

V. Fizika čestica na ubrzivačima (I)

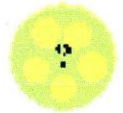
PRODUKCIJE ČESTICA PRIJE ERE HADRONSKIH SUDARIVAČA

- OD OKUSNIH MULTIPLETA DO SUDARA:
- ELEKTRON - PROTON
- ELEKTRON - POZITRON
- PROTON - AT. JEZGRE
- PROTON - ANTIPROTON
- PROTON - PROTON (LHC)

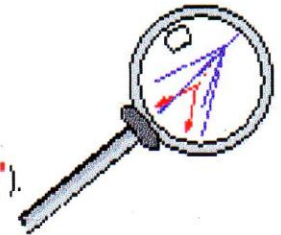
KRATKA POVIJEST HADRONSKJE FIZIKE

1932: Discovery of the **neutron**

1933: $\vec{\mu}_p \cong 2.5 \frac{e}{2 m_p} \vec{\sigma} \Rightarrow$ **Substructure** of the proton

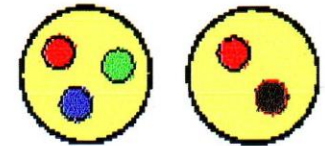


1947: Discovery of π -mesons and of long-lived V-particles (K^0, Λ) in **cosmic rays**

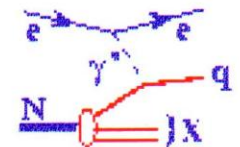


1953: V-particles produced at **accelerators**; new inner quantum number ('**strangeness**').

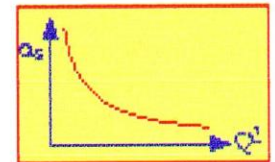
1964: Static **Quark-Model**; new inner quantum number: **color**.



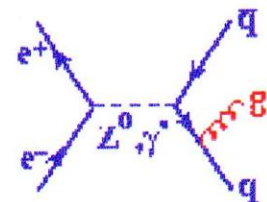
1969: Dynamic **Parton Model**:



1973: Concept of **Asymptotic Freedom**; non-abelian gauge theory: **QCD**.

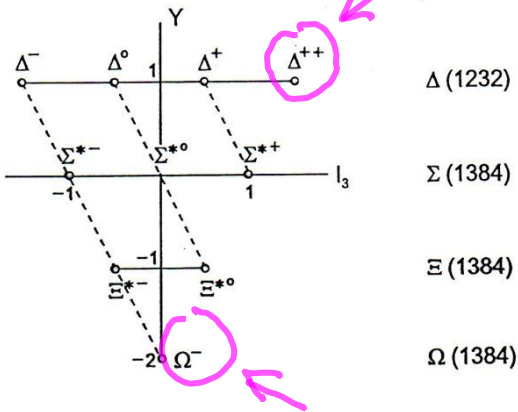
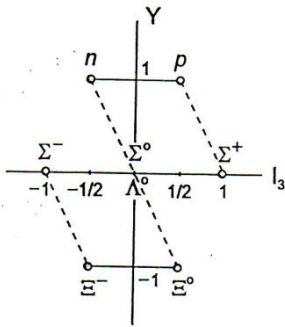
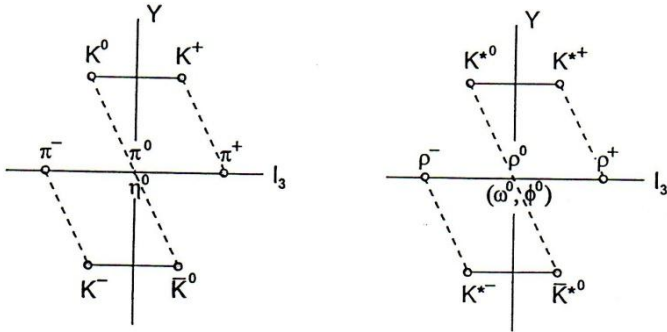


1975: **2-Jet structure** in e^+e^- -annihilation; confirmation of **Quark-Parton-Model**.



1979: Discovery of the **gluon** in **3-Jet**-events of e^+e^- -annihilation.

OD IZOSPINA DO OKUSA DIJAGRAMI KVARKOVSKOG TOKA



PRODUKCIJA STRANOSTI

- DIJAGRAMI KVARKOVSKOG TOKA
- KVARKOVSKA STANJA (uuu) i (sss) & "BOJA"

POJAM PŘIBLIŽNE SIMETRIJE

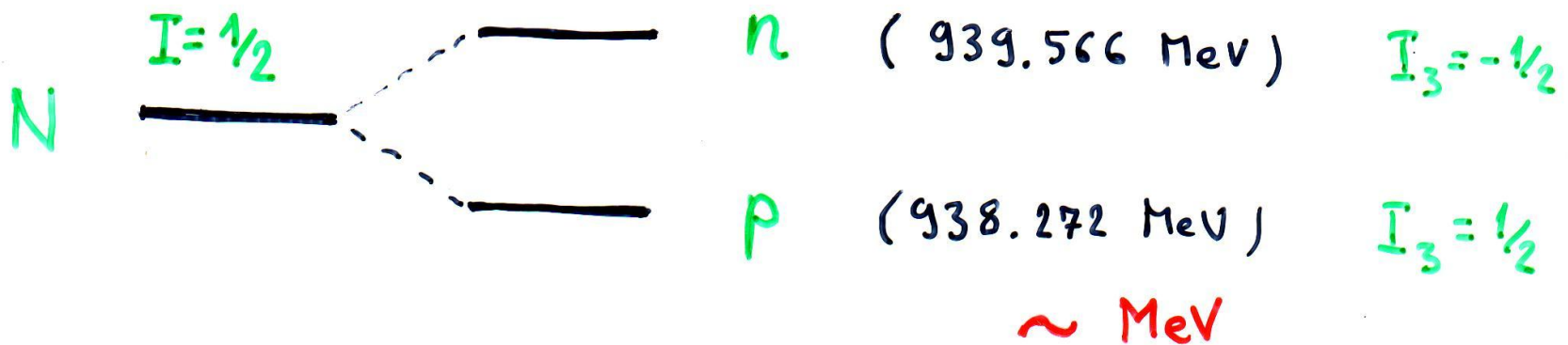
- JAKO MEĎUDJELOVANJE POKAZUJE NAJVIŠE SIMETRIJA
- OD NABOJNE SIMETRIJE JAKE SILE DO IZOSPINA
(FEČ § 2.1.3 str. 58)
- OD IZOSPINA DO OKUSA
(FEČ § 4.1.2, str. 188)

SLOMLJENA SIMETRIJA

ČESTIČNOG SPEKTRA *

SU(2)
IZOSPIN-a

narušena u prisutnosti
elektromagnetskog međudjelovanja



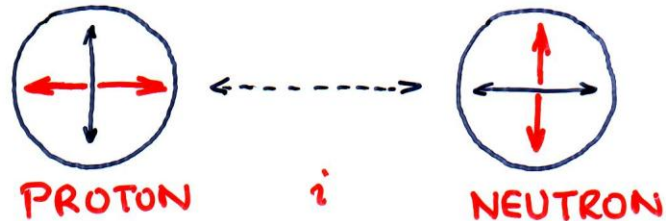
* Wigner-Weylova realizacija simetrije

SU(2)

$$e^{i\epsilon^a \frac{\tau^a}{2}}$$

NE ABELOVSKA
Yang-Millsova

primjenice, rotacije u
apstraktnom izospinskom
internom prostoru, povezuju



Globalni \mathcal{E} - istodobno isti posvuda ;
ista rotacija (konvencija) primjenjuje
se na svim nukleonskim stanjima u svemiru!

(simetrija jakog nuklearnog međudjelovanja

$$[H, \vec{I}] = 0 \quad \text{za} \quad H = H_{\text{jaki}},$$

$$\text{no} \quad [H, I_3] = 0 \quad \text{za} \quad H = H_{\text{jaki}} + H_{\text{e.m.}})$$

CASIMIROV OPERATOR – KOMUTIRA SA SVIM GENERATORIMA GRUPE

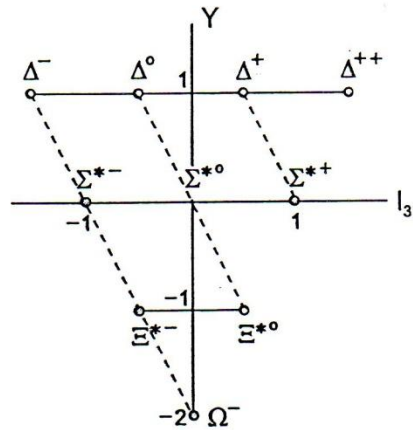
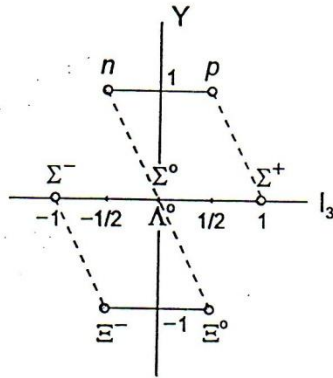
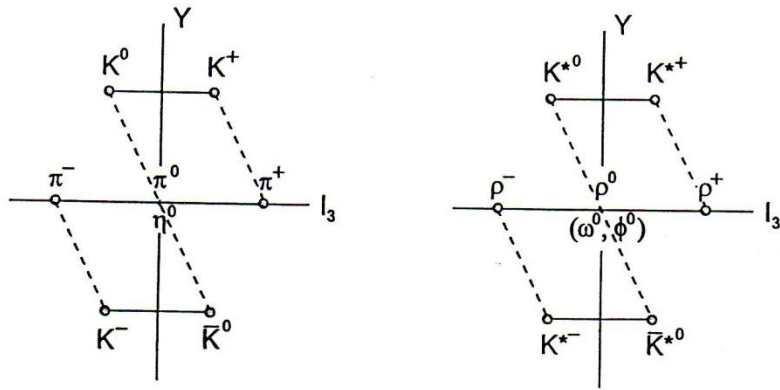
$$S^2 = S_x^2 + S_y^2 + S_z^2$$

Explicit construction: $S_{\pm} = S_x \pm iS_y$ $m = -s, -s + 1, \dots, s$

$[S_z, S_{\pm}] = \pm S_{\pm}$ $S_z |s, m\rangle = m |s, m\rangle$ $s = 0, 1/2, 1, 3/2, \dots$

$[S_+, S_-] = 2S_z$ $S^2 |s, m\rangle = s(s + 1) |s, m\rangle$

$[S^2, S_i] = 0$ $S_{\pm} |s, m\rangle = \sqrt{[(s \mp m)(s \pm m + 1)]} |s, m \pm 1\rangle$



35. CLEBSCH-GORDAN COEFFICIENTS, SPHERICAL HARMONICS, AND d FUNCTIONS

Note: A square-root sign is to be understood over every coefficient, e.g., for $-8/15$ read $-\sqrt{8/15}$.

J	J	...
M	M	...
m_1	m_2	Coefficients
...

$Y_l^0 = \sqrt{\frac{3}{4\pi}} \cos \theta$
 $Y_l^1 = -\sqrt{\frac{3}{8\pi}} \sin \theta e^{i\phi}$
 $Y_l^2 = \sqrt{\frac{5}{4\pi}} \left(\frac{3}{2} \cos^2 \theta - \frac{1}{2} \right)$
 $Y_l^2 = -\sqrt{\frac{15}{8\pi}} \sin \theta \cos \theta e^{i\phi}$
 $Y_l^2 = \frac{1}{4} \sqrt{\frac{15}{2\pi}} \sin^2 \theta e^{2i\phi}$

$Y_l^{-m} = (-1)^m Y_l^{m*}$
 $d_{m,0}^l = \sqrt{\frac{4\pi}{2l+1}} Y_l^m e^{-im\phi}$

$d_{m',m}^j = (-1)^{m-m'} d_{m,m'}^j = d_{j,-m,-m'}$
 $d_{0,0}^j = \cos \theta$
 $d_{1/2,1/2}^j = \cos \frac{\theta}{2}$
 $d_{1/2,-1/2}^j = -\sin \frac{\theta}{2}$
 $d_{1,1}^j = \frac{1 + \cos \theta}{2}$
 $d_{1,0}^j = \frac{\sin \theta}{\sqrt{2}}$
 $d_{1,-1}^j = \frac{1 - \cos \theta}{2}$

$d_{3/2,3/2}^j = \frac{1 + \cos \theta}{2} \cos \frac{\theta}{2}$
 $d_{3/2,1/2}^j = -\sqrt{3} \frac{1 + \cos \theta}{2} \sin \frac{\theta}{2}$
 $d_{3/2,-1/2}^j = \sqrt{3} \frac{1 - \cos \theta}{2} \cos \frac{\theta}{2}$
 $d_{3/2,-3/2}^j = -\frac{1 - \cos \theta}{2} \sin \frac{\theta}{2}$
 $d_{1,1/2}^j = \frac{3 \cos \theta - 1}{2} \cos \frac{\theta}{2}$
 $d_{1,1/2,-1/2}^j = -\frac{3 \cos \theta + 1}{2} \sin \frac{\theta}{2}$
 $d_{2,2}^j = \left(\frac{1 + \cos \theta}{2} \right)^2$
 $d_{2,1}^j = \frac{1 + \cos \theta}{2} \sin \theta$
 $d_{2,0}^j = \frac{\sqrt{6}}{4} \sin^2 \theta$
 $d_{2,-1}^j = -\frac{1 - \cos \theta}{2} \sin \theta$
 $d_{2,-2}^j = \left(\frac{1 - \cos \theta}{2} \right)^2$
 $d_{1,1}^j = \frac{1 + \cos \theta}{2} (2 \cos \theta - 1)$
 $d_{1,0}^j = -\sqrt{2} \sin \theta \cos \theta$
 $d_{1,-1}^j = \frac{1 - \cos \theta}{2} (2 \cos \theta + 1)$
 $d_{0,0}^j = \left(\frac{3}{2} \cos^2 \theta - \frac{1}{2} \right)$

Figure 35.1: The sign convention is that of Wigner (*Group Theory*, Academic Press, New York, 1959), also used by Condon and Shortley (*The Theory of Atomic Spectra*, Cambridge Univ. Press, New York, 1953), Rose (*Elementary Theory of Angular Momentum*, Wiley, New York, 1957), and Cohen (*Tables of the Clebsch-Gordan Coefficients*, North American Rockwell Science Center, Thousand Oaks, Calif., 1974). The coefficients here have been calculated using computer programs written independently by Cohen and at LBNL.

BARIONSKA REZONANCIJA

$I=3/2$ $\Delta(1232)$ $J^P=3/2^+$

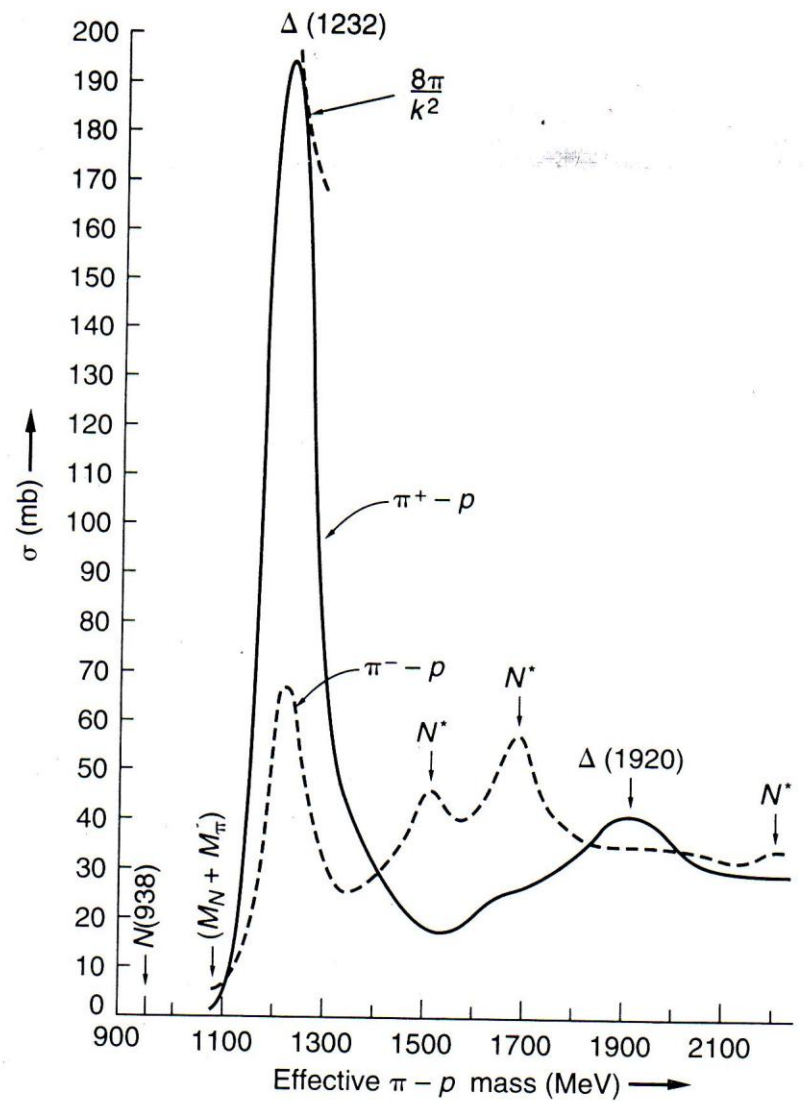
$I=1/2$ $N(1525)$ $J^P=3/2^-$

Za K.E. π 195 MeV $A_{3/2} \rightarrow A_{1/2}$

$$\frac{\sigma_{\pi^+p}}{\sigma_{\pi^-p}} \approx 3:1$$

Za K.E. π 600 MeV $A_{1/2} \rightarrow A_{3/2}$

$$\frac{\sigma_{\pi^-p \rightarrow \pi^0 p}}{\sigma_{\pi^-p \rightarrow \pi^- n}} = 2:1$$



In December 1947, Rochester and Butler published the cloud chamber photograph which turned out to be the production of a neutral K-meson: $K^0 \rightarrow \pi^+ + \pi^-$

In 1949, Powell published the decay of a charged Kaon: $K^+ \rightarrow \pi^+ + \pi^+ + \pi^-$

In 1950, Anderson discovered the Lambda baryon: $\Lambda \rightarrow p^+ + \pi^-$

All those particles seemed "strange" in the sense that they are produced copiously (10^{-23} s), but they decay relatively slowly (10^{-10} s)!

Gell-Mann assigned those particles a new quantum number called **strangeness** besides their respective charge:

- Production of two strange particles: $\pi^- + p^+ \rightarrow K^+ + \Sigma^-$

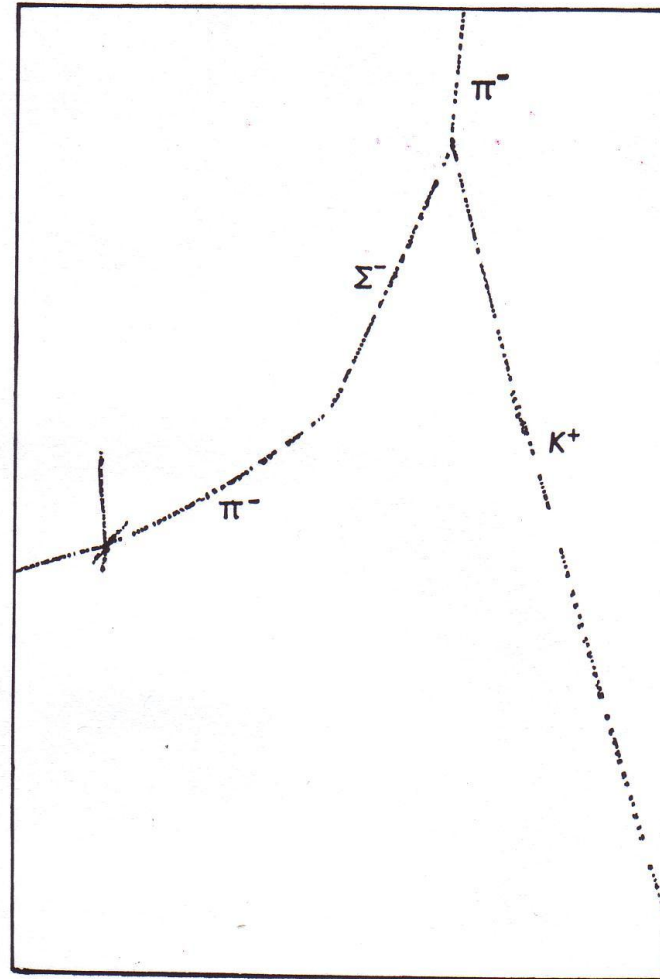
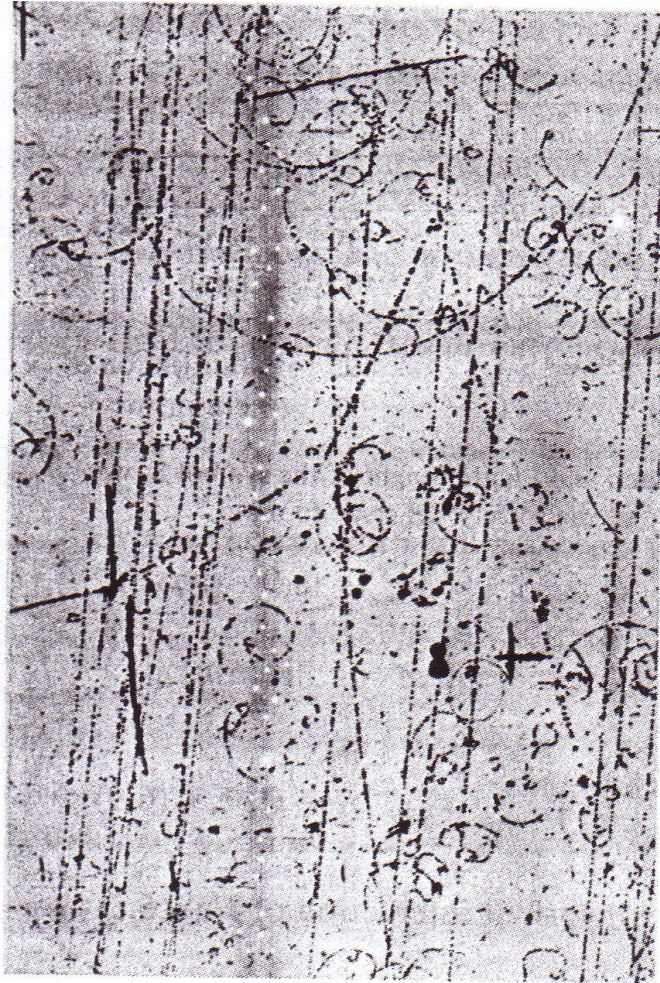
$$\pi^- + p^+ \rightarrow K^0 + \Sigma^0$$

$$\pi^- + p^+ \rightarrow K^0 + \Lambda$$

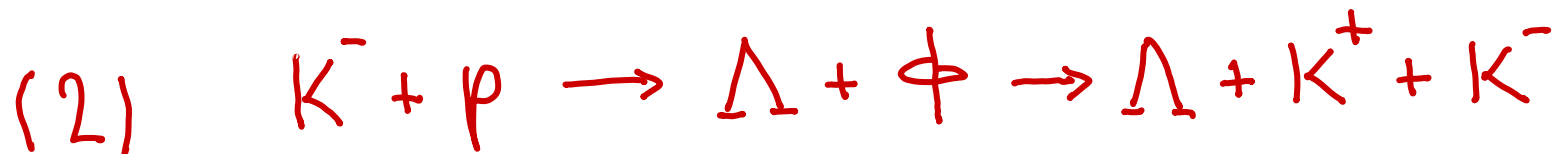
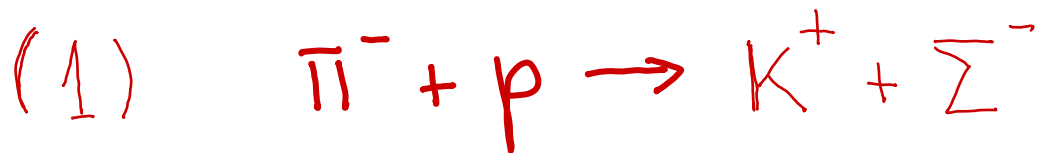
- Assign strangeness quantum number S: S=+1 for Σ and S=-1 for Λ with S=0 for p,n and π

**AMPLITUDE - MATRIČNE
ELEMENTE JAKIH PRIJELAZA -
MOŽEMO POVEZIVATI POMOĆU
IZOSPINSKE SIMETRIJE**

PRODUKCIJA STRANOSTI

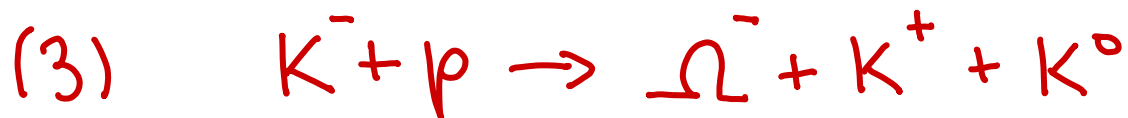


PRODUKCIJA STRANOSTI

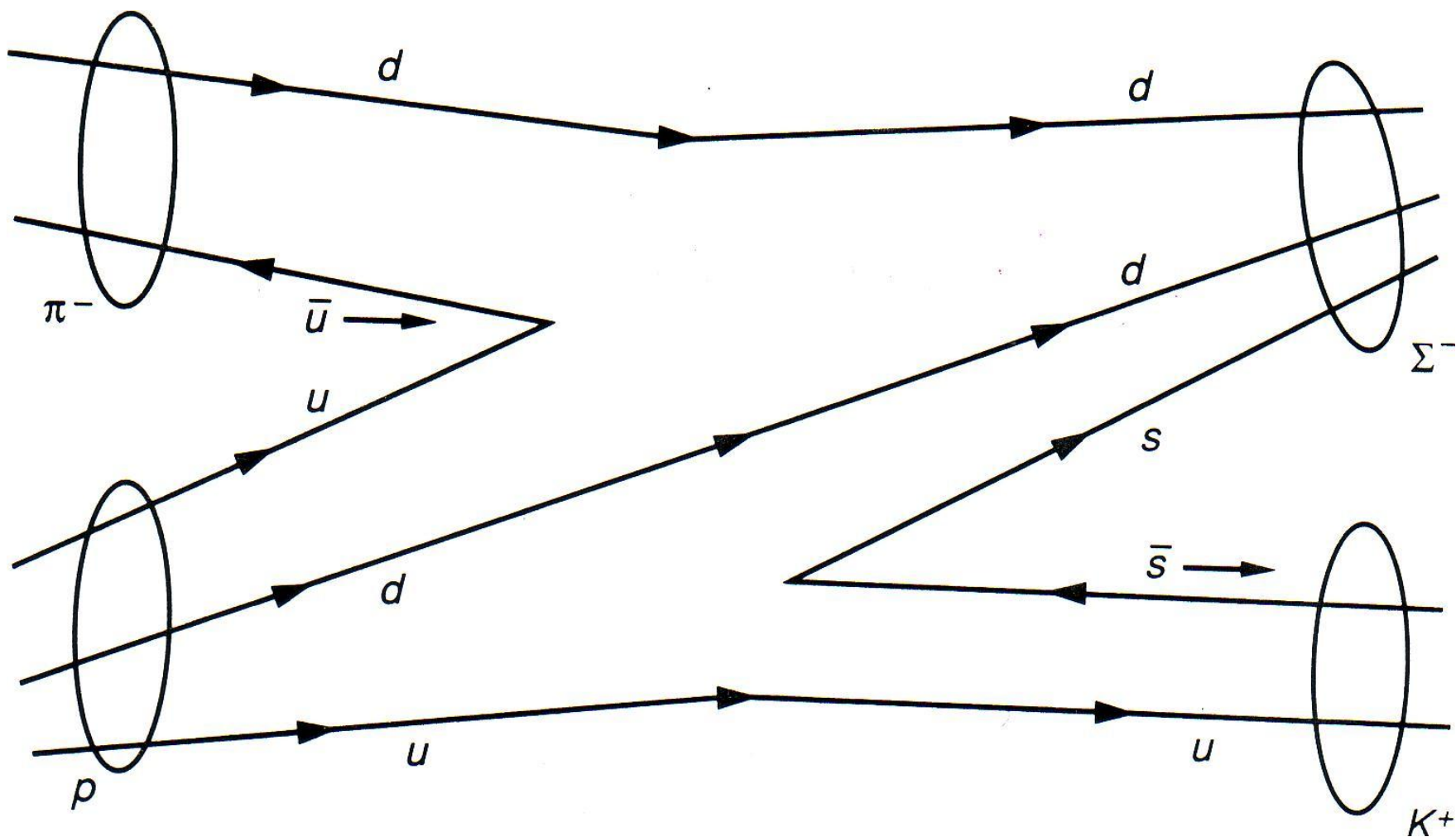


Okubo-Zweig-Iizuka
(OZI-) potisnuti

$K^+ K^-$	49%
$K^0 \bar{K}^0$	34%
9π	13%
$\pi^+ \pi^- \pi^0$	2%



DIJAGRAM KVARKOVSKOG TOKA



DOGADAJ Ω HIPERONA

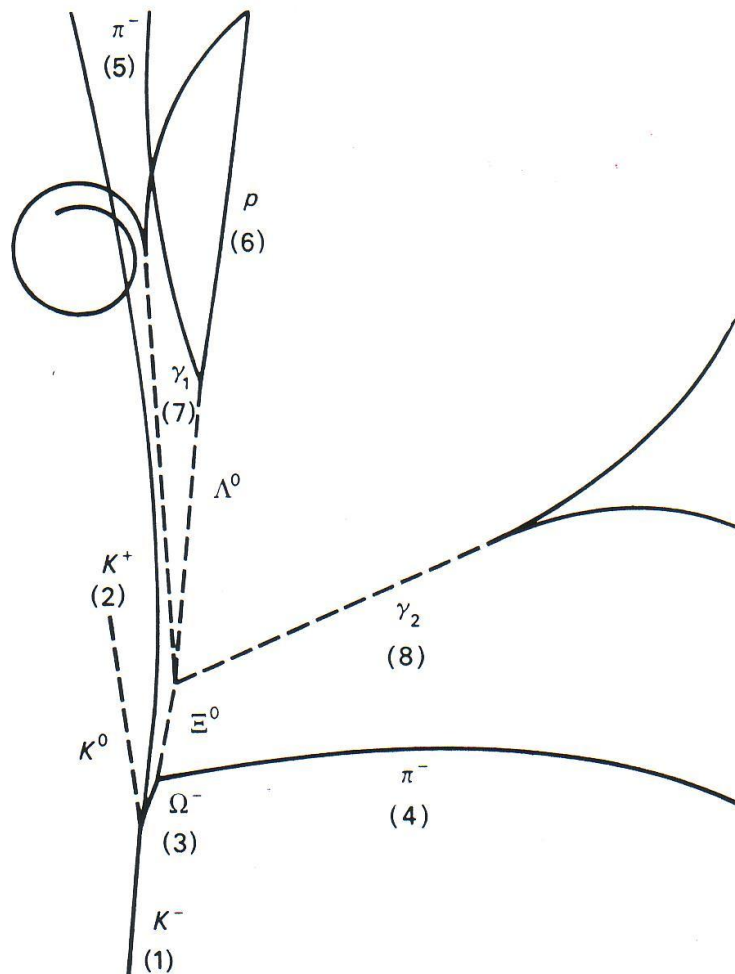
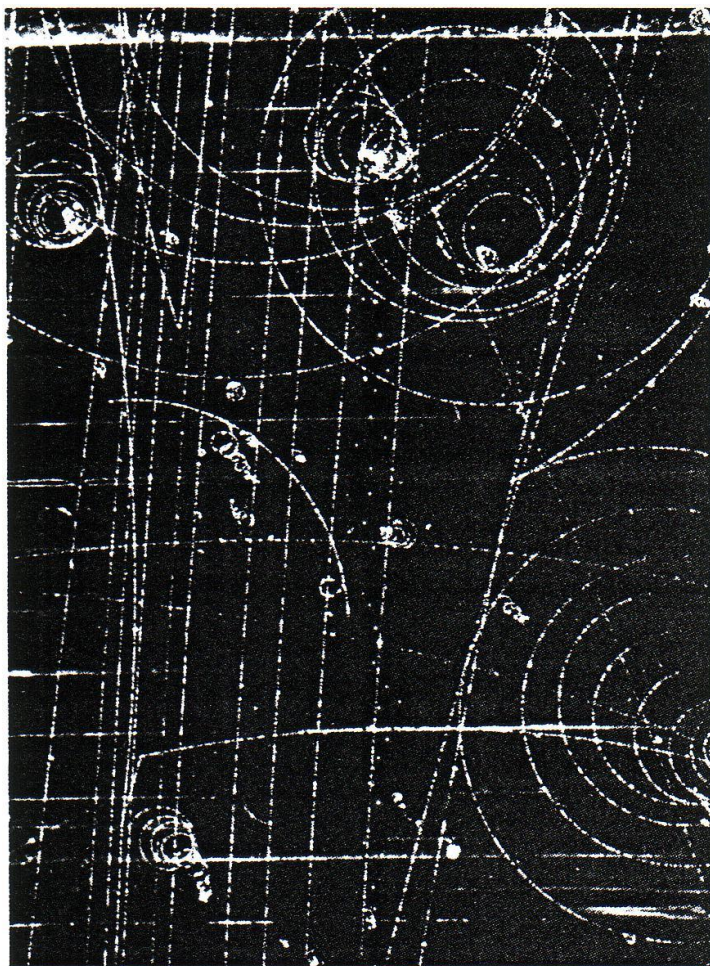
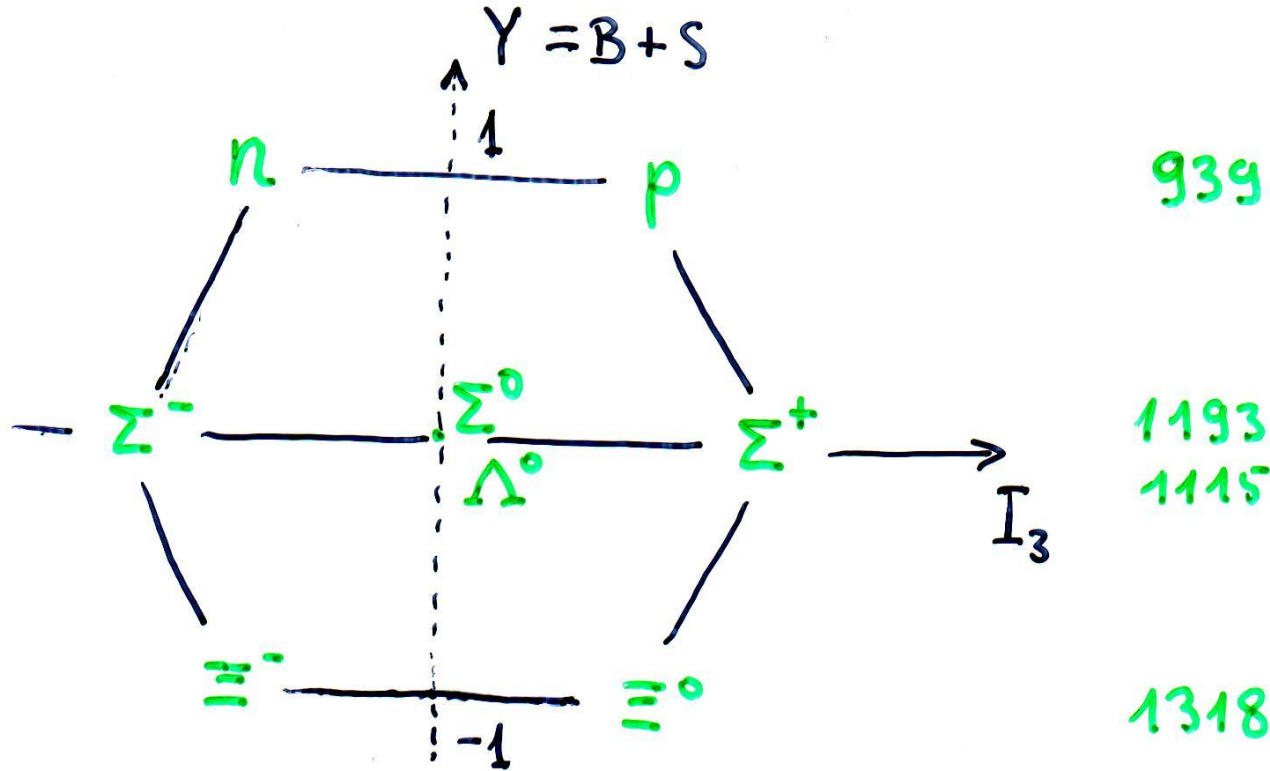


FIGURE 6.4

SU(3)

OSMEROSTRUKOG PUTA



~ 100 MeV

PRODUKCIJE NOVIH STANJA

1974: The J/Psi (charm) discovery

$$p+N \rightarrow J/\psi$$

... 1976 Nobel Prize

1977: The Upsilon (bottom) discovery

$$p+N \rightarrow \Upsilon$$

1983: The W and Z discovery

$$p + \bar{p} \rightarrow W/Z$$

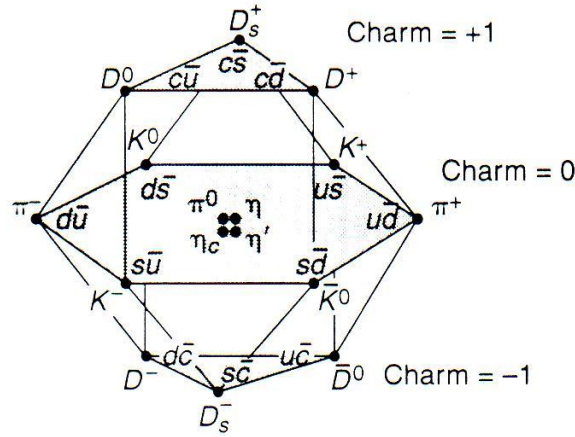
... 1984 Nobel Prize

TEŽÍ OKUSI

$SU(4)$

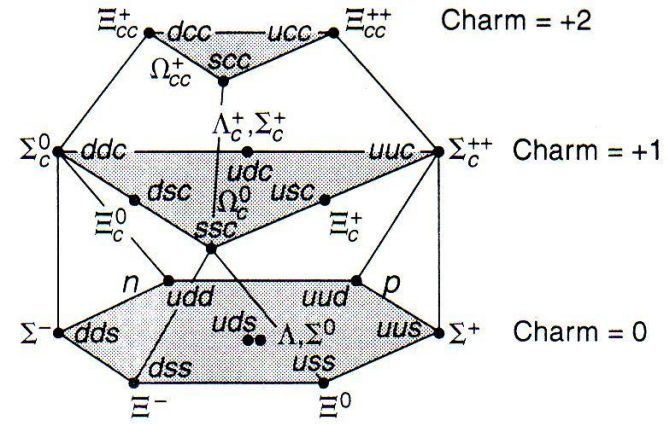
15-plet mezona
20-plet bariona

$\bar{F}E\check{C}_1$
stv. 192



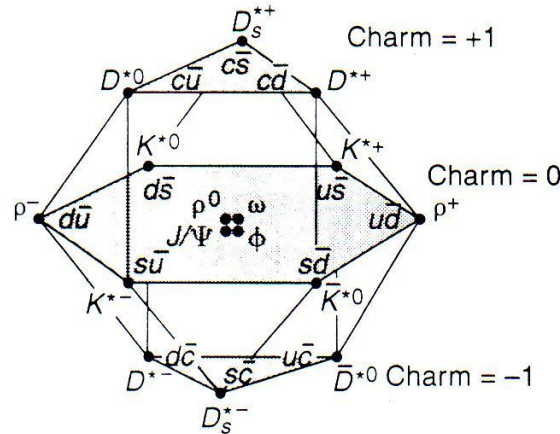
0- Mesons

(a)



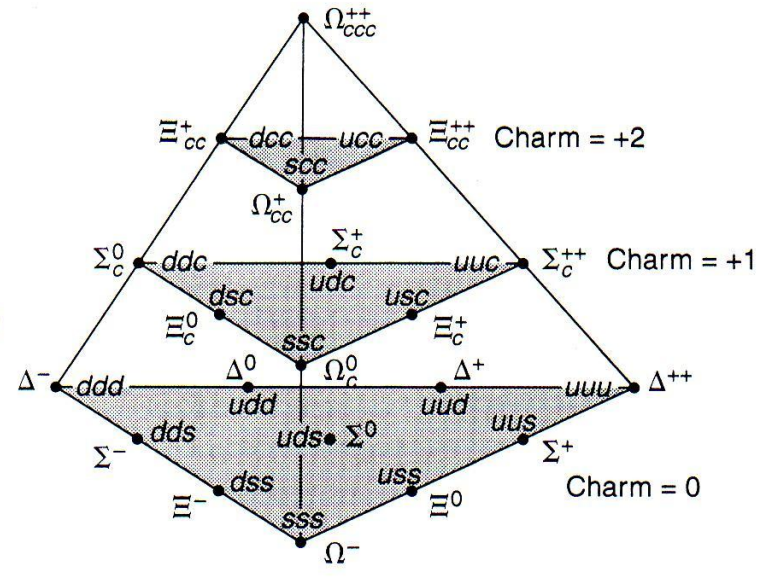
$\frac{1}{2}^+$ Baryons

(c)



1- Mesons

(b)



$\frac{3}{2}^+$ Baryons

(d)

TREBA IZUČITI DINAMIKU -SILU KVARKOVSKOG VEZANJA

$$\begin{array}{cccccc}
 \pi^+ & = & u\bar{d}, & K^+ & = & u\bar{s}, & K^0 & = & d\bar{s}, & \pi^0 & = & (u\bar{u} - d\bar{d})/\sqrt{2} \\
 D^+ & = & c\bar{d}, & D^0 & = & c\bar{u}, & D_s^+ & = & c\bar{s} & & & \dots \\
 B^+ & = & u\bar{b}, & B^0 & = & d\bar{b}, & B_s^0 & = & s\bar{b}, & B_c^+ & = & c\bar{b}
 \end{array}$$

$$\begin{array}{cccccc}
 p & = & uud, & n & = & udd, & \Sigma^+ & = & uus, & \Sigma^0 & = & uds \\
 \Sigma_c^+ & = & udc, & \Sigma_c^{++} & = & uuc, & \Xi_c^+ & = & usc, & \Xi_c^0 & = & dsc \\
 \Xi_{cc}^+ & = & dcc, & \Xi_{cc}^{++} & = & ucc, & \Omega_{cc}^+ & = & scc & & & \dots
 \end{array}$$

O SUDARIVAČIMA - FEČ 1.2.2

Table 1. Recent and future energy-frontier particle colliders. (Parameters listed for the LHC and the ILC are design values.)

Name	Type	\sqrt{s} (GeV)	L_{int} (pb^{-1})	Years of operation	Detectors	Location
LEP	e^+e^-	91.2 (LEP-1) 130-209 (LEP-2)	≈ 200 (LEP-1) ≈ 600 (LEP-2)	1989-95 (LEP-1) 1996-2000 (LEP-2)	ALEPH, OPAL, DELPHI, L3	CERN
SLC	e^+e^-	91.2	20	1992-98	SLD	SLAC
HERA	$e^\pm p$	320	500	1992-2007	ZEUS, H1	DESY
Tevatron	$p\bar{p}$	1800 (Run-I) 1960 (Run-II)	160 (Run-I) 6 K (Run-II, 06/09)	1987-96 (Run-I) 2000-??? (Run-II)	CDF, DØ	FNAL
LHC	pp	14000	10 K/yr ("low-L") 100 K/yr ("high-L")	2010? - 2013? 2013?? - 2016???	ATLAS, CMS	CERN
ILC	e^+e^-	500-1000	1 M???	???	???	???

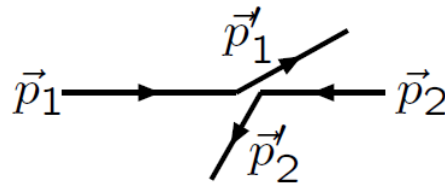
Table 1. Comparison of the LHC and Tevatron accelerator statistics.

	LHC (design)	Tevatron (achieved)
Center-of-mass energy	14 TeV	1.96 TeV
Number of bunches	2808	36
Bunch spacing	25ns	396ns
Energy stored in beam	360MJ	1MJ
Peak Luminosity	$10^{33} - 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	3.87×10^{32} (April 2010)
Integrated Luminosity / year	10-100 fb^{-1}	$> 2 \text{fb}^{-1}$ (2008)

PARAMETRI SUDARIVAČA:

- ENERGIJA
- LUMINOZNOST

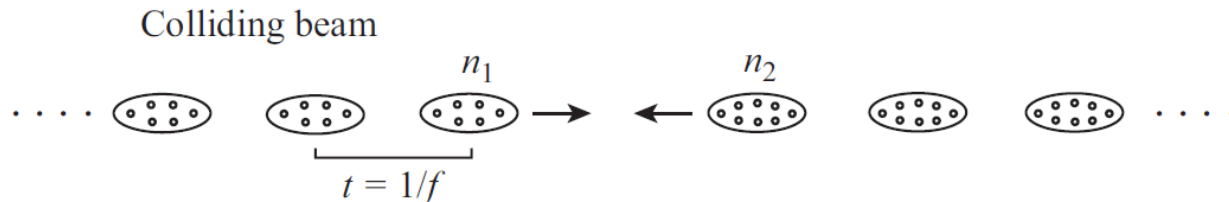
The energy:



$$s \equiv (p_1 + p_2)^2 = \begin{cases} (E_1 + E_2)^2 & \text{in the c.m. frame } \vec{p}_1 + \vec{p}_2 = 0, \\ m_1^2 + m_2^2 + 2(E_1 E_2 - \vec{p}_1 \cdot \vec{p}_2). & \end{cases}$$

$$E_{cm} \equiv \sqrt{s} \approx \begin{cases} 2E_1 \approx 2E_2 & \text{in the c.m. frame } \vec{p}_1 + \vec{p}_2 = 0, \\ \sqrt{2E_1 m_2} & \text{in the fixed target frame } \vec{p}_2 = 0. \end{cases}$$

The luminosity:

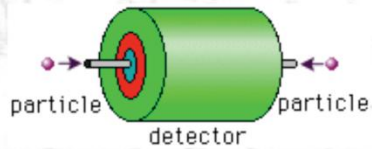


$$\mathcal{L} \propto f n_1 n_2 / a,$$

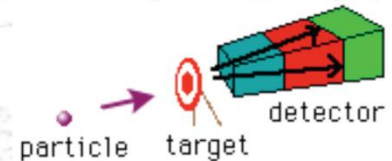
$$\# \text{particles/cm}^2/\text{s} \quad 10^{33} \text{ cm}^{-2} \text{s}^{-1} = 1 \text{ nb}^{-1} \text{ s}^{-1} \approx 10 \text{ fb}^{-1}/\text{year}$$

Hadron Electron Ring Accelerator

- Collider experiment: Electron-Proton collisions at HERA (DESY, Hamburg, Germany)

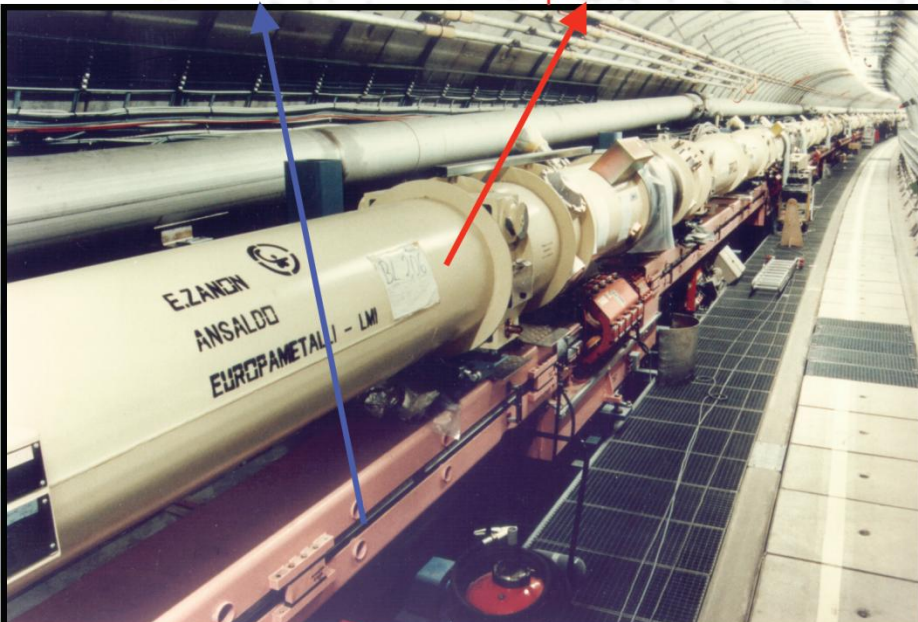


Equivalent to fixed target of
 $E_e = 50600 \text{ GeV}$:

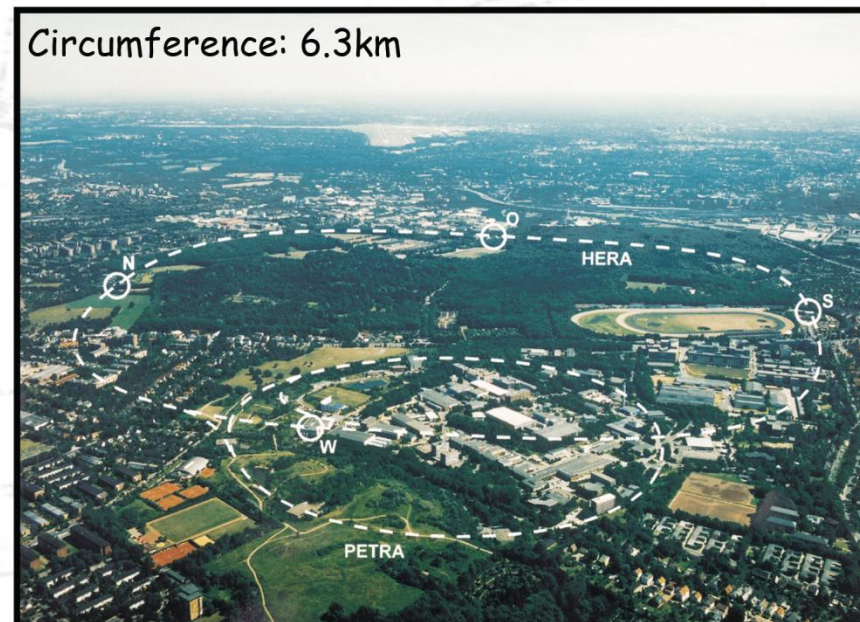


$E_e = 27.5 \text{ GeV}$

$E_p = 920 \text{ GeV}$

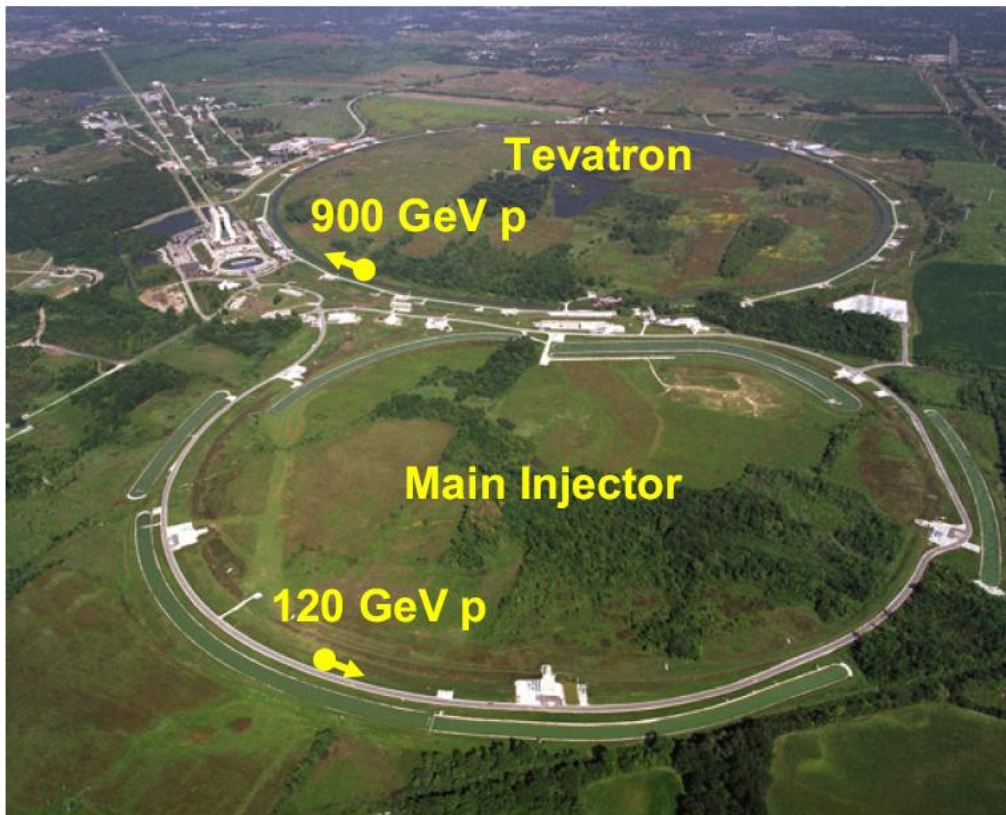


Circumference: 6.3km



SUDARI PROTONA i ANTIPROTONA NA TEVATRONU

★ $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV



Two main accelerators:

★ Main Injector

- Accelerates 8 GeV p to 120 GeV
- also \bar{p} to 120 GeV
- Protons sent to **Tevatron & MINOS**
- \bar{p} all go to **Tevatron**

★ Tevatron

- 4 mile circumference
- accelerates p/\bar{p} from 120 GeV to 900 GeV

LHC

supra-
vodljivi
magneti
opsega
27 km
energ.
Ecm
14TeV

