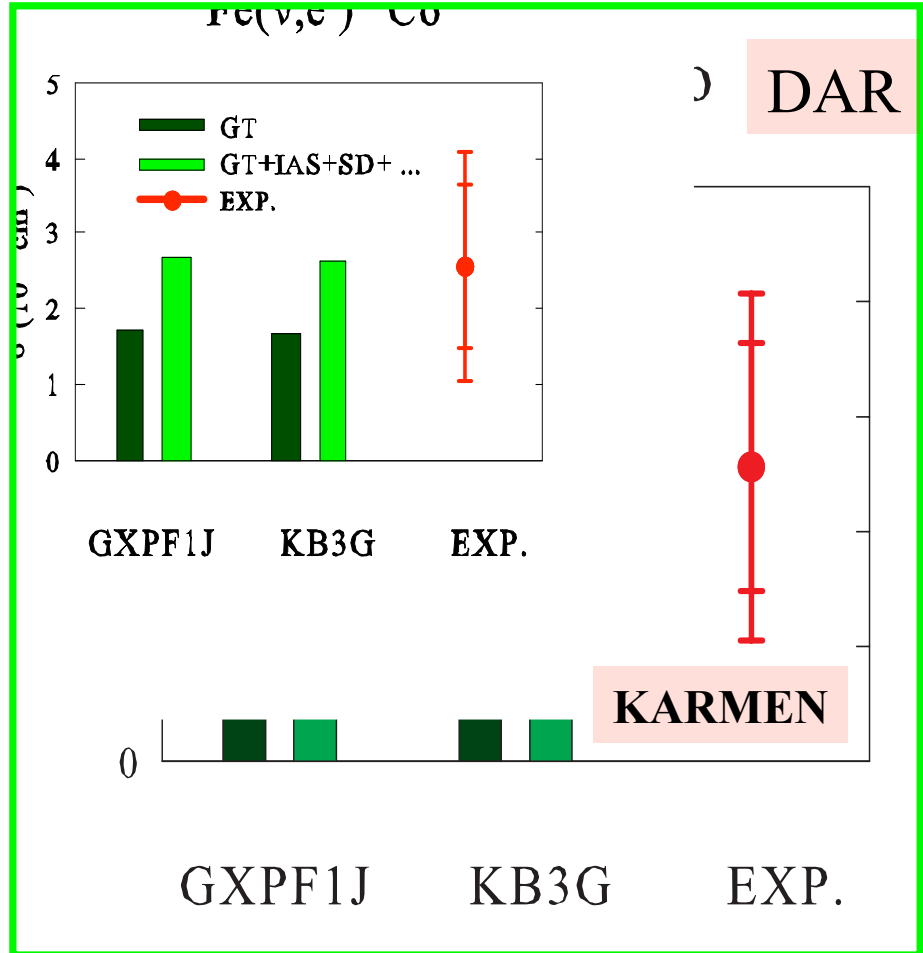


$$B(\text{GT})=9.5$$

$$B(\text{GT})_{\text{exp}}=9.9\pm 2.4$$

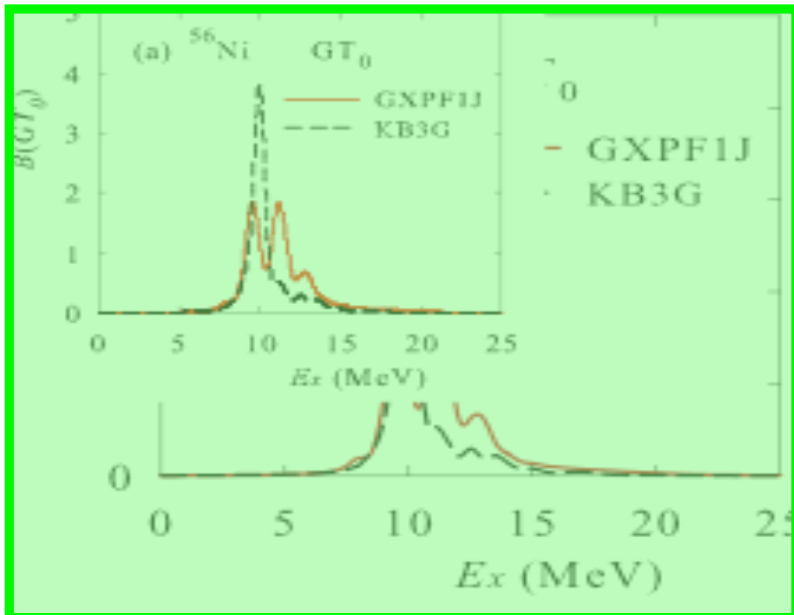
$$B(\text{GT})_{\text{KB3G}}=9.0$$

GXPFIJ Honma et al.
cf. KB3 Caurier et al.

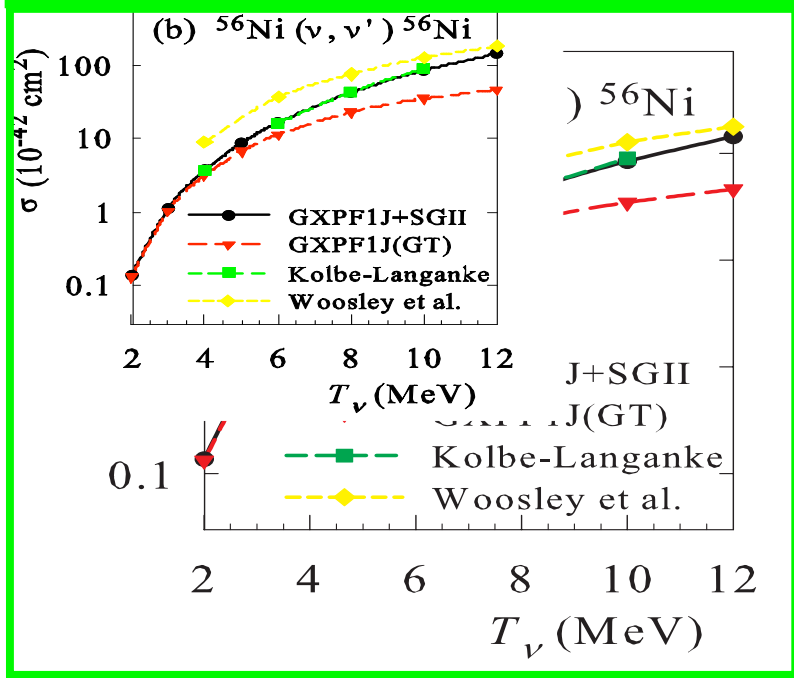


SD + ... : RPA (SGII)

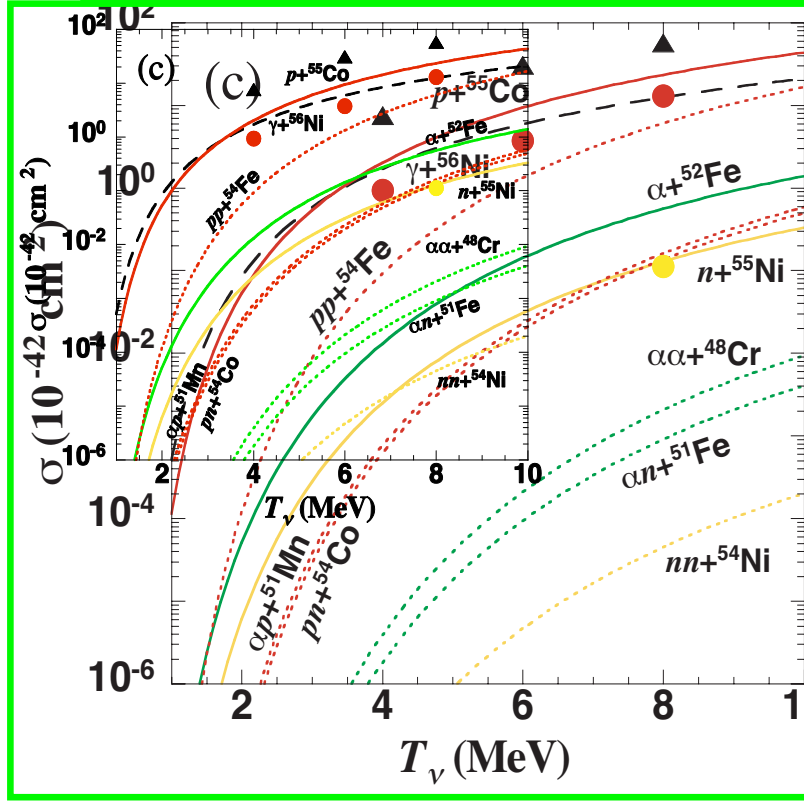
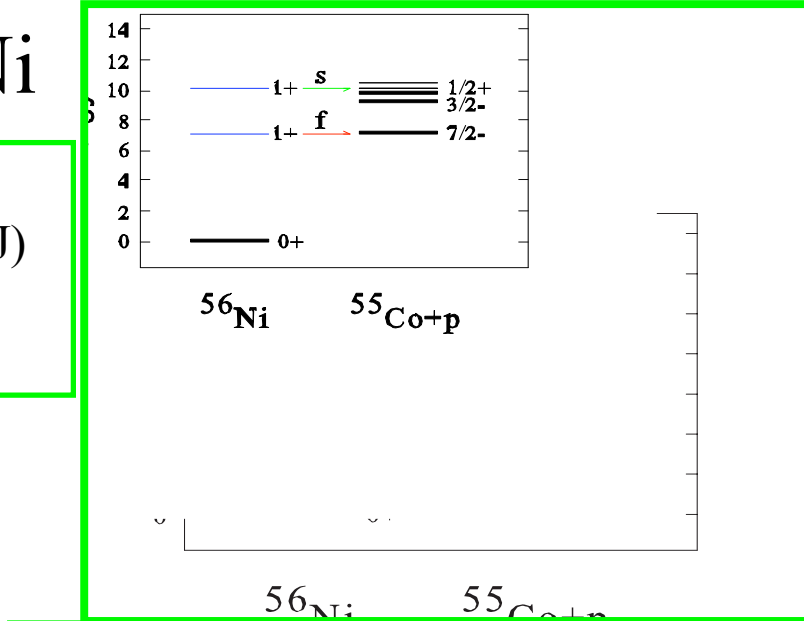
• Neutral current reaction on ^{56}Ni



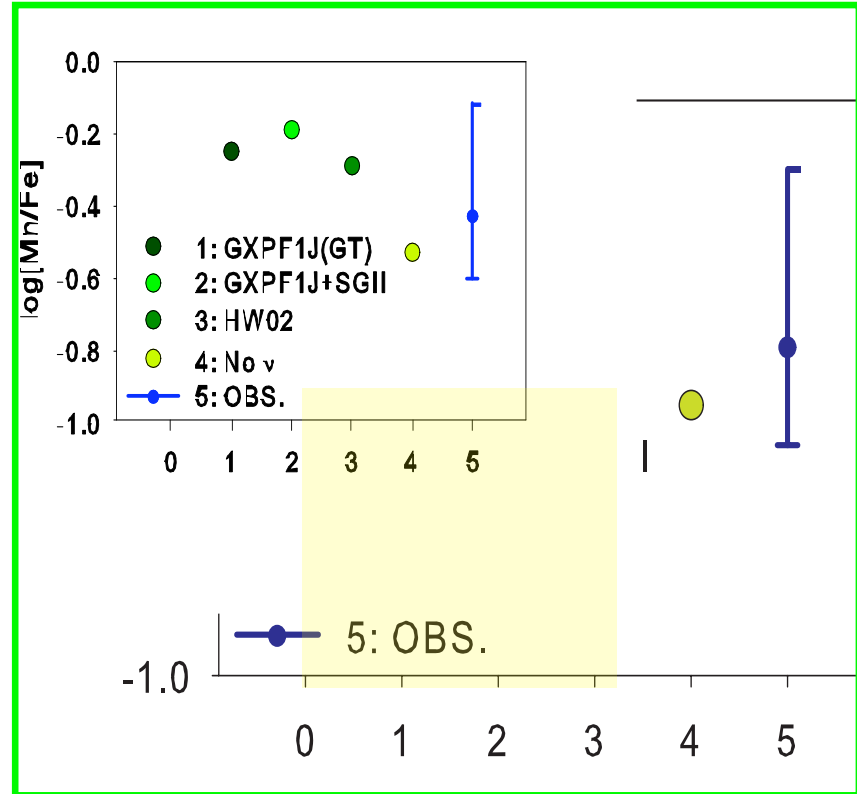
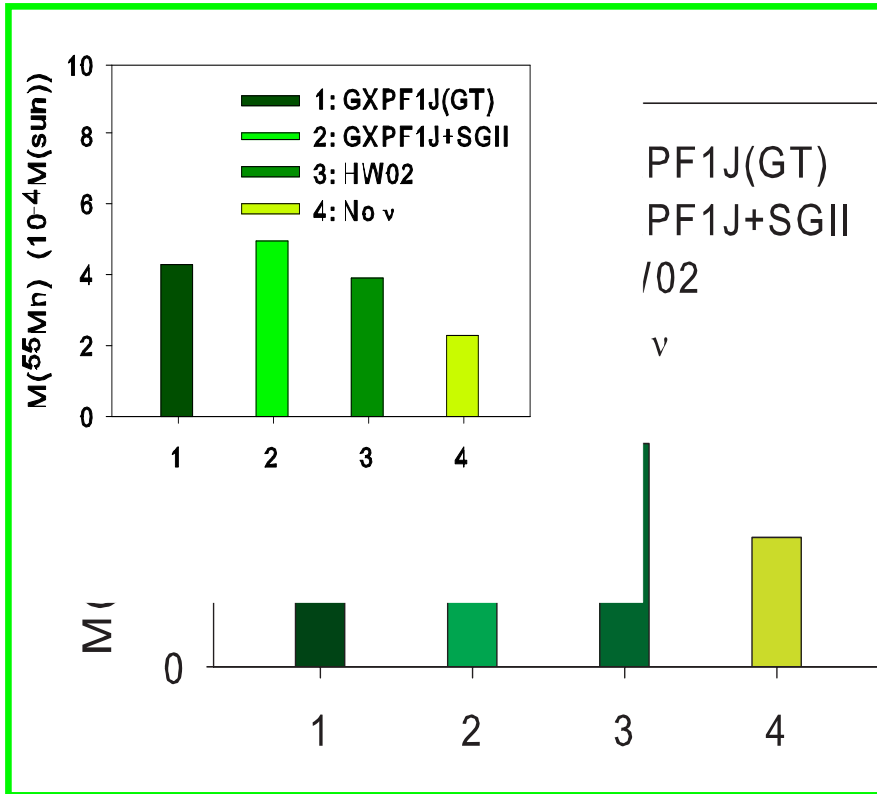
$B(\text{GT})=6.2$
 (GXPFIJ)
 $B(\text{GT})=5.4$
 (KB3G)



cf:
 HW02
 ▲ gamma
 ● p
 ● n



Synthesis of Mn in Population III Star

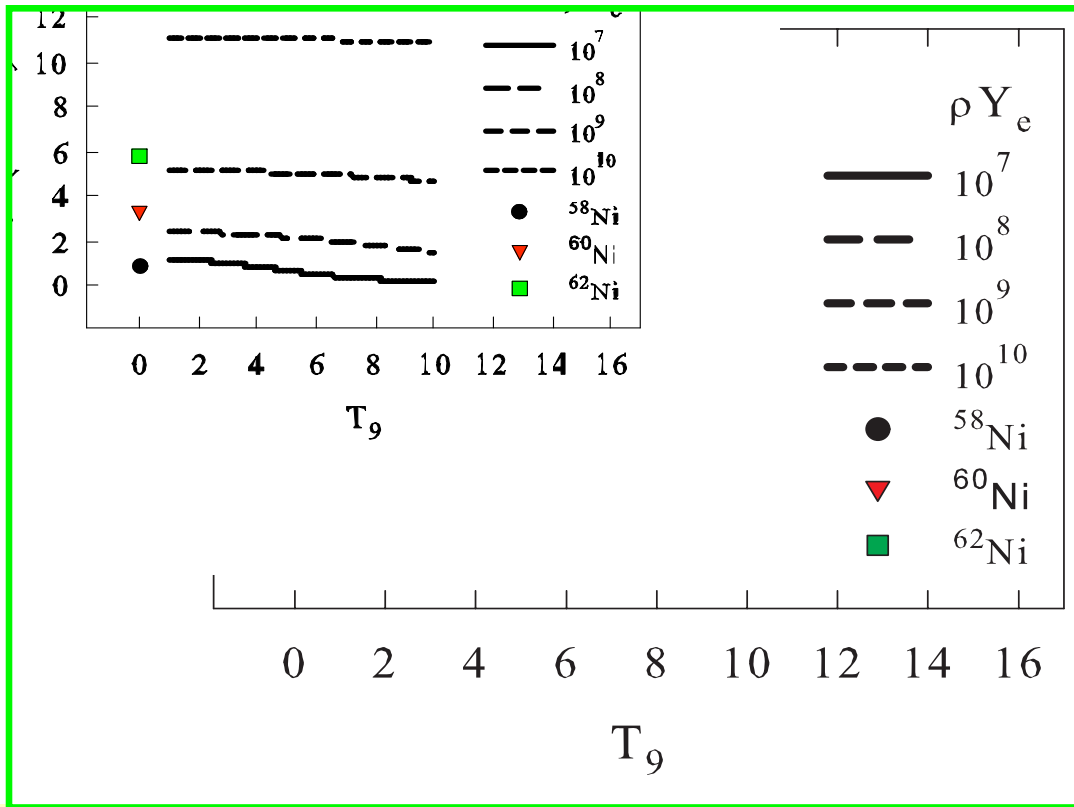


Yoshida, Umeda, Nomoto

Suzuki et al., PR C79 (2009)

OBS: Cayrel et al., Astron. Astrophys. 416 (2004)

● Electron-capture rate in steller environment



$$T = 0: \mu + M({}_Z\text{A}) \geq M({}_{Z-1}\text{A})$$

$$\mu \geq M({}_{Z-1}\text{A}) - M({}_Z\text{A})$$

$$\rho Y_e = 10^7 - 10^{10} \text{ mol/cm}^3$$

$$T = T_9 \times 10^9 \text{ K}$$

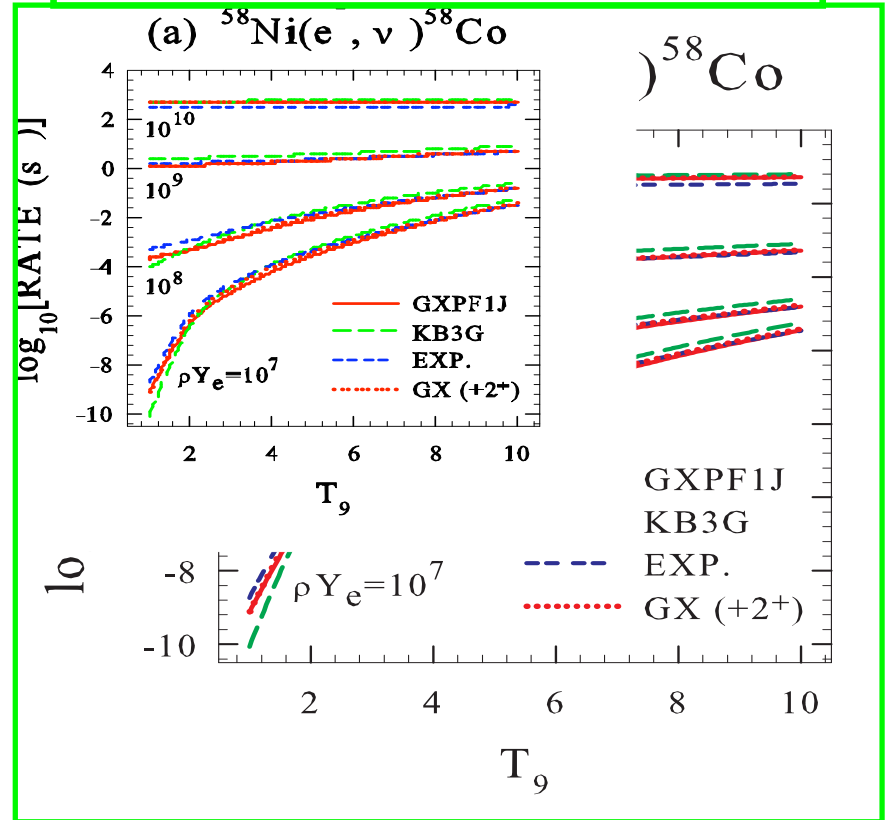
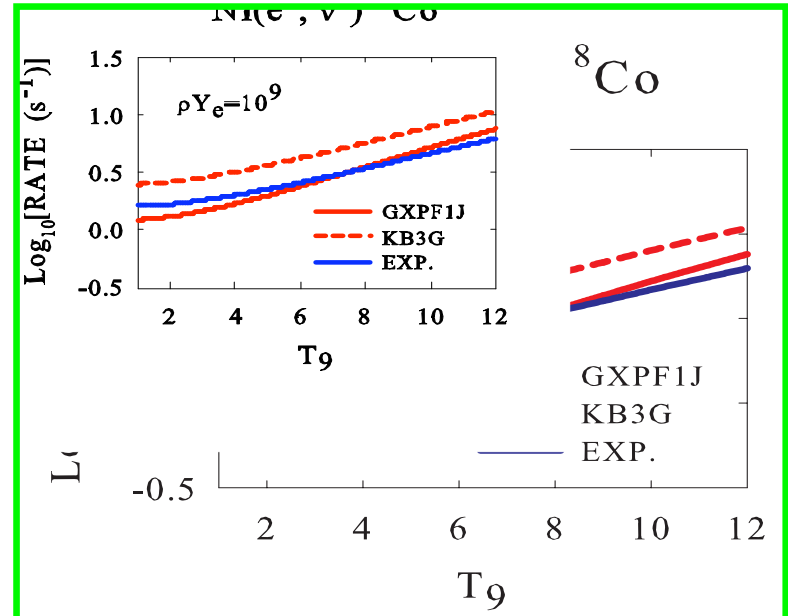
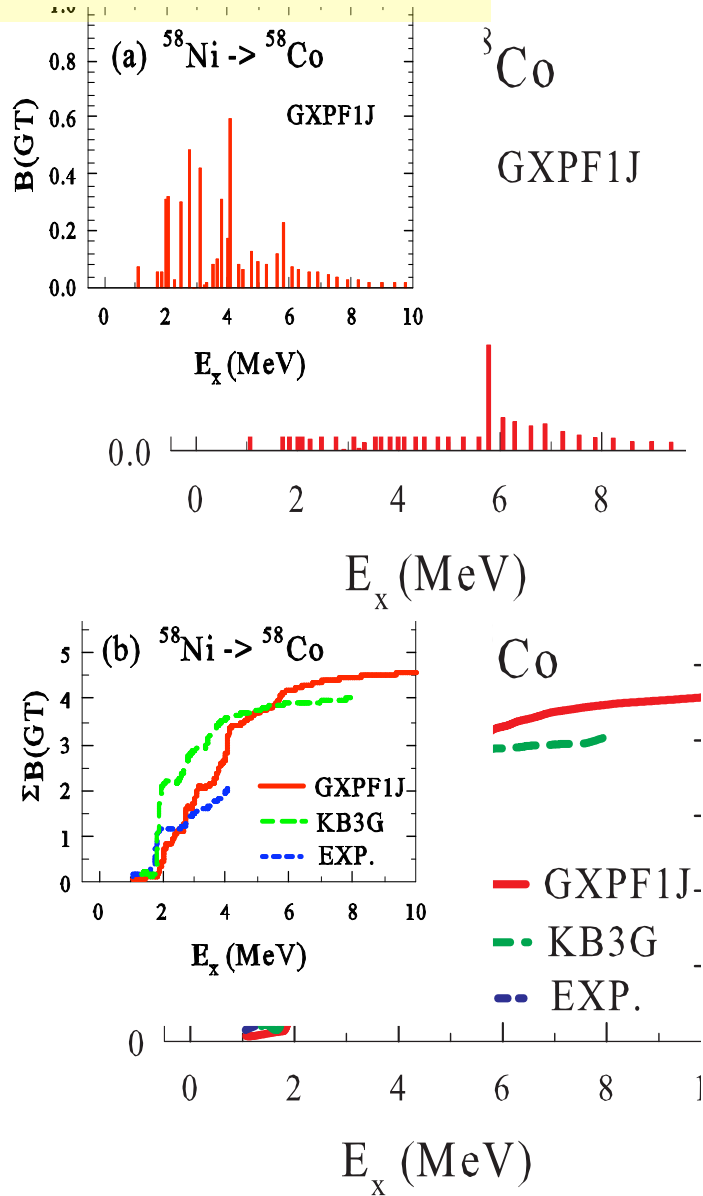
$$\lambda = \frac{\ln 2}{6146(s)} \sum_j B_j (GT) \int_{\omega_e}^{\infty} \omega p(Q_j + \omega)^2 F(Z, \omega) S_e(\omega) d\omega$$

$$Q_j = (M_p c^2 - M_d c^2 - E_j) / m_e c^2$$

$$T = T_9 \times 10^9 \text{ K}, \quad S_e(E_e) = \frac{1}{\exp[(E_e - \mu_e) / kT] + 1}$$

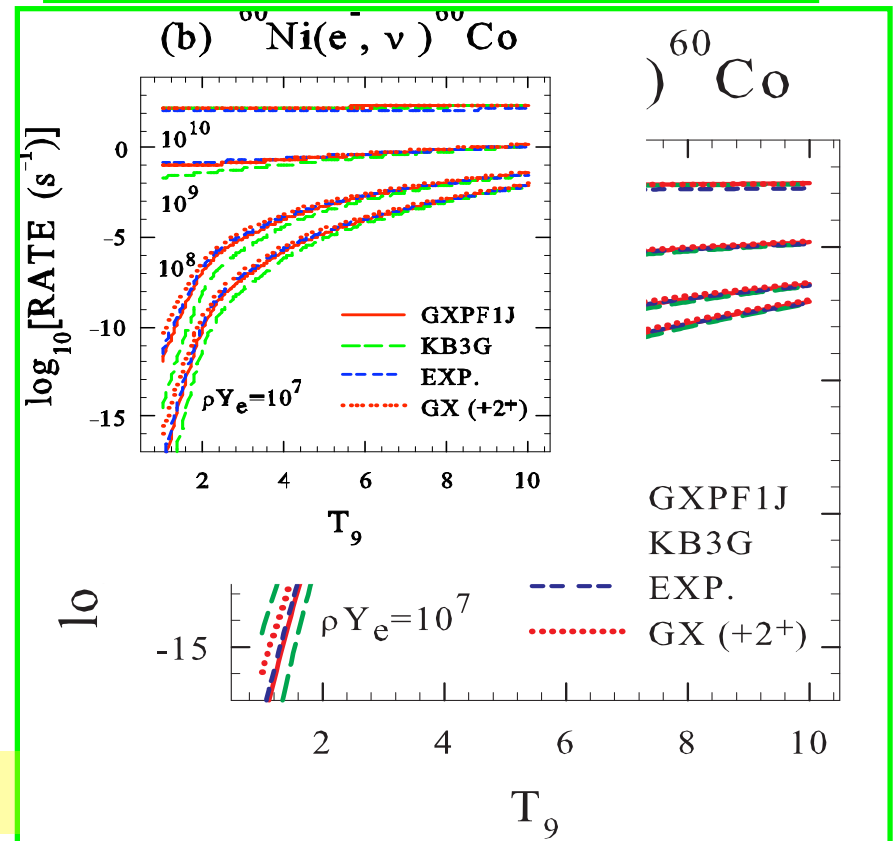
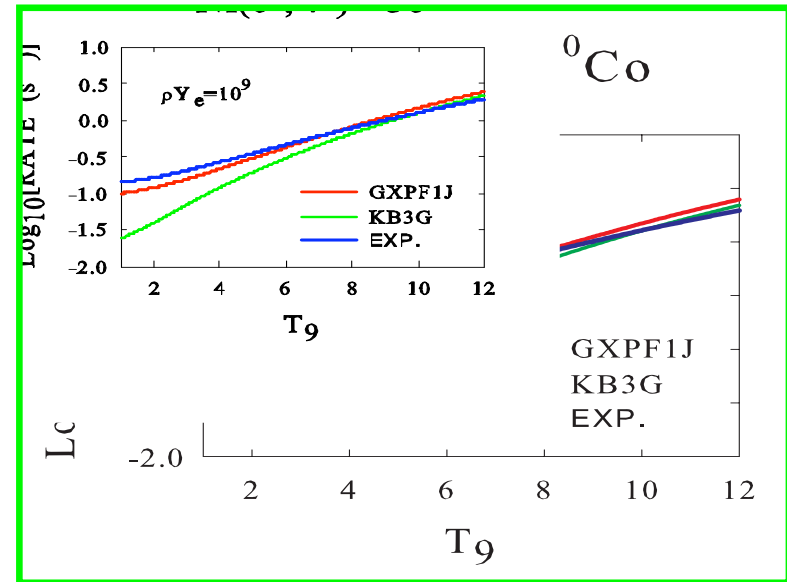
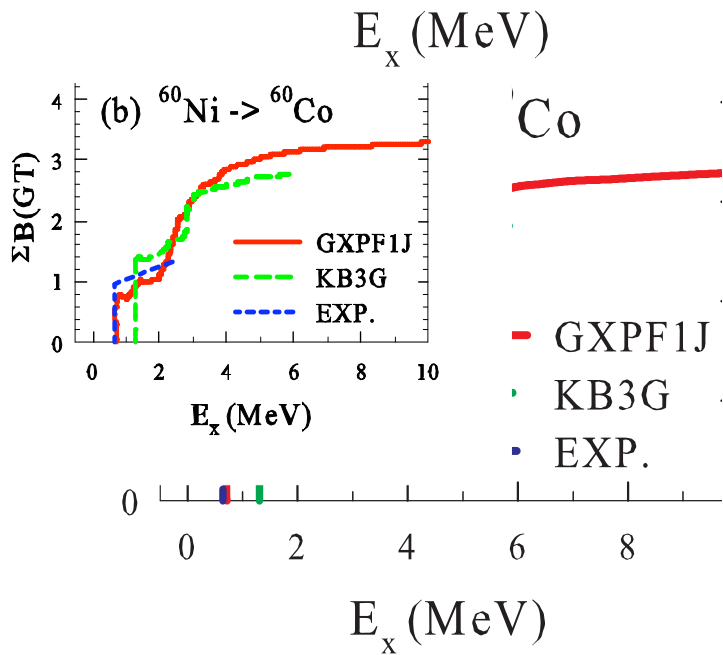
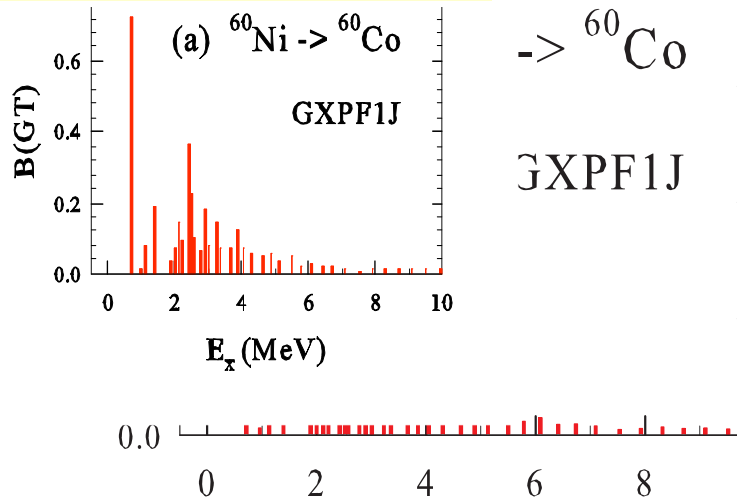
$$\rho Y_e = \frac{1}{\pi^2 N_A} \left(\frac{m_e c}{\hbar} \right)^3 \int_0^{\infty} (S_e - S_p) p^2 dp \quad \mu_p = -\mu_e$$

$^{58}\text{Ni} \rightarrow ^{58}\text{Co}$



Exp: Hagemann et al., PL B579 (2004)

$^{60}\text{Ni} \rightarrow ^{60}\text{Co}$



Exp: Anantaraman et al., PR C78 (2008)

Summary

- **New shell model Hamiltonians with proper tensor interaction**
- **→ new ν -nucleus reaction cross sections in ^{12}C and ^{16}O**
 - Enhancement of production rate of ^7Li , ^{11}B**
 - Cross sections in ^{16}O : shell model \sim CRPA**
 - Contamination effect of ^{13}C \sim a few %**
 - sd-pf-VMU: $^{40}\text{Ar}(\nu, e^-)^{40}\text{K}$ for solar ν**
- **ν - ^{56}Fe cross sections (DAR), electron capture rates in ^{58}Ni and ^{60}Ni are well described by a new shell model Hamiltonian, GXPF1J.**
 - ν - ^{56}Ni → enhancement of production of Mn**

Collaborators

**M. Honma^a, T. Yoshida^b, S. Chiba^f,
T. Kajino^{b,d}, T. Otsuka^e, H. Mao^g**

^aUniversity of Aizu

^bDepartment of Astronomy, University of Tokyo

^dNational Astronomical Observatory of Japan

^eDepartment of Physics and CNS, University of Tokyo

^fJAEA

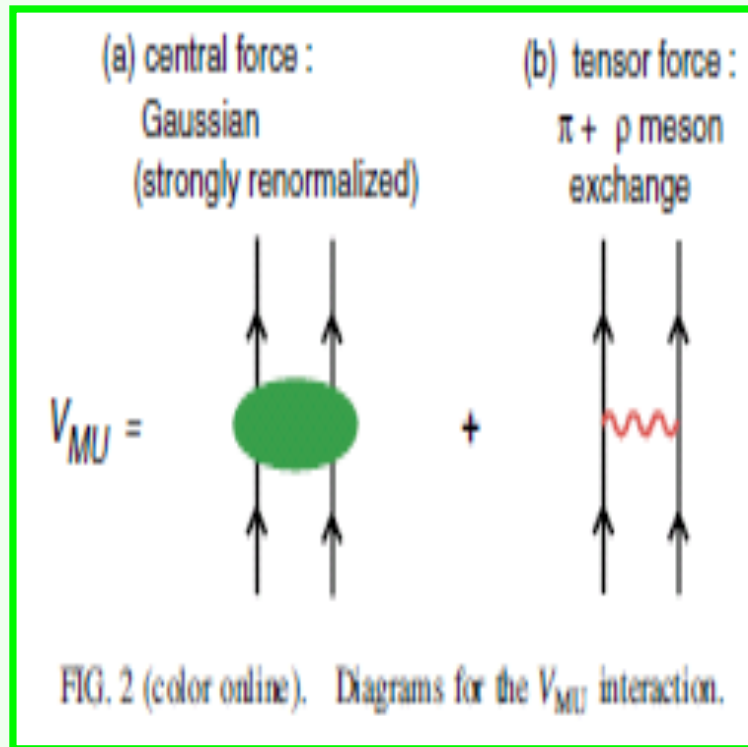
^gENSPPS, Strasbourg

B. Balantekin (Wisconsin) for the ^{13}C problem

70 **77** **80** **88** **90** **99** **100**

110 **111** **120** **...**

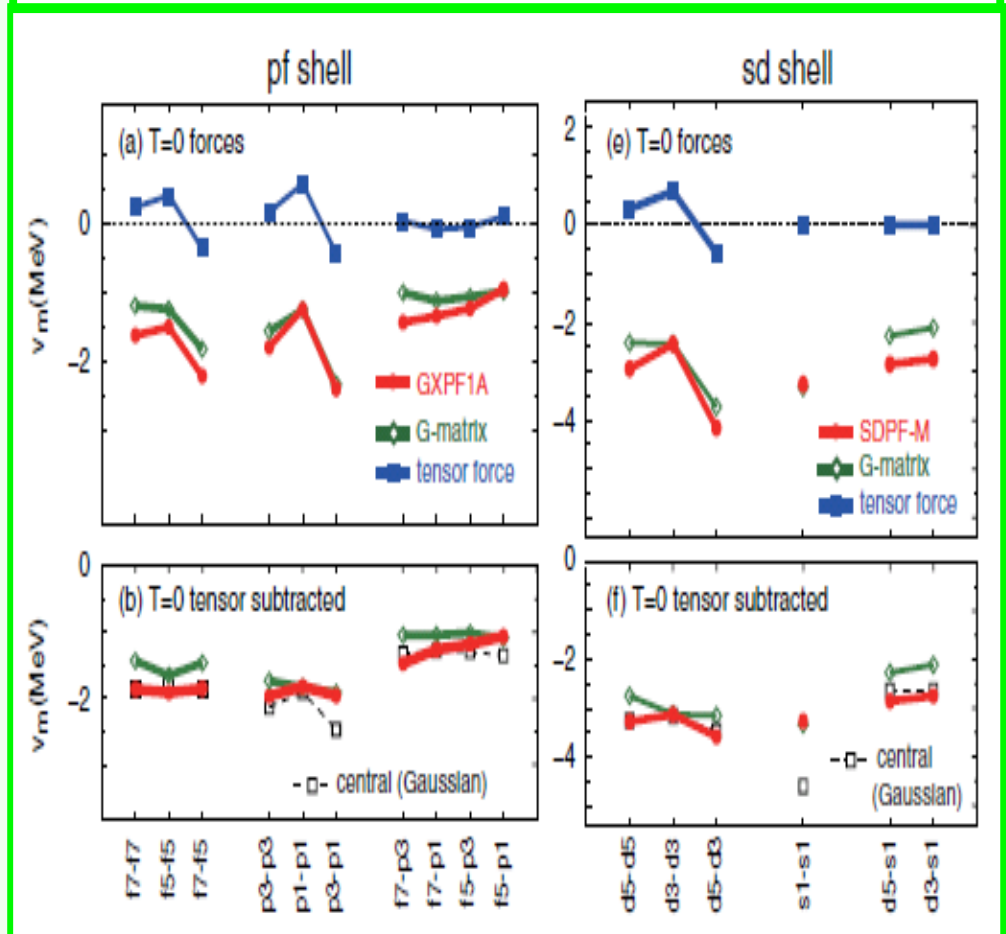
VMU= Monopole based Universal Interaction



- Important roles of tensor force
→ SFO (p, p-sd)
(Suzuki-Fujimoto-Otsuka)

Monopole terms in V_{nn}

$$V_M^T(j_1 j_2) = \frac{\sum_J (2J + 1) \langle j_1 j_2; JT | V | j_1 j_2; JT \rangle}{\sum_J (2J + 1)}$$



tensor force