



XII. Novi standardni model

MASE FERMIONA i SM NAKON OTKRIĆA OSCILACIJA NEUTRINA I POTVRDE HIGGSA

- **MASE FERMIONA**
- **MASE NEUTRINA**
- **ČAROLIJA i ENIGMA
HIGGSOVOG SEKTORA**

MASE FERMIONA ILI YUKAWINA VEZANJA

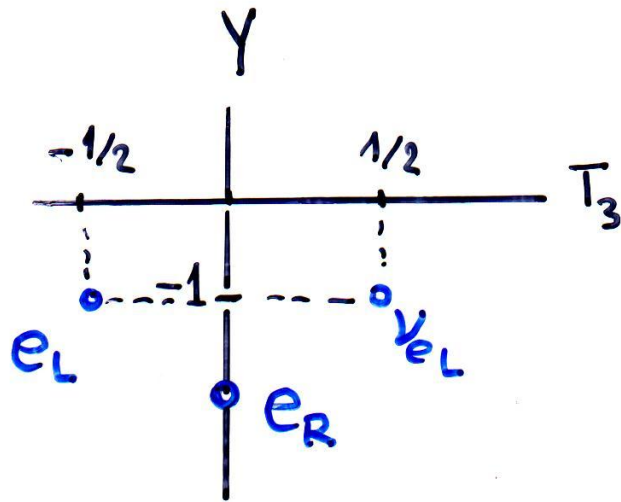
Mase fermiona generirane
 $SU(2) \times U(1)$ simetričnim
Yukawinim međudjelovanjem

12 fundamentalnih
fermiona u 3 obitelji

15 stanja heliciteta
unutar jedne obitelji

u, d, ν_e, e
 c, s, ν_μ, μ
 t, b, ν_τ, τ

Obitelj fermiona realizirana s pet reprezentacija SM-a



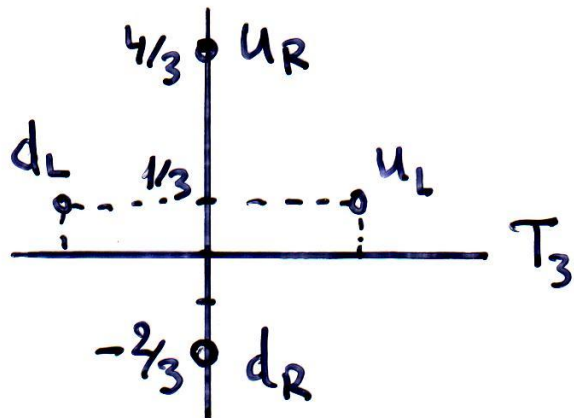
$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$$

e_R

$$SU(3)_{\text{boje}} \times SU(2) \times U(1)$$

$$(1, 2, -1)$$

$$(1, 1, -2)$$



$$\begin{pmatrix} u \\ d \end{pmatrix}_L$$

u_R

d_R

$$(3, 2, 1/3)$$

$$(3, 1, 4/3)$$

$$(3, 1, -2/3)$$

MASE LEPTONA - u unitarnom bažd.

$$m_e = \frac{y_e v}{\sqrt{2}}$$

$$\mathcal{L}_{\text{Yukawa}} \supset - \left[y_e \bar{e}_R \Phi^\dagger L_L + y_e^* \bar{L}_L \Phi e_R \right]$$
$$L_L = (\nu_L, e_L)^T$$
$$\Phi = \begin{pmatrix} 0 \\ (v+h)/\sqrt{2} \end{pmatrix}$$

■ Uz umnožak dva dubleta

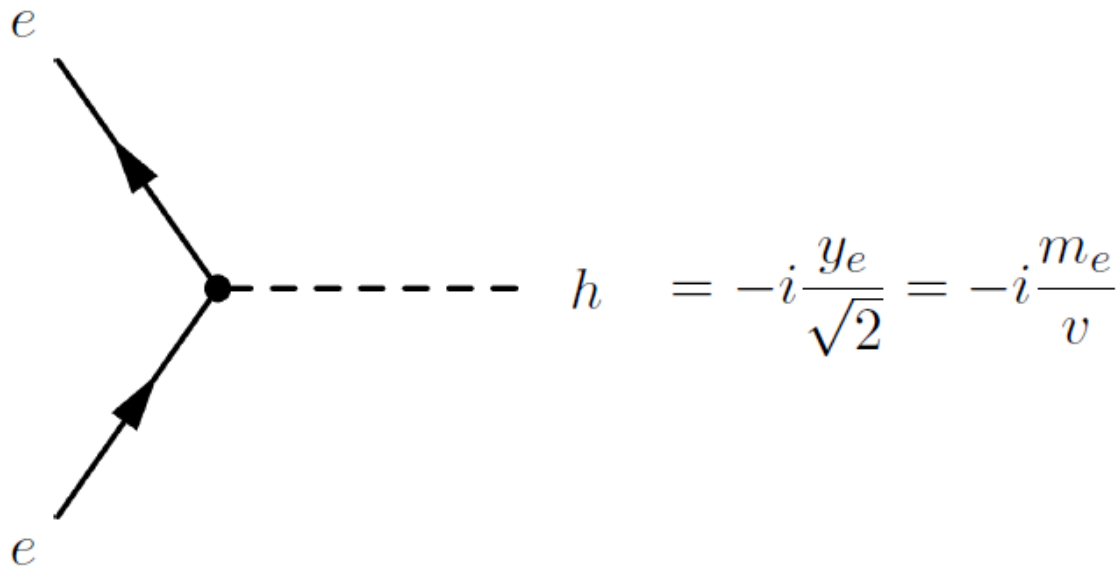
$$\Phi^\dagger L_L = \left(0, \frac{v+h}{\sqrt{2}} \right) \begin{pmatrix} \nu_e \\ e \end{pmatrix}_L = \frac{v+h}{\sqrt{2}} e_L$$

$$\mathcal{L}_{\text{Yukawa}} \supset -y_e \frac{1}{\sqrt{2}} [(v+h) \bar{e}_R e_L + (v+h) \bar{e}_L e_R]$$

$$= -\frac{y_e}{\sqrt{2}} (v+h) \bar{e} e = -\left(\frac{y_e v}{\sqrt{2}} \right) \bar{e} e - \frac{y_e}{\sqrt{2}} h \bar{e} e$$

Feynmanovo pravilo Yukawinog vrha

$$h\bar{e}e : \frac{-iy_e}{\sqrt{2}} = \frac{-im_e}{v}$$



- Odražava afinitet fermiona na higgs

$$\frac{y_e}{\sqrt{2}} = \frac{m_e}{v} = \frac{511 \text{ keV}}{246 \text{ GeV}} \simeq 2.1 \times 10^{-6}$$

$$\frac{y_\tau}{\sqrt{2}} = \frac{m_\tau}{v} = \frac{1.78 \text{ GeV}}{246 \text{ GeV}} \simeq 7.2 \times 10^{-3}$$

MASE KVARKOVA - donjih i gornjih, za realno Yukawino vezanje

$$m_d = y_d v / \sqrt{2},$$

$$m_u = y_u v / \sqrt{2}$$

$$\mathcal{L}_{\text{Yukawa}} \supset - \left[y_d \bar{d}_R \underbrace{\Phi^\dagger}_{\text{wavy}} Q_L + y_d^* \bar{Q}_L \Phi d_R \right] - \left[y_u \bar{u}_R \underbrace{\tilde{\Phi}^\dagger}_{\text{wavy}} Q_L + y_u^* \bar{Q}_L \tilde{\Phi} u_R \right]$$

$$\mathcal{L}_{\text{Yukawa}} \supset - \left(\frac{y_d v}{\sqrt{2}} \right) \bar{d} d - \frac{y_d}{\sqrt{2}} h \bar{d} d \quad \underbrace{\Phi^\dagger Q_L}_{\text{wavy}} = \begin{pmatrix} 0 & \frac{v+h}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \frac{v+h}{\sqrt{2}} d_L$$

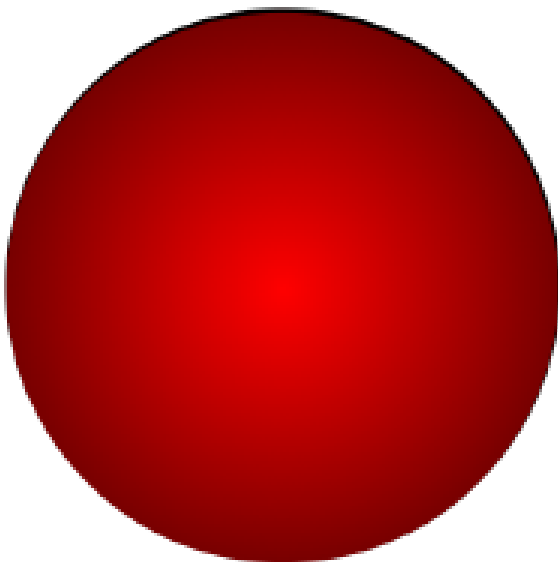
■ Uz konjugiran dublet $\underbrace{\tilde{\Phi} \equiv i\sigma^2 \Phi^*}_{\text{wavy}} = i \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \begin{pmatrix} \phi^- \\ \phi^{0*} \end{pmatrix} = \begin{pmatrix} \phi^{0*} \\ -\phi^- \end{pmatrix}$

$$\mathcal{L}_{\text{Yukawa}} \supset - \left(\frac{y_u v}{\sqrt{2}} \right) \bar{u} u - \frac{y_u}{\sqrt{2}} h \bar{u} u \quad \underbrace{\tilde{\Phi}^\dagger Q_L}_{\text{wavy}} = \begin{pmatrix} \frac{v+h}{\sqrt{2}} & 0 \end{pmatrix} \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \frac{v+h}{\sqrt{2}} u_L$$

Up Quark
~ 0.002 GeV

Charm Quark
1.25 GeV

Top Quark
175 GeV



Down Quark
~ 0.005 GeV

Strange Quark
~ 0.095 GeV

Bottom Quark
4.2 GeV

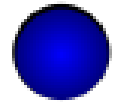
These are relative masses not size – they have no measurable size

Electron
0.0005 GeV

Muon
0.105 GeV

Tau
1.78 GeV

For reference:



Proton
0.938 GeV

Electron Neutrino
~ 0

Muon Neutrino
~ 0

Tau Neutrino
~ 0

Originally thought to be massless but now not

Raspad Higgsovog bozona na fermionsko-antiferminski par

■ Invarijantna amplituda

$$i\mathcal{M} = \bar{u}_f \left(\frac{-im_f}{v} \right) v \bar{f}$$

čije kvadriranje, sumiranje po polarizacijama (i bojama) i integracija po 2-čestičnom faznom prostoru, daje parcijalnu širinu raspada:

$$\Gamma(h \rightarrow f\bar{f}) = \frac{N_c}{8\pi} \frac{m_f^2}{v^2} m_h \left[1 - \frac{4m_f^2}{m_h^2} \right]^{3/2}$$

Miješanje kvarkovskih generacija

$$Q_{Lj}, \quad u_{Rj}, \quad d_{Rj}, \quad j = 1, 2, 3$$

$$\mathcal{L}_{\text{Yukawa}}^q = - \sum_{i=1}^3 \sum_{j=1}^3 \left[y_{ij}^u \bar{u}_{Ri} \tilde{\Phi}^\dagger Q_{Lj} + y_{ij}^d \bar{d}_{Ri} \Phi^\dagger Q_{Lj} \right] + \text{h.c.}$$

$$\mathcal{L}_{\text{Yukawa}}^q \supset - (\bar{u}_1, \bar{u}_2, \bar{u}_3)_R \mathcal{M}^u \begin{pmatrix} u_1 \\ u_2 \\ u_3 \end{pmatrix}_L - (\bar{d}_1, \bar{d}_2, \bar{d}_3)_R \mathcal{M}^d \begin{pmatrix} d_1 \\ d_2 \\ d_3 \end{pmatrix}_L + \text{h.c.}$$

u unit. bažd. kompleksne Yukawine
(3x3) matrice vode na matrice masa

$$\mathcal{M}_{ij}^u = \frac{v}{\sqrt{2}} y_{ij}^u, \quad \mathcal{M}_{ij}^d = \frac{v}{\sqrt{2}} y_{ij}^d$$

BAZA KVARKOVSKIH MASA -

dijagonalizacijom biunitarnim transform. $U^{-1} = U^\dagger$

$$\begin{pmatrix} u_1 \\ u_2 \\ u_3 \end{pmatrix}_{L,R} = U_{L,R} \begin{pmatrix} u \\ c \\ t \end{pmatrix}_{L,R}, \quad \begin{pmatrix} d_1 \\ d_2 \\ d_3 \end{pmatrix}_{L,R} = D_{L,R} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{L,R}$$

■ Dijagonalizacija masa/Yukawinih matrica

$$U_R^{-1} \mathcal{M}^u U_L = \begin{pmatrix} m_u & 0 & 0 \\ 0 & m_c & 0 \\ 0 & 0 & m_t \end{pmatrix}, \quad D_R^{-1} \mathcal{M}^d D_L = \begin{pmatrix} m_d & 0 & 0 \\ 0 & m_s & 0 \\ 0 & 0 & m_b \end{pmatrix}$$

■ Dijagonalna i realna Higgsova vezanja u bazi masa

$$h\bar{q}q : \frac{-iy_q}{\sqrt{2}} = \frac{-im_q}{v}$$

CKM miješanje u nabijenoj struji & okusno dijagonalna neutralna

$$J_L^{+\mu} = (\bar{u}_1, \bar{u}_2, \bar{u}_3)_L \gamma^\mu \begin{pmatrix} d_1 \\ d_2 \\ d_3 \end{pmatrix}_L = (\bar{u}, \bar{c}, \bar{t})_L U_L^\dagger \gamma^\mu D_L \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L = (\bar{u}, \bar{c}, \bar{t})_L \gamma^\mu V \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L$$

CKM matrica

$$U_L^\dagger D_L \equiv V$$

je unitarna $V^\dagger V = (U_L^\dagger D_L)^\dagger (U_L^\dagger D_L) = D_L^\dagger U_L U_L^\dagger D_L = 1$

- Univerzalno vezanje fotona i Z bozona: Q
 GIM i granasta odsutnost FCNC $(T^3 - s_W^2 Q)$

$$(\bar{u}_1, \bar{u}_2, \bar{u}_3)_L \gamma^\mu \begin{pmatrix} u_1 \\ u_2 \\ u_3 \end{pmatrix}_L = (\bar{u}, \bar{c}, \bar{t})_L U_L^\dagger \gamma^\mu U_L \begin{pmatrix} u \\ c \\ t \end{pmatrix}_L = (\bar{u}, \bar{c}, \bar{t})_L \gamma^\mu \begin{pmatrix} u \\ c \\ t \end{pmatrix}_L$$

Za više obitelji (generacija)
 -općenito Yukawin lagrangian
 nije dijagonalan u okusu

$$- \mathcal{L}_Y = G_{ij}^{(d)} \bar{Q}'_{Li} \Phi D'_{Rj} + G_{ij}^{(u)} \bar{Q}'_{Li} \tilde{\Phi} U'_{Rj} + h.c.$$

Nakon SSB :

$$- \mathcal{L}_Y = \left(1 + \frac{H(x)}{2} \right) \sum_{i,j=1}^3 \left\{ (m_U)_{ij} \bar{U}'_{Li} U'_{Rj} + (m_D)_{ij} \bar{D}'_{Li} D'_{Rj} + h.c. \right\}$$

$$U' = \begin{pmatrix} u' \\ c' \\ t' \end{pmatrix} \quad D' = \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}$$

matrice mase u "bazdarnoj" bazi
nisu dijagonalne

$$(m_U)_{ij} = -\frac{v}{\sqrt{2}} G_{ij}^{(u)} \quad ; \quad (m_D)_{ij} = -\frac{v}{\sqrt{2}} G_{ij}^{(d)}$$

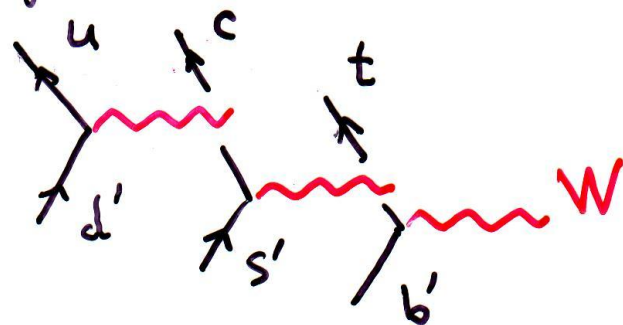
Prijelaz na "fizikalnu" bazu

$$U_L = V_L^U U_L' = V_L^U \begin{pmatrix} u' \\ c' \\ t' \end{pmatrix}_L \quad ; \quad D_L = V_L^D D_L' = V_L^D \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_L$$

daje dijagonalne matrice mase

$$\mathcal{L}_M = -[\bar{U}_L \text{diag}(m_u, m_c, m_t) U_R + \bar{D}_L \text{diag}(m_d, m_s, m_b) D_R + \text{h.c.}]$$

U fizikalnoj bazi (dobro def. masa)
 "zakomplicira" se nabijena slaba struja



$$-\mathcal{L}_{cc} = \frac{g}{\sqrt{2}} (\bar{U}'_L \gamma^\mu W_\mu^+ D'_L + \text{h.c.})$$

$$\rightarrow \frac{g}{\sqrt{2}} [\bar{U}_L \gamma^\mu (V_L^U V_L^{D\dagger}) D_L + \text{h.c.}]$$

volimo oznaku

$$U_L^\dagger D_L \equiv V$$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

(n x n)

$$n^2 - (2n-1) = (n-1)^2 = \frac{n(n-1)}{2} + \frac{(n-1)(n-2)}{2}$$

kutova

komplex. faza

Pogodan je odabir slabe baze u kojoj su gornji kvarkovi masena stanja. Izospinski dubleti tada imaju zapis

$$\begin{pmatrix} u \\ d' \end{pmatrix}_L, \quad \begin{pmatrix} c \\ s' \end{pmatrix}_L, \quad \begin{pmatrix} t \\ b' \end{pmatrix}_L,$$

- gdje je V u prostoru generacija

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_L = V \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L.$$

"STANDARDNA" PARAMETRIZACIJA - POGODNA ZA POOPĆENJE NA $n > 3$

$$V = R_{23} \times R_{13} \times R_{12}$$

$$R_{12} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad R_{13} = \begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta} \\ 0 & i\delta & 1 \\ -s_{13} e^{i\delta} & 0 & c_{13} \end{pmatrix}, \quad R_{23} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}$$

"standard parametrization"

with $c_{ij} \equiv \cos \vartheta_{ij}$, $s_{ij} \equiv \sin \vartheta_{ij}$,
 i & j labeling quark families

$$V_{PDG} \approx \begin{pmatrix} c_{12} c_{13} & s_{12} c_{13} \\ -s_{12} c_{23} & c_{12} c_{23} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i\delta_{13}} & -c_{12} s_{23} \\ & s_{13} e^{-i\delta_{13}} \\ & s_{23} c_{13} \\ & c_{23} c_{13} \end{pmatrix}$$

Wolfenstein's [PRL 51 ('83) 1945] approx. with $\lambda \equiv \sin \Theta_c = 0.221$

POSAO FIZIKE OKUSA

$u \leftrightarrow d$
 β decay
 μ decay
 $\pi^+ \rightarrow \pi^0 e^+ \nu$

$u \leftrightarrow s$
 $K \rightarrow \pi e \nu$
 Hyperon β dec's

$u \leftrightarrow b$
 charmless
 b decays

$|V_{CKM}| \sim$

$$\begin{bmatrix} 1 & 0.22 & 0.004 \\ 0.22 & 1 & 0.04 \\ 0.01 & 0.04 & 1 \end{bmatrix}$$

$c \leftrightarrow d$
 ν prod. of charm
 $\nu_{\mu} d \rightarrow \mu^- c$

$c \leftrightarrow s$
 $D \rightarrow K e \nu$
 $\bar{\nu}_{\mu} s \rightarrow \mu^+ \bar{c}$

$c \leftrightarrow b$
 b -decays

$t \leftrightarrow d$ $t \leftrightarrow s$
 [only indirect evidence]

$t \leftrightarrow b$
 dominance
 of $t \rightarrow W b$

6 ZAHTJEVA UNITARNOSTI: 3 "GORNJA" TROKUTA

$$\begin{array}{l} V_{ud}V_{cd}^* + V_{us}V_{cs}^* + V_{ub}V_{cb}^* = 0 \\ \sim \lambda \quad \quad \quad \sim \lambda \quad \quad \quad \sim \lambda^5 \end{array}$$

$$\begin{array}{l} V_{ud}V_{td}^* + V_{us}V_{ts}^* + V_{ub}V_{tb}^* = 0 \\ \sim \lambda^3 \quad \quad \quad \sim \lambda^3 \quad \quad \quad \sim \lambda^3 \end{array}$$

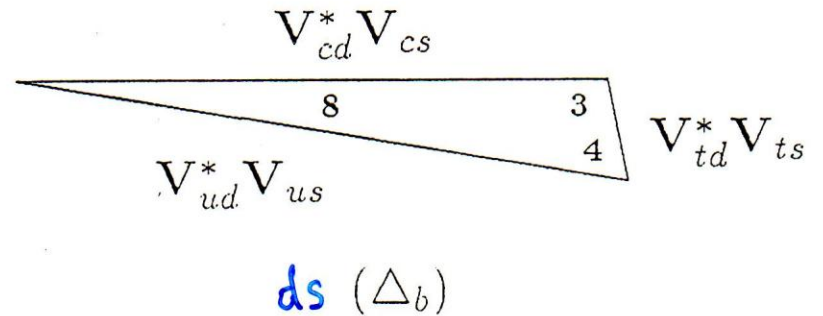
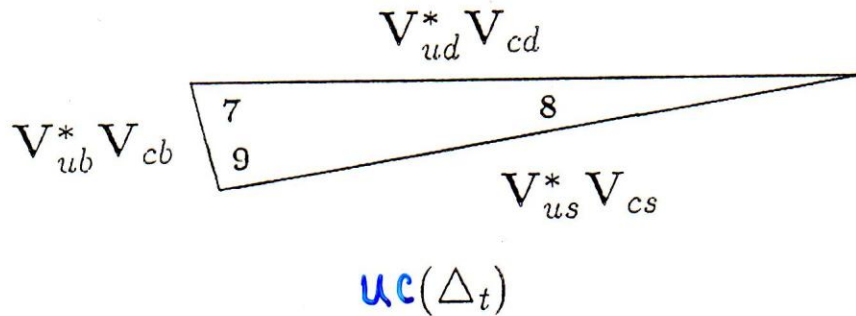
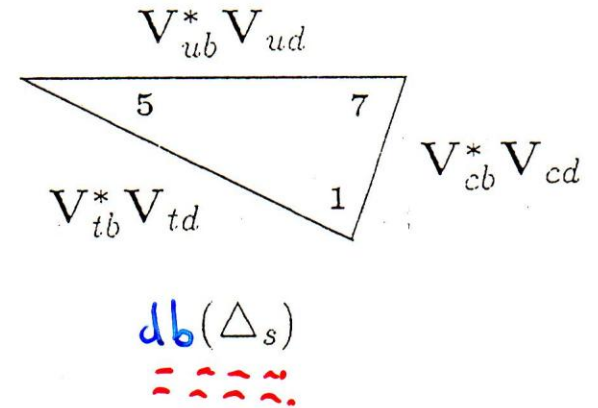
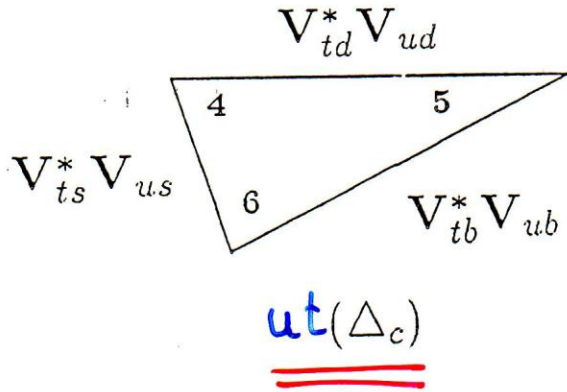
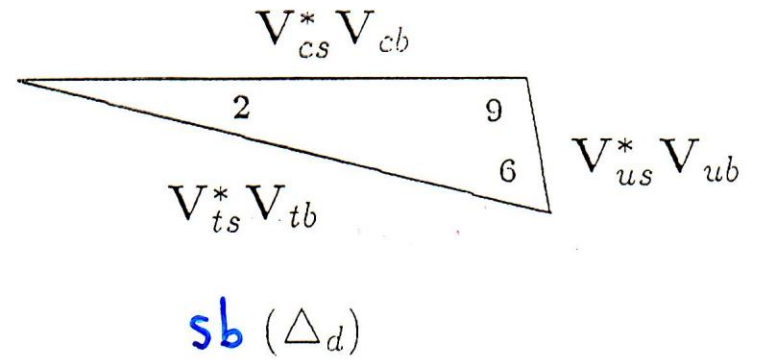
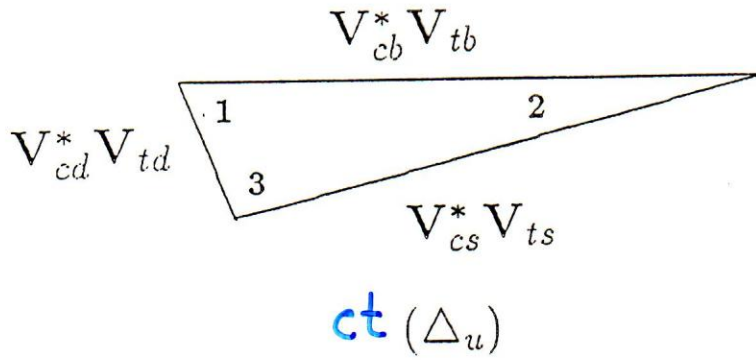
$$\begin{array}{l} V_{cd}V_{td}^* + V_{cs}V_{ts}^* + V_{cb}V_{tb}^* = 0 \\ \sim \lambda^4 \quad \quad \quad \sim \lambda^2 \quad \quad \quad \sim \lambda^2 \end{array}$$

& 3 "donja" UNITARNA TROKUTA

$$\begin{array}{ccccccc} V_{ud}^* V_{us} & + & V_{cd}^* V_{cs} & + & V_{td}^* V_{ts} & = & 0 \\ \sim \lambda & & \sim \lambda & & \sim \lambda^5 & & \end{array}$$

$$\begin{array}{ccccccc} V_{ud}^* V_{ub} & + & V_{cd}^* V_{cb} & + & V_{td}^* V_{tb} & = & 0 \\ \sim \lambda^3 & & \sim \lambda^3 & & \sim \lambda^3 & & \end{array}$$

$$\begin{array}{ccccccc} V_{us}^* V_{ub} & + & V_{cs}^* V_{cb} & + & V_{ts}^* V_{tb} & = & 0 \\ \sim \lambda^4 & & \sim \lambda^2 & & \sim \lambda^2 & & \end{array}$$

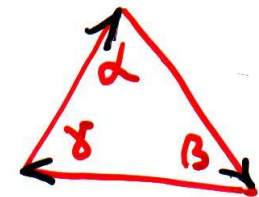
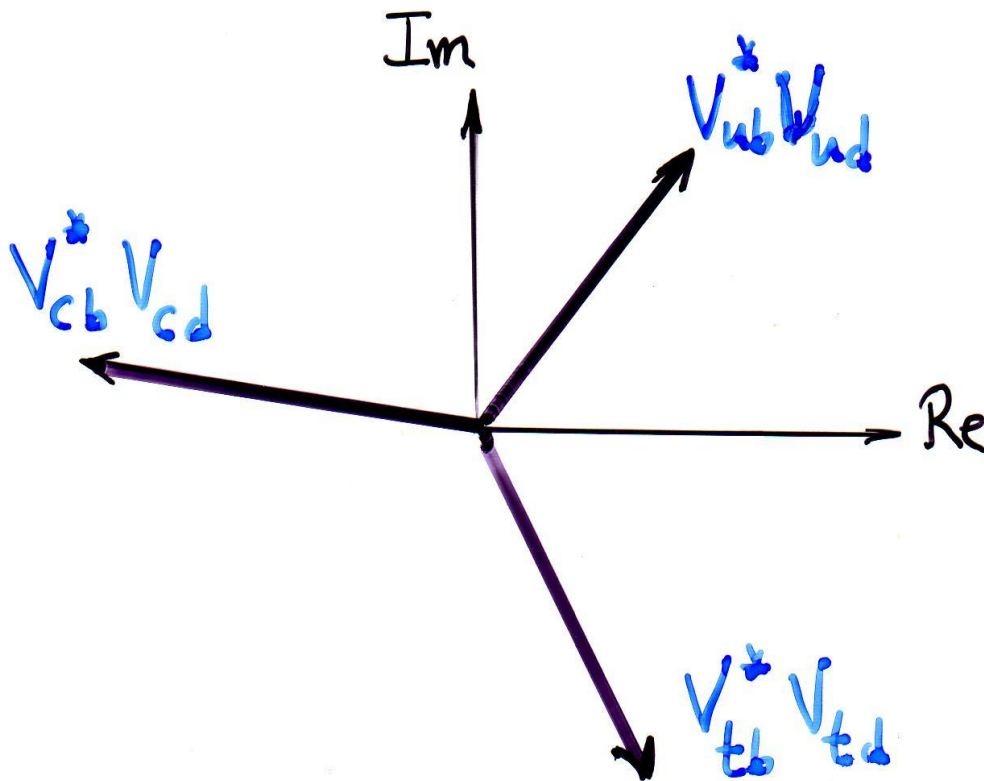


Unitarity (e.g. (db) :

$$V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$

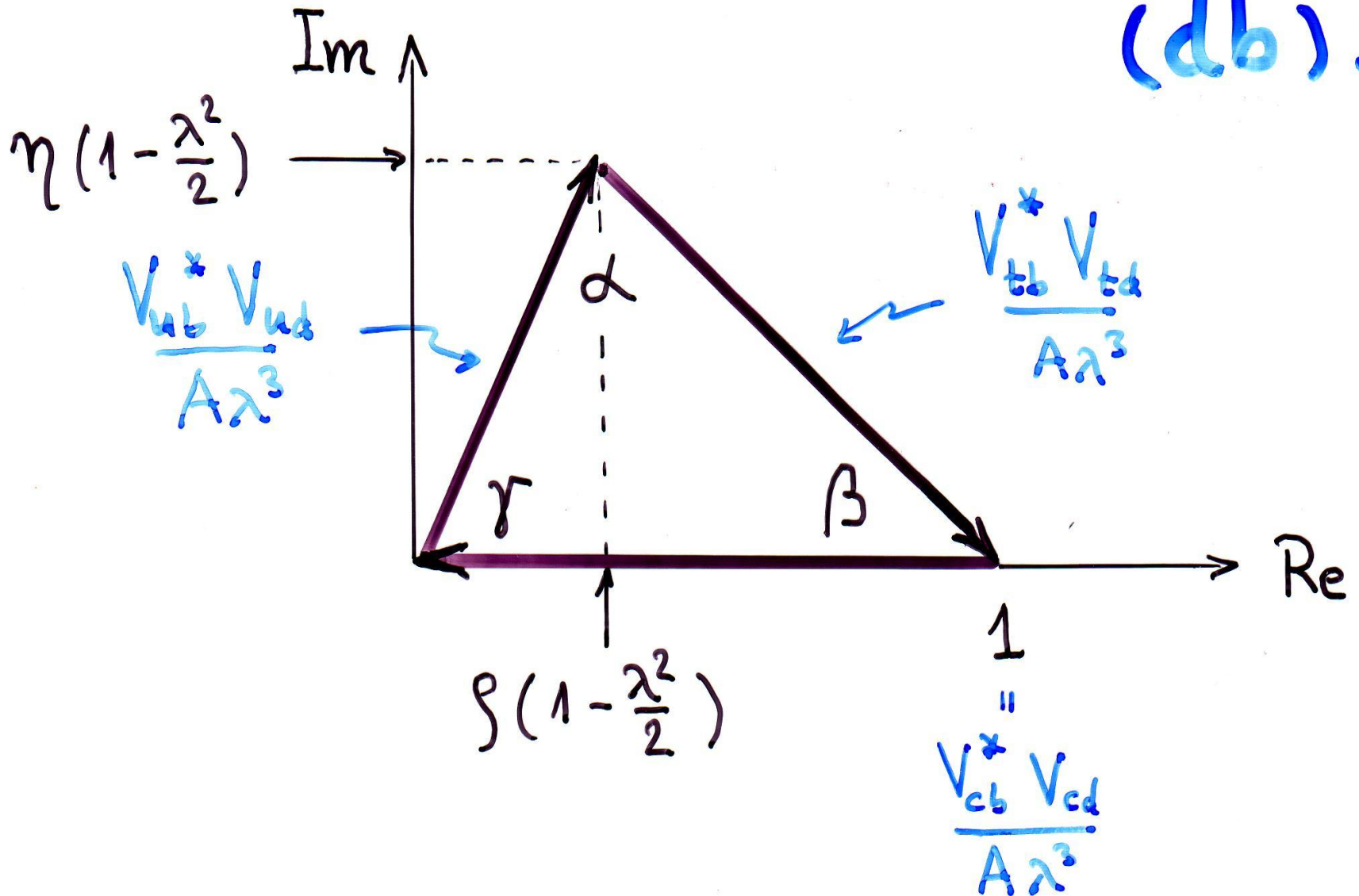
\Rightarrow triangle closes

$$\alpha + \beta + \gamma = \pi$$



The two non-squashed unitarity triangles

(db):



Miješanje leptona (Pontecorvo-Maki-Nakagawa-Sakata)

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} V_{e1} & V_{e2} & V_{e3} \\ V_{\mu 1} & V_{\mu 2} & V_{\mu 3} \\ V_{\tau 1} & V_{\tau 2} & V_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

utvrđeno na temelju pojave
OSCILACIJA NEUTRINA

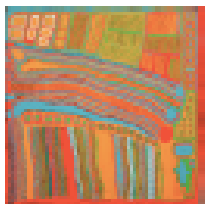
prva opipljiva naznaka fizike izvan
standardnog modela

Kao za kvarkove, moguć je odabir slabe baze u kojoj su nabijeni leptoni masena stanja. Izospinski dubleti tada imaju zapis

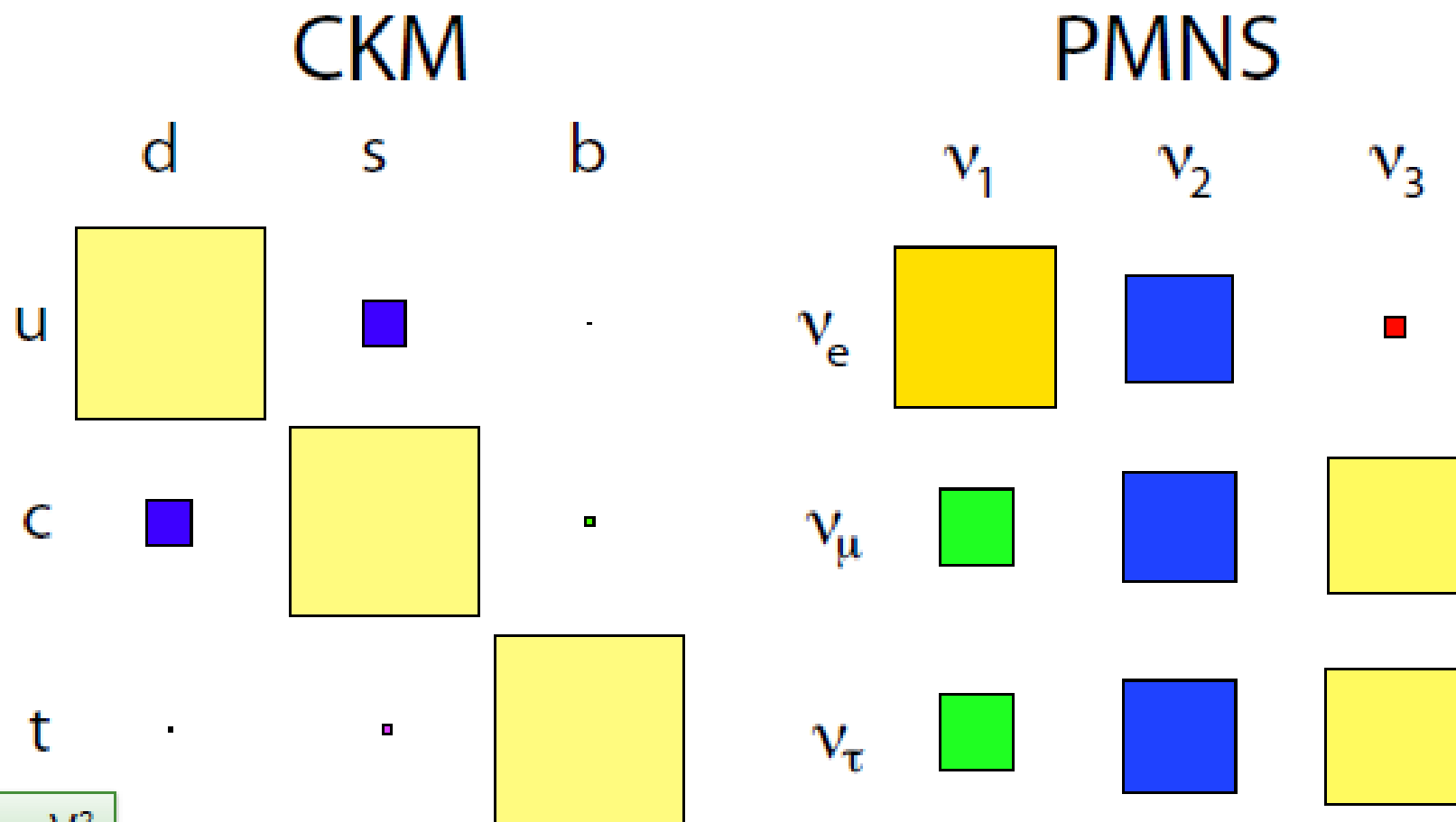
$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L, \quad \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L, \quad \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L,$$

- tako da PMNS matrica povezuje okusna stanja neutrina s masenim (1,2,3)

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}_L = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}_L$$



CKM vs. PMNS



Area $\sim V^2$

Why these values? Are the two related? Are they related to masses?

$$|U_{\text{LEP}}| = \begin{pmatrix} 0.73 - 0.89 & 0.44 = 0.66 & < 0.24 \\ 0.23 - 0.66 & 0.24 = 0.75 & 0.51 - 0.87 \\ 0.06 - 0.57 & 0.40 = 0.82 & 0.48 - 0.85 \end{pmatrix}.$$

$$|U_{\text{LEP}}| \simeq \begin{pmatrix} \frac{1}{\sqrt{2}}(1 + \mathcal{O}(\lambda)) & \frac{1}{\sqrt{2}}(1 - \mathcal{O}(\lambda)) & \epsilon \\ -\frac{1}{2}(1 - \mathcal{O}(\lambda) + \epsilon) & \frac{1}{2}(1 + \mathcal{O}(\lambda) - \epsilon) & \frac{1}{\sqrt{2}} \\ \frac{1}{2}(1 - \mathcal{O}(\lambda) - \epsilon) & -\frac{1}{2}(1 + \mathcal{O}(\lambda) - \epsilon) & \frac{1}{\sqrt{2}} \end{pmatrix} \quad \begin{array}{l} \lambda \sim 0.2 \\ \epsilon < 0.25 \end{array}$$

from quark's

$$|U_{\text{CKM}}| \simeq \begin{pmatrix} 1 & \mathcal{O}(\lambda) & \mathcal{O}(\lambda^3) \\ \mathcal{O}(\lambda) & 1 & \mathcal{O}(\lambda^2) \\ \mathcal{O}(\lambda^3) & \mathcal{O}(\lambda^2) & 1 \end{pmatrix} \quad \lambda \sim 0.2$$

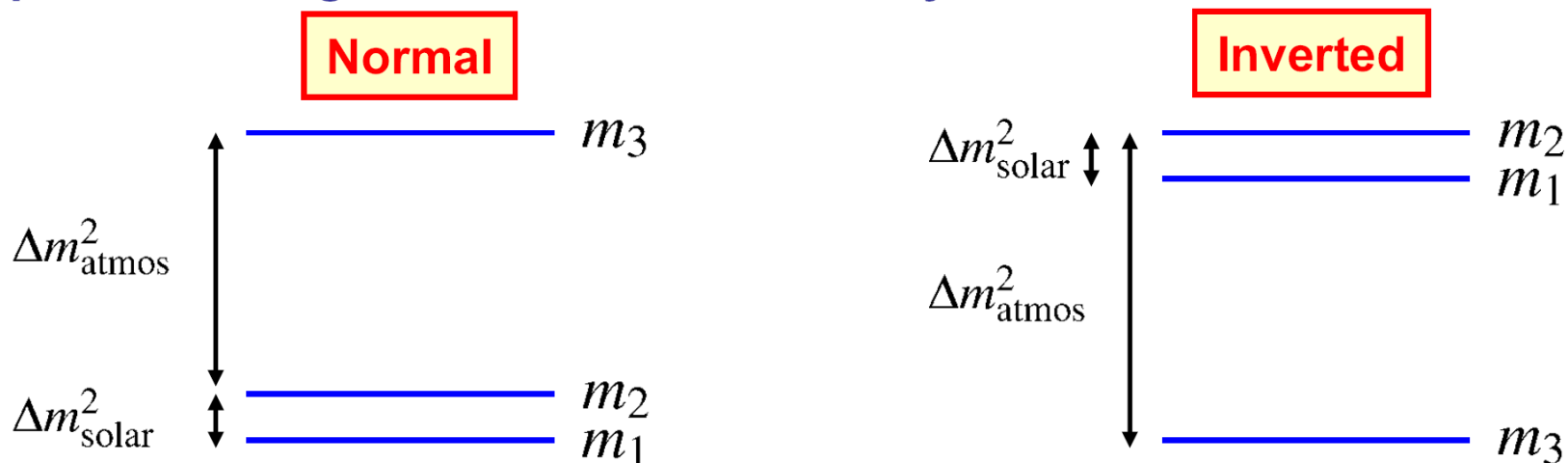
★ To date, results on neutrino oscillations only determine

$$|\Delta m_{ji}^2| = |m_j^2 - m_i^2|$$

★ Two distinct and very different mass scales:

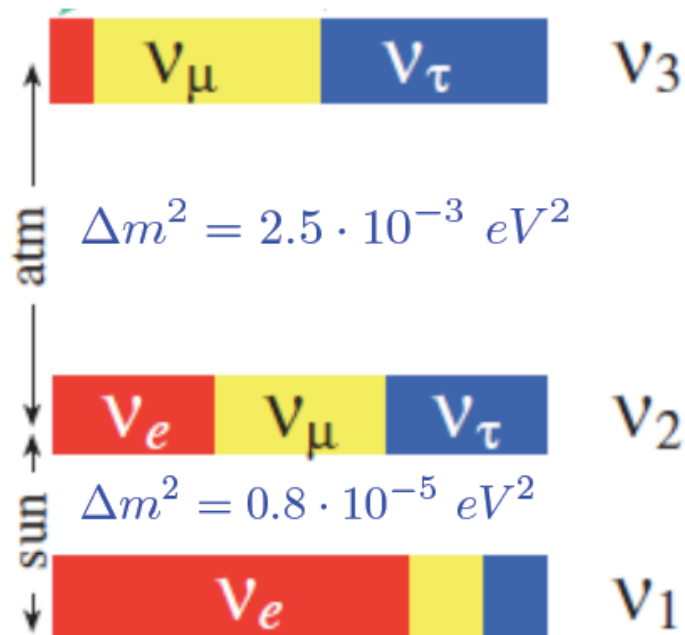
- Atmospheric neutrino oscillations : $|\Delta m^2|_{\text{atmos}} \sim 2.5 \times 10^{-3} \text{ eV}^2$
- Solar neutrino oscillations: $|\Delta m^2|_{\text{solar}} \sim 8 \times 10^{-5} \text{ eV}^2$

• Two possible assignments of mass hierarchy:

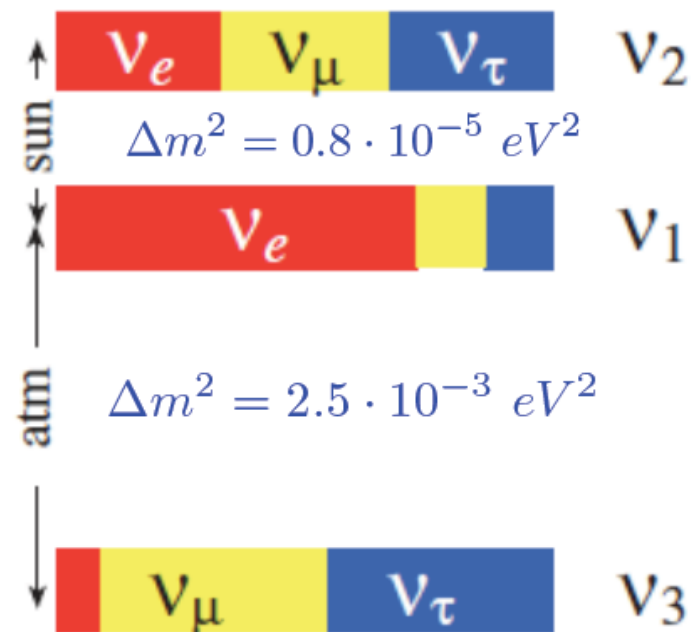


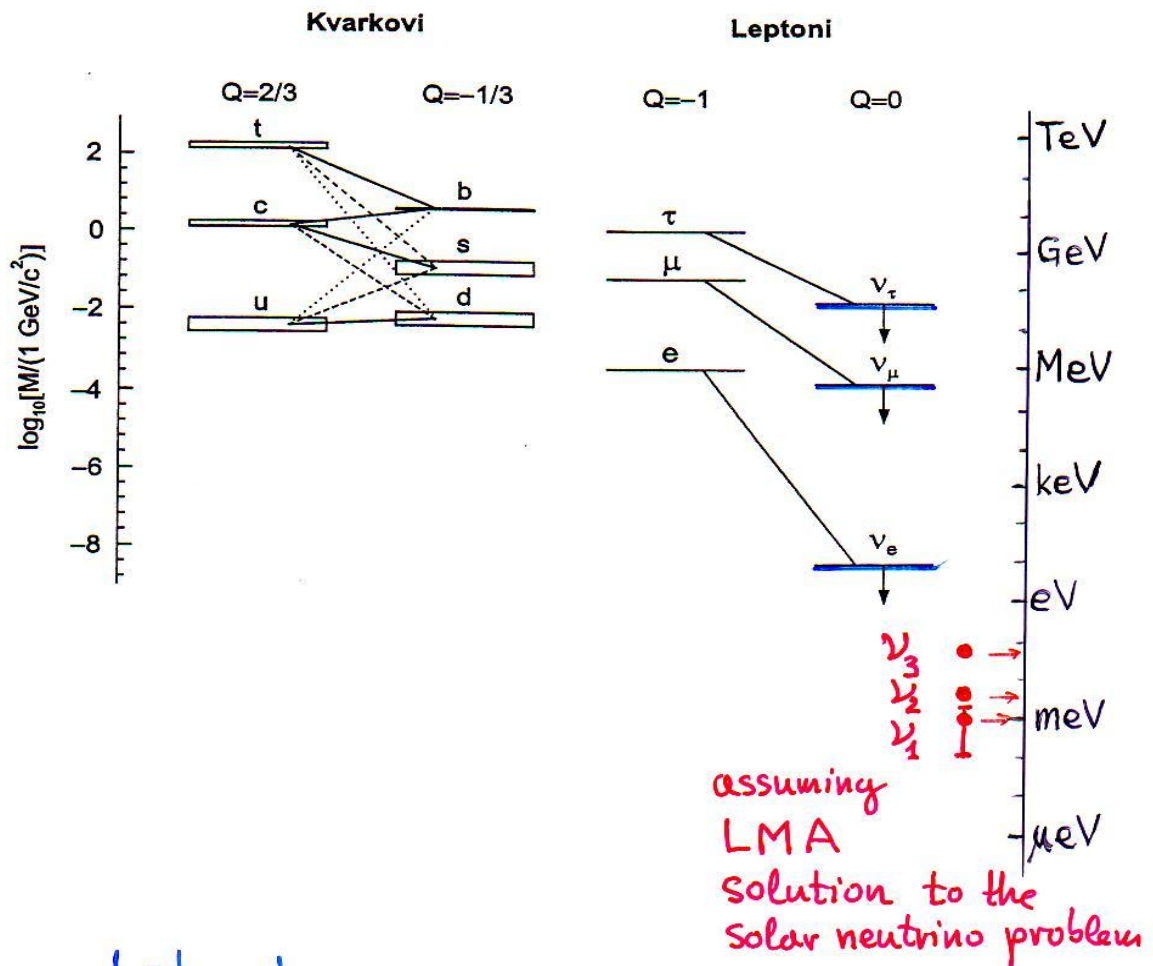
- In both cases: $\Delta m_{21}^2 \sim 8 \times 10^{-5} \text{ eV}^2$ (solar)
- $|\Delta m_{31}^2| \approx |\Delta m_{32}^2| \sim 2.5 \times 10^{-3} \text{ eV}^2$ (atmospheric)

NORMALNA I INVERZNA HIJERARHIJA MASA NEUTRINA



normal
or
inverted
hierarchy?





Laboratory mass limits:

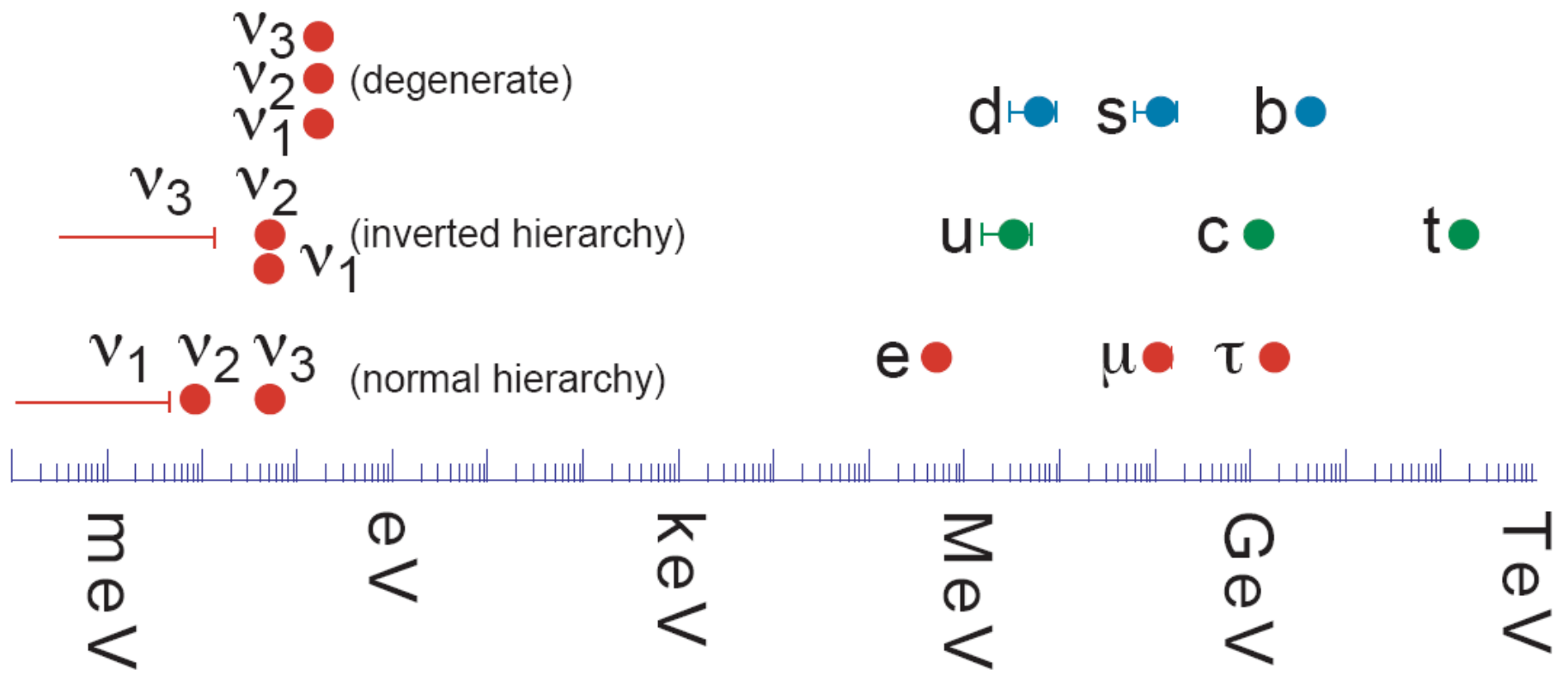
$m_{\nu_e} < 5 \text{ eV}$ (^3H β -decay)

$m_{\nu_\mu} < 0.17 \text{ MeV}$ (PSI)

$m_{\nu_\tau} < 18.2 \text{ MeV}$ (ALEPH)

Neutrinske mase kao opipljivo odstupanje od SM-a Fig. Murayama'08

fermion masses



PERIODIČKA TABLICA SM-a

Three Generations
of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III		
mass →	2.4 MeV	1.27 GeV	173.2 GeV	0	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
name →	Left u Right up	Left c Right charm	Left t Right top	g gluon	
Quarks	4.8 MeV	104 MeV	4.2 GeV	0	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	0
	Left d Right down	Left s Right strange	Left b Right bottom	γ photon	
	0 ν_e electron neutrino	0 ν_μ muon neutrino	0 ν_τ tau neutrino	91.2 GeV	126 GeV
Leptons	0.511 MeV	105.7 MeV	1.777 GeV	0	0
	-1	-1	-1	0	0
	Left e Right electron	Left μ Right muon	Left τ Right tau	Z weak force	H Higgs boson
			80.4 GeV		spin 0
			± 1		
			W weak force		

Bosons (Forces) spin 1

NAKON OTKRIĆA HIGGSA

3 parametra Higgsovog potencijala

$$V = \text{const.} + m_H^2 |H|^2 + \lambda |H|^4$$

- Problem kozmološke konstante
- Problem prirodnosti higgsa
- Problem vakuumske stabilnosti

Diracove mase neutrina ukoliko postoje i desni neutрини ν_{Ri} ($i = 1, 2, 3$)

$$\mathcal{L}_{\text{Yukawa}} \supset -y_\nu \bar{\nu}_R \tilde{\Phi}^\dagger L_L + \text{h.c.}$$

$$\mathcal{L}_{\text{Yukawa}}^\ell = - \sum_{i=1}^3 \sum_{j=1}^3 \left[\underset{=}{y_{ij}^\nu} \bar{\nu}_{Ri} \tilde{\Phi}^\dagger L_{Lj} + y_{ij}^\ell \bar{e}_{Ri} \Phi^\dagger L_{Lj} \right] + \text{h.c.}$$

- PMNS miješanje okusnih i masenih (1, 2, 3) stanja, pri čemu male mase neutrina

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}_L = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}_L$$

expt.
 $m_\nu \sim 0.1 \text{ eV}$



$$\frac{y_\nu}{\sqrt{2}} = \frac{m_\nu}{v} \simeq 4 \times 10^{-13}$$



Weinbergov operator dim 5,
 generiran česticama nove fizike skale
 Λ , daje Majoraninu masu neutrina

$$\mathcal{L}_{\text{Majorana}} = -\frac{(\tilde{\Phi}^\dagger L_L)^2}{\Lambda} \quad m\nu_L\nu_L$$

- nakon SSB, iz korektno napisanog operatora izraženog konjugiranim "L" spinorom koji se Lor-transf. kao "R"

$$\bar{L}_L^c \equiv -L_L^T C, \quad C = -i\gamma^2\gamma^0$$

$$\mathcal{L}_{\text{Majorana}} = -\frac{y_{ij}^{\text{Maj}}}{\Lambda} \bar{L}_{Li}^c \tilde{\Phi}^* \tilde{\Phi}^\dagger L_{Lj} \quad \Delta L = 2$$

COUNTING the SM's FREE PARAMETERS

3 Gauge couplings

3 g_s, g, g'

or $\alpha = \frac{e^2}{4\pi}$, Θ_w , Λ_{QCD}

2 Higgs parameters

2 μ, λ

or M_H, λ

9 fermion masses

m_e, m_u, m_d ; m_μ, m_c, m_s ; m_τ, m_t, m_b

4 CKM parameters for 3 generations

ν_1, ν_2, ν_3 (mixing angles) & δ (CP-phase)

1 parameter of CP in QCD

Θ_{QCD}

19 parameters in the minimal case
(massless neutrinos)

"OLD SM"

EXTRA PARAMETERS

IN THE "NEW SM" \supset SM

◇ after SNO results

3 neutrino masses

4 MNSP parameters

3 mixing angles & 1 CP-phase

⇒ 7

eventually (in the see-saw scenario)

3 Majorana N's masses

2 other angles

⇒ 12 new parameters